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Chapter 1

Tool Description

1.1 What TwoTowers 5.1 Is

TwoTowers 5.1 is an open-source software tool for the functional verification, security analysis, and performance evaluation of computer, communication and software systems modeled in the architectural description language Æmilia [8, 1, 9, 2], which is based on the stochastic process algebra EMPAgr [4, 10, 7].

The study of the properties of the Æmilia specifications is conducted in TwoTowers 5.1 through equivalence verification with diagnostics [17], symbolic model checking with diagnostics [14] via NuSMV 2.2.5 [12], information flow analysis with diagnostics [19], reward Markov chain solution [32, 22], and discrete event simulation [34].

1.2 Architecture of TwoTowers 5.1

TwoTowers 5.1 is composed of about 45,000 lines of ANSI C [26] code organized as depicted in Fig. 1.1.

TwoTowers 5.1 is equipped with a simple graphical user interface written in Tcl/Tk [30] through which the user can invoke the analysis routines by means of suitable menus. Each routine needs input files of certain types and writes its results onto files of other types. The graphical user interface takes care of the integrated management of the various file types needed by the different routines, which belong to the Æmilia compiler, the equivalence verifier, the model checker, the security analyzer, and the performance evaluator.

The compiler is in charge of parsing Æmilia specifications stored in .aem files and signalling possible lexical, syntax and static semantic errors through a .lis file. Based on the translation semantics for Æmilia into EMPAgr and the operational semantics for EMPAgr, if an Æmilia specification is correct the compiler can generate its integrated, functional or performance semantic model, which is written to a .ism, .fsm or .psm file, respectively. As a faster option that does not require printing the state space onto a file, the compiler can show only the size – in terms of number of states and transitions – of the semantic model, which is written to a .siz file. The integrated semantic model of an Æmilia specification for a given system is a state transition graph whose transitions are labeled with the name and the duration/priority/probability of the corresponding system activities. The functional semantic model is a state transition graph and the performance semantic model, which can be extracted only if the Æmilia specification is performance closed, is a continuous- or discrete-time Markov chain [32].

The equivalence verifier checks through the application of the Kanellakis-Smolka algorithm [24] whether two correct, finite-state Æmilia specifications are equivalent according to one of four different behavioral equivalences: strong bisimulation equivalence, weak bisimulation equivalence, strong (extended) Markovian bisimulation equivalence, and weak (extended) Markovian bisimulation equivalence [29, 10, 6]. The result of the verification is written to a .evr file. In the case of non-equivalence a distinguishing modal logic formula is reported as well, which is computed on the basis of the algorithm of [15] and is expressed in a verbose variant of the Hennessy-Milner logic [20] or one of its probabilistic extensions [27, 13].

The equivalence verifier allows a comparative study of two Æmilia specifications to be conducted, aiming at establishing whether they possess the same functional, security and performance properties in general.
Should the two Æmilia specifications be equivalent, in order to know whether they satisfy a particular functional property, security requirement, or performance guarantee, it is necessary to apply to one of the two Æmilia specifications the model checker, the security analyzer, or the performance evaluator, respectively.

![Figure 1.1: Tool architecture](image)

The model checker verifies through the BDD-based routines of NuSMV 2.2.5 [12] whether a set of functional properties expressed through verbose LTL formulas [14], which are stored in a .ltl file, are satisfied by a correct, finite-state Æmilia specification. The result of the check, together with a counterexample for each property that is not met, is written to a .mcr file.

The security analyzer checks through the equivalence verifier whether a correct, finite-state Æmilia specification satisfies non-interference or non-deducibility on composition [19], both of which establish the absence of illegal information flows from high security system components to low security system components. This requires the classification in an additional .sec file of the system activities that are high and low with respect to the security level. The result of the analysis is written to a .sar file, together with a modal logic formula expressed in a verbose variant of the Hennessy-Milner logic to explain a possible security violation.

Finally, the performance evaluator assesses the quantitative characteristics of correct, finite-state and performance closed Æmilia specifications. First, it can calculate the stationary/transient probability distribution for the state space of the performance semantic model of an Æmilia specification. The distribution is written to a .dis file. Second, the performance evaluator can calculate for an Æmilia specification a set of instant-of-time, stationary/transient performance measures specified through state and transition rewards [22] stored in a .rew file. The values of the measures are written to a .val file. The solution methods implemented for the stationary case are Gaussian elimination and an adaptive variant of symmetric stochas-
tic over-relaxation, while for the transient case uniformization is available [32]. Third, the performance evaluator can estimate via discrete event simulation the mean, variance or distribution of a set of performance measures specified through an extension of state and transition rewards, which are stored in a .sim file together with the number and the length of the simulation runs. The simulation, which can be applied also to Ũemilia specifications with infinitely many states and general distributions, is based on the method of independent replications with 90% confidence level [34] and can be trace driven, in which case the traces are stored in .trc files. The result of the simulation is written to a .est file.

1.3 What TwoTowers 5.1 Offers

From the user viewpoint, TwoTowers 5.1 supplies the following capabilities:

- Component-oriented modeling with Ũemilia:
  - Separation of system component behavior specification from system topology specification.
  - Support for the parameterization of system component behavior.
  - Indexing mechanism for defining parameterized system topologies.
  - Several data types: integer, bounded integer, real, boolean, list, array, and record.
  - Representation of continuous- and discrete-time systems.
  - Component activities with exponentially distributed, zero or unspecified durations.
  - Random number generators for sampling durations/probabilities from other distributions [23].
  - Prioritized and probabilistic choices among component activities.
  - Generative-reactive synchronizations among component activities [10].
  - Value passing across components (compiled concretely – if possible – or symbolically [5]).

- Companion languages for the parameterized specification of:
  - Functional properties expressed in a verbose variant of LTL.
  - Security levels.
  - Performance measures based on state and transition rewards [7].
  - Simulation experiments.

- Parsing of Ũemilia and companion specifications with the generation of listings that pinpoint lexical, syntactical and static semantical errors.

- Compilation of Ũemilia specifications into state transition graphs that are shown in a readable format, through the indication for each global state of the constituting local states of the components.

- Integrated framework for the study of functional, security and performance properties of Ũemilia specifications and the provision of diagnostic information in the case of negative outcome.

1.4 Case Studies

A complete and updated list of the case studies conducted with TwoTowers 5.1 (or earlier versions) is maintained at http://www.sti.uniurb.it/bernardo/twotowers/, where their Ũemilia and companion specifications as well as the related papers can be found.
1.5 History of TwoTowers

The development of TwoTowers started in 1996, then restarted from scratch in 1997. Its name stems from the two medieval towers – Asinelli (97 mt.) and Garisenda (48 mt.) – that are the symbol of Bologna, the city where the implementation of the tool started.

Version 1.0 was distributed in July 2001 for Linux and Unix operating systems only. Its input language was EMPA$_{gr}$, enriched with the symbolically treated data types integer, real, boolean, list, array, and record. Its graphical user interface contained a menu for a parser and a compiler of EMPA$_{gr}$ specifications into state transition graphs, an integrated analyzer for equivalence checking (strong Markovian bisimulation equivalence), a functional analyzer based on CWB-NC 1.2 [17] for model checking ($\mu$-calculus and GCTL* [14]) and equivalence/preorder checking with diagnostics (strong/weak bisimulation equivalence, may/must testing equivalence and preorder [18]), and a performance analyzer in charge of reward-based Markovian analysis through the solution methods of the commercial tool MarCA 3.0 [33] as well as discrete event simulation.

Version 2.0 was distributed in November 2002. As a faster compilation option not requiring any possibly huge file to be written, it provided the capability to report only the size of the semantic models underlying an EMPA$_{gr}$ specification. Unlike the previous version, it no longer relied on MarCA 3.0, as it had three built-in analysis routines – Gaussian elimination, an adaptive variant of symmetric stochastic over-relaxation, and uniformization – for the solution of reward Markov chains of arbitrary size. This allowed TwoTowers to be distributed free of charge to educational and non-profit organizations.

Version 3.0 was completed in October 2003 but not distributed. In this version EMPA$_{gr}$ was replaced by Æmilia, thus adopting a component-oriented modeling style leading to more confidence in the correctness of the system specifications as well as a higher degree of parameterization and reuse. Also the companion languages for the specification of functional properties and performance measures were modified according to the adopted component-oriented style and became more verbose, thus increasing their ease of use. The component-orientation reflected on a more readable state representation, as each global state could be described through its constituting local states corresponding to the components. On the data type side, bounded integers were introduced and the concrete treatment of data values of type different from integer, real, and list was implemented in addition to the original symbolic treatment.

Version 4.0 was completed in January 2004 but not distributed. Its graphical user interface was reorganized in order to contain a menu for equivalence verification with diagnostics fully based on built-in routines (strong/weak functional/Markovian bisimulation equivalence), a menu for model checking (based on CWB-NC 1.2 as before), a novel menu for security analysis, and a menu for performance evaluation (as before). The routines for security analysis required a companion language for the specification of the security levels of the component activities, and employed weak bisimulation equivalence checking to assess non-interference and non-deducibility on composition.

Version 5.0 was distributed in May 2004. In this version a symbolic model checker was adopted by replacing the one of CWB-NC 1.2 with NuSMV 2.1.2. Consequently, the companion language for the specification of functional properties was modified to express LTL formulas instead of $\mu$-calculus and GCTL* formulas.

Version 5.1 is being distributed since January 2006. Some minor modifications were done in order to make the tool available for the Windows operating system as well. Moreover the use of NuSMV 2.1.2 was replaced by the use of NuSMV 2.2.5.

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Chapter 2

Tool Installation and Execution

2.1 Introduction

In this chapter we explain how to install and run TwoTowers 5.1 on a computer with the Linux or Windows operating system.

2.2 Source Distribution

TwoTowers 5.1 is distributed through the compressed file `TwoTowers.tar.gz`. After moving this compressed file into a new directory, the source files can be extracted together with the related documentation and utilities through the following two commands (symbol `>` denotes the prompt of the operating system shell):

```plaintext
> gunzip TwoTowers.tar.gz
> tar -xvf TwoTowers.tar
```

which should result in the following directory structure:

```
  . bin
  |___ TTKernel.exe
  . docs
  |___ license.txt
      . manual.pdf
      . readme.txt
  . gui
  |___ TTGUI
  . src
  |___ Makefile
      . compiler
          |___ Makefile
          . aemilia_compiler.c
          . aemilia_parser.y
          . aemilia_scanner.l
          . listing_generator.c
          . ltl_parser.y
          . ltl_scanner.l
          . rew_parser.y
          . rew_scanner.l
          . sec_parser.y
          . sec_scanner.l
```
. sim_parser.y
. sim_scanner.l
. symbol_handler.c
 . driver
 |_. Makefile
 . driver.c
 . equivalence_verifier
 |_. Makefile
 . equivalence_verifier.c
 . headers
 |_. Library.h
 . aemilia_compiler.h
 . aemilia_parser.h
 . aemilia_scanner.h
 . driver.h
 . equivalence_verifier.h
 . file_handler.h
 . list_handler.h
 . listing_generator.h
 . ltl_parser.h
 . ltl_scanner.h
 . markov_solver.h
 . memory_handler.h
 . number_handler.h
 . nusmv.connector.h
 . rew_parser.h
 . rew_scanner.h
 . sec_parser.h
 . sec_scanner.h
 . security_analyzer.h
 . sim_parser.h
 . sim_scanner.h
 . simulator.h
 . string_handler.h
 . symbol_handler.h
 . table_handler.h
 . model_checker
 |_. Makefile
 . nusmv.connector.c
 . performance_evaluator
 |_. Makefile
 . markov_solver.c
 . simulator.c
 . security_analyzer
 |_. Makefile
 . security_analyzer.c
 . utilities
 |_. Makefile
 . file_handler.c
 . list_handler.c
 . memory_handler.c
 . number_handler.c
 . string_handler.c
2.3 Installation Procedure

The procedure for installing TwoTowers 5.1 comprises a couple of quick and easy steps.

2.3.1 Linux

On a Linux machine, make sure that the following packages are available:


The first step consists of compiling the ANSI C source files through the following commands:

```
> cd <TwoTowers 5.1 directory>/src/
> make
> make clean
```

which should result in the following executable file:

```
<TwoTowers 5.1 directory>/bin/TTKernel
```

The second step consists of creating a symbolic link to the above executable file through the following command:

```
> ln -s <TwoTowers 5.1 directory>/bin/TTKernel TTKernel
```
given in a directory whose pathname occurs in the shell variable `PATH`.

2.3.2 Windows

The executable file for Windows is already available at:

```
<TwoTowers 5.1 directory>/bin/TTKernel.exe
```

Should you need to generate it again, make sure that the following packages are available in `Program Files\GnuWin32`:

- flex (lexical analyzer generator, http://gnuwin32.sourceforge.net/packages/flex.htm)
and that the following packages are available as well:

- make (program maintainance utility, [http://www.mingw.org/](http://www.mingw.org/))

Then compile the C source files through the following commands:

```
> make
> make clean
```

which should create the following executable file:

```
<TwoTowers 5.1 directory>\bin\TTKernel.exe
```

### 2.4 Running the Tool

Running the tool is very simple.

#### 2.4.1 Linux

On a Linux machine, make sure that the following packages are available:

- wish (windowing shell for Tcl/Tk 8.0 or higher, [http://www.tcl.tk/software/tcltk/8.0.tml](http://www.tcl.tk/software/tcltk/8.0.tml))
- NuSMV 2.2.5 (symbolic model checker, [http://nusmv.irst.itc.it/](http://nusmv.irst.itc.it/))

Then type the following command to run the tool:

```
> wish <TwoTowers 5.1 directory>/gui/TTGUI &
```

To simplify this, we suggest to define an alias like the following:

```
alias tt 'wish <TwoTowers 5.1 directory>/gui/TTGUI &'
```

so that the command to run the tool simply becomes:

```
> tt
```

In order to be able to use the model checker, we also suggest to make sure that the following symbolic links:

```
> ln -s <NuSMV 2.2.5 directory>/NuSMV NuSMV
> ln -s <NuSMV 2.2.5 directory>/src/ltl/ltl2smv/ltl2smv ltl2smv
```

have been created in a directory whose pathname occurs in the shell variable `path`.

#### 2.4.2 Windows

On a Windows machine, make sure that the following package is available in `\Program Files\Tcl`:

- wish (windowing shell for Tcl/Tk 8.0 or higher, [http://www.tcl.tk/software/tcltk/8.0.tml](http://www.tcl.tk/software/tcltk/8.0.tml))

and that the following package is available in `\Program Files\NuSMV-2.2.5`:

- NuSMV 2.2.5 (symbolic model checker, [http://nusmv.irst.itc.it/](http://nusmv.irst.itc.it/))

Then give the following command to run the tool:

```
<TwoTowers 5.1 directory>\win_utils\tt_exec
```
Chapter 3

The Æmilia Compiler

3.1 Introduction

TwoTowers 5.1 accepts only system models that are written in the architectural description language Æmilia [9, 2] and are stored in .aem files.

An Æmilia description represents an architectural type [8, 1]. This is an intermediate abstraction between a single system and an architectural style [31]. It consists of a family of systems sharing certain constraints on the observable behavior of the system components as well as on the system topology. As shown in Table 3.1, the description of an architectural type in Æmilia starts with the name and the formal parameters of the architectural type and is composed of three sections.

| ARCHI_TYPE | <name and formal parameters> |
| ARCHI_ELEM_TYPES |  <definition of the first architectural element type> |
| ELEM_TYPE |  :  |
| ELEM_TYPE |  <definition of the last architectural element type> |
| ARCHI_TOPOLOGY |  <declaration of the architectural element instances> |
| ARCHI_INTERACTIONS |  <declaration of the architectural interactions> |
| ARCHI_ATTACHMENTs |  <declaration of the architectural attachments> |
| [BEHAV_VARIATIONS |  <declaration of the behavioral hidings> |
| [BEHAV_HIDINGS |  ]
| [BEHAV_RESTRICTIONS |  <declaration of the behavioral restrictions> |
| [BEHAV_RENAMINGS |  ]
| END | |

Table 3.1: Structure of an Æmilia description

The first section defines the types of components that characterize the system family. In order to include both the computational components and the connectors among them, these types are called architectural element types (AETs). The definition of an AET starts with its name and formal parameters and consists of the specification of its behavior and its interactions. The behavior has to be provided in the form of a list of sequential defining equations written in a verbose variant of the stochastic process algebra EMPA gr [4, 10, 7]. The interactions are those EMPA gr action types occurring in the behavior that act as interfaces for the AET. Each of them has to be equipped with two qualifiers, which establish whether it is an input or output
interaction and the multiplicity of the communications in which it can be involved, respectively. All the other action types occurring in the behavior are assumed to represent internal activities.

The second section defines the architectural topology. This is specified in three steps. First we have the declaration of the instances of the AETs (called AEs) with their actual parameters, which represent the real system components and connectors. Then we have the declaration of the architectural (as opposed to local) interactions, which are those interactions of the AEs that act as interfaces for the whole system family. Finally we have the declaration of the directed architectural attachments among the local interactions of the AEs, which make the AEs communicate with each other.

The third section, which is optional, defines some variations of the observable behavior of the system family. This is accomplished by declaring some action types occurring in the behavior of certain AEs to be unobservable, prevented from occurring, or renamed into other action types.

### 3.2 Keywords and Comments

Here is the complete list of the keywords of Æmilia that can occur in .aem files:

| ARCHI_TYPE | BEHAV_HIDINGS | const | max | beta | first |
| ARCHI_ELEM_TYPES | HIDE | local | abs | normal | tail |
| ELEM_TYPE | INTERNALS | stop | ceil | pareto | concat |
| BEHAVIOR | INTERACTIONS | invisible | floor | b_pareto | insert |
| INPUT_INTERACTIONS | ALL | exp | power | d_uniform | remove |
| OUTPUT_INTERACTIONS | BEHAV_RESTRICTIONS | inf | epower | bernoulli | length |
| UNI | RESTRICT | choice | loge | binomial | array |
| AND | OBS_INTERNALS | cond | log10 | poisson | array_cons |
| OR | OBS_INTERACTIONS | void | sqrt | neg_binomial | read |
| ARCHI_TOPOLOGY | ALL_OBSERVABLES | prio | sin | geometric | write |
| ARCHI_ELEM_INSTANCES | BEHAV_RENAMINGS | rate | cos | pascal | record |
| ARCHI_INTERACTIONS | RENAME | weight | c_uniform | boolean | record_cons |
| ARCHI_ATTACHMENTS | AS | integer | erlang | true | get |
| FROM | FOR_ALL | real | gamma | false | put |
| TO | IN | mod | exponential | list |
| BEHAV_VARIATIONS | END | min | weibull | list_cons |

where the upper-case keywords in the two leftmost columns refer in general to the three sections of an Æmilia specification, while the lower-case keywords of the other four columns are used within specific parts of an Æmilia specification like the architectural type formal parameters, the AET formal parameters, the AET behavior, and the AEI actual parameters.

In addition to the keywords above, there are the following keywords that belong to the companion languages and can occur in .evr, .ltl, .sec, .sar, .rew, and .sim files:

| PROPERTY | DEADLOCK_FREE | OBS_NRESTR_INTERNALS |
| IS | FOR_ALL_PATHS | OBS_NRESTR_INTERACTIONS |
| TRUE | FOR_ALL_PATHS_ALL_STATES_SAT | ALL_OBS_NRESTR |
| FALSE | FOR_ALL_PATHS_SOME_STATE_SAT | MEASURE |
| NOT | EXISTS_PATH | ENABLED |
| EXISTS_TRANS | EXISTS_PATH_ALL_STATES_SAT | STATE_REWARD |
| EXISTS_WEAK_TRANS | EXISTS_PATH_SOME_STATE_SAT | TRANS_REWARD |
| FOR_ALL_TRANS | STRONG_UNTIL | RUN_LENGTH_ON_EXEC |
| FOR_ALL_WEAK_TRANS | WEAK_UNIFORM | RUN_LENGTH |
| EXISTS_TRANS_SET | NEXT_STATE_SAT | RUN_NUMBER |
| EXISTS_WEAK_TRANS_SET | ALL_FUTURE_STATES_SAT | MEAN |
| FOR_ALL_TRANS_SETS | SOME_FUTURE_STATE_SAT | VARIANCE |
| FOR_ALL_WEAK_TRANS_SETS | UNTIL | DISTRIBUTION |
| LABEL | RELEASES | REWARD |
3.3 Identifiers

The user-defined identifiers denote architectural type names, AET names, AEI names, behavior names, action type names, formal parameter names, local variable names, record field names, property names, and measure names. Every user-defined identifier occurring in a .aem, .ltl, .sec, .rew, or .sim file must be a sequence of upper- and lower-case letters, decimal digits, and underscores, which starts with a letter and is different from any of the keywords listed in Sect. 3.2. Every user-defined identifier occurring in a .ltl, .sec, .rew, or .sim file must have previously occurred in a .aem file, unless it denotes a property or a measure.

Except for architectural type names, AET names, and AEI names, every user-defined identifier is internally represented (and consequently written to output files) through the dot notation by prefixing it with the name of the context in which it is defined/used, hence the user is free to give the same name to several entities in different contexts. The internal representation of the type of an action stemming from the synchronization of several actions is given by the concatenation of the internal representation of the types of the synchronizing actions, using symbol # as a separator.

3.4 Data Types, Operators, and Expressions

In this section we provide the syntax for typed identifier declaration and expressions, we define the value domains for the data types available in Æmilia, and we introduce the related operators by specifying their precedence and associativity whenever necessary. In order to describe the syntax, we adopt the BNF notation, with terminal symbols enclosed within double quotes, non-terminal symbols enclosed within angular parentheses, and optional parts enclosed within square brackets.

### 3.4.1 Typed Identifier Declarations and Expressions

A typed identifier occurring in a .aem file represents a constant formal parameter of the architectural type or one of its AETs, a variable formal parameter or a local variable of a behavior, or an action priority, rate, or weight. A typed identifier can be declared within the header of an architectural type, AET, or behavior in the following C-like way:

```
<data_type> <identifier>
```

with <data_type> being defined by:

```
<data_type> ::= <normal_type> 
  | <special_type> 

<normal_type> ::= "integer"
  | "integer" 
    "(" <expr> ".." <expr> ")"
  | "real"
```

where the keywords in the two leftmost columns (except for the last two keywords) are used within modal and temporal logic formulas, while the other keywords are used to express security levels as well as performance measures and simulation experiments.

Comments can be inserted wherever in a .aem, .ltl, .sec, .rew or .sim file. A comment starts with symbol % and terminates at the end of the line.
| "boolean" |
| "list" "(" <normal_type> ")" |
| "array" "(" <expr> "," <normal_type> ")" |
| "record" "(" <field_decl_sequence> ")" |

<special_type> ::= "prio"
| "rate"
| "weight"

An expression – denoted by <expr> in the following – is composed of atomic elements, given by typed identifiers, numeric constants, and truth values, possibly combined through the available operators. The type of an expression is determined by the type of its atomic elements and the codomain of the operators occurring in it, while the order in which the infix operators have to be applied to evaluate the expression is given by their precedence and associativity. The order can be altered using parentheses ( ).

### 3.4.2 Integers, Bounded Integers, and Reals

The type **integer** denotes the set of integer numbers that can be represented in the used computer according to the ANSI C standard. A special case is given by the bounded integer set defined as follows:

```
"integer" "(" <expr> "." <expr> ")"
```

which denotes the set of integers between the value of the first expression and the value of the second expression. Both expressions must be integer valued, free of undeclared identifiers, and free of invocations to pseudo-random number generators. Moreover, the value of the first expression cannot be greater than the value of the second expression.

The type **real** denotes the set of real numbers in fixed-point notation that can be represented in the used computer according to the ANSI C standard.

#### Arithmetical Operators

The following four binary arithmetical operators are available in Æmilia:

```
<expr> ::= <expr> "+" <expr>
| <expr> "-" <expr>
| <expr> "*" <expr>
| <expr> "/" <expr>
```

with the division requiring the second operand to be different from zero and always returning a real number. All the operators above are left associative, with the multiplicative ones taking precedence over the additive ones. The unary `-` operator is not explicitly available as its effect can be achieved through a multiplication by -1.

#### Relational Operators

The following six binary relational operators are available in Æmilia:

```
<expr> ::= <expr> "=" <expr>
| <expr> "+=" <expr>
| <expr> "-=" <expr>
| <expr> "*=" <expr>
| <expr> "/=" <expr>
```

All of them are non-associative. The arithmetical operators take precedence over them.
Mathematical Functions

The following thirteen mathematical functions are available in Æmilia:

\[ \text{expr} ::= \text{"mod" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"abs" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"ceil" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"floor" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"min" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"max" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"power" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"epower" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"loge" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"log10" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"sqrt" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"sin" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"cos" } \left(\text{" } \text{expr} \text{"} \right) \]

where:

- \text{mod} computes the modulus of its first argument with respect to its second argument. Both arguments must be integer, with the second one greater than zero.
- \text{abs} computes the absolute value of its argument.
- \text{ceil} (resp. \text{floor}) computes the smallest (resp. greatest) integer greater (resp. smaller) than or equal to its argument.
- \text{min} (resp. \text{max}) computes the minimum (resp. maximum) of its two arguments.
- \text{power} computes the power of its first argument raised to its second argument. It cannot be applied to a pair of arguments such that the first one is zero and the second one is not positive, or the first one is negative and the second one is real.
- \text{epower} computes the power of e raised to its argument.
- \text{loge} (resp. \text{log10}) computes the natural (resp. base-10) logarithm of its argument, which must be greater than zero.
- \text{sqrt} computes the square root of its argument, which cannot be negative.
- \text{sin} (resp. \text{cos}) computes the sine (resp. cosine) of its argument expressed in radians.

Pseudo-random Number Generators

The following sixteen pseudo-random number generators [23] are available in Æmilia:

\[ \text{expr} ::= \text{"c_uniform" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"erlang" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"gamma" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"exponential" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"weibull" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"beta" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"normal" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"pareto" } \left(\text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"b_pareto" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"d_uniform" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\[ \mid \text{"bernoulli" } \left(\text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"}, \text{" } \text{expr} \text{"} \right) \]
\textbf{c\_uniform} generates a random number following a continuous uniform distribution between its two arguments, with the second one greater than the first one:

\[
\text{pdf}_{\text{c\_uniform}}(x) = \frac{1}{\text{expr2} - \text{expr1}} \quad \text{for } \text{expr1} \leq x \leq \text{expr2}
\]

\textbf{erlang} generates a random number following an Erlang distribution with rate parameter given by its first argument, which must be greater than zero, and shape parameter given by its second argument, which cannot be less than one:

\[
\text{pdf}_{\text{erlang}}(x) = x^{\text{expr2}-1} \cdot e^{-\text{expr1} \cdot x} \cdot \frac{1}{(\text{expr2} - 1)! \cdot (1/\text{expr1})^{\text{expr2}}} \quad \text{for } x \geq 0
\]

\textbf{gamma} generates a random number following a gamma distribution with rate parameter given by its first argument, which must be greater than zero, and shape parameter given by its second argument, which must be greater than zero:

\[
\text{pdf}_{\text{gamma}}(x) = \frac{(\text{expr1} \cdot x)^{\text{expr2}-1} \cdot e^{-\text{expr1} \cdot x}}{(1/\text{expr1}) \cdot \Gamma(\text{expr2})} \quad \text{for } x \geq 0,
\]

where \(\Gamma(y) = \int_{0}^{\infty} z^{y-1} \cdot e^{-z} dz\)

\textbf{exponential} generates a random number following an exponential distribution with rate parameter given by its argument, which must be greater than zero:

\[
\text{pdf}_{\text{exponential}}(x) = \text{expr} \cdot e^{-\text{expr} \cdot x} \quad \text{for } x \geq 0
\]

\textbf{weibull} generates a random number following a Weibull distribution with rate parameter given by its first argument, which must be greater than zero, and shape parameter given by its second argument, which must be greater than zero:

\[
\text{pdf}_{\text{weibull}}(x) = \frac{\text{expr2} \cdot x^{\text{expr2}-1}}{1/(\text{expr1})^{\text{expr2}}} \cdot e^{-\text{expr1} \cdot (x)^{\text{expr2}}} \quad \text{for } x \geq 0
\]

\textbf{beta} generates a random number following a beta distribution with shape parameters given by its two arguments, which must be greater than zero:

\[
\text{pdf}_{\text{beta}}(x) = \frac{x^{\text{expr1}-1} \cdot (1 - x)^{\text{expr2}-1}}{\beta(\text{expr1}, \text{expr2})} \quad \text{for } 0 \leq x \leq 1,
\]

where \(\beta(y, z) = \frac{\Gamma(y) \cdot \Gamma(z)}{\Gamma(y + z)}\)

\textbf{normal} generates a random number following a normal distribution with mean given by its first argument and standard deviation given by its second argument, which must be greater than zero:

\[
\text{pdf}_{\text{normal}}(x) = \frac{1}{\text{expr2} \cdot \sqrt{2 \cdot \pi}} \cdot e^{-\frac{(x - \text{expr1})^2}{2 \cdot \text{expr2}^2}}
\]

\textbf{pareto} generates a random number following a Pareto distribution with shape parameter given by its argument, which must be greater than zero:

\[
\text{pdf}_{\text{pareto}}(x) = \text{expr} \cdot x^{-(\text{expr1} + 1)} \quad \text{for } x \geq 1
\]

\textbf{b\_pareto} generates a random number following a Pareto distribution with shape parameter given by its first argument, which must be greater than zero, bounded between its other two arguments, with the second argument not less than one but less than the third argument:

\[
\text{pdf}_{\text{b\_pareto}}(x) = \frac{\text{expr1} \cdot \text{expr2}^{\text{expr1}}}{1 - (\text{expr2}/\text{expr3})^{\text{expr1}}} \cdot x^{-(\text{expr1} + 1)} \quad \text{for } \text{expr2} \leq x \leq \text{expr3}
\]
• **d_uniform** generates a random number following a discrete uniform distribution between its two arguments, which must be integer with the second one greater than the first one:

\[
\text{pmf}_{\text{d_uniform}}(x) = \frac{1}{\text{expr2} - \text{expr1} + 1} \quad \text{for } \text{expr1} \leq x \leq \text{expr2}
\]

• **bernoulli** generates a random number following a Bernoulli distribution where the two possible values are given by its first two arguments and the probability of choosing the first value is given by its third argument, which must be in the open interval between zero and one:

\[
\text{pmf}_{\text{bernoulli}}(\text{expr1}) = \text{expr3} \quad \text{and} \quad \text{pmf}_{\text{bernoulli}}(\text{expr2}) = 1 - \text{expr3}
\]

• **binomial** generates a random number following a binomial distribution with probability of success given by its first argument, which must be in the open interval between zero and one, and number of trials given by its second argument, which must be an integer not less than one:

\[
\text{pmf}_{\text{binomial}}(x) = \binom{\text{expr2}}{x} \cdot \text{expr1}^x \cdot (1 - \text{expr1})^{\text{expr2} - x} \quad \text{for } 0 \leq x \leq \text{expr2}
\]

• **poisson** generates a random number following a Poisson distribution with mean given by its argument, which must be greater than zero:

\[
\text{pmf}_{\text{poisson}}(x) = \frac{\text{expr}^x}{x!} \cdot e^{-\text{expr}} \quad \text{for } x \geq 0
\]

• **neg_binomial** generates a random number following a negative binomial distribution with probability of success given by its first argument, which must be in the open interval between zero and one, and number of successes given by its second argument, which must be an integer not less than one:

\[
\text{pmf}_{\text{neg_binomial}}(x) = \binom{\text{expr2} + x - 1}{\text{expr2} - 1} \cdot \text{expr1}^{\text{expr2}} \cdot (1 - \text{expr1})^x \quad \text{for } x \geq 0
\]

• **geometric** generates a random number following a geometric distribution with probability of success given by its argument, which must be in the open interval between zero and one:

\[
\text{pmf}_{\text{geometric}}(x) = \text{expr} \cdot (1 - \text{expr})^{x-1} \quad \text{for } x \geq 1
\]

• **pascal** generates a random number following a Pascal distribution with probability of success given by its first argument, which must be in the open interval between zero and one, and number of successes given by its second argument, which must be an integer not less than one:

\[
\text{pmf}_{\text{pascal}}(x) = \binom{x - 1}{\text{expr2} - 1} \cdot \text{expr1}^{\text{expr2}} \cdot (1 - \text{expr1})^{x - \text{expr2}} \quad \text{for } x \geq \text{expr2}
\]

### 3.4.3 Booleans

The type **boolean** denotes the set composed of the two truth values **true** and **false**. The following three logical operators are available in Æmilia:

\[
<\text{expr}> ::= <\text{expr}> "&&" <\text{expr}> \\
| <\text{expr}> "||" <\text{expr}> \\
| "!" <\text{expr}>
\]

with the logical negation (!) being right associative and taking precedence over the logical conjunction (&&) and the logical disjunction (||), which are left associative and subject to short-circuitation. The relational operators and the arithmetical operators take precedence over the logical ones.
### 3.4.4 Lists

The type `list`, which denotes a possibly empty, variable-length sequence of elements of the same type, is defined as follows:

```
"list" "(" <normal_type> ")"
```

where `<normal_type>` is the type of its elements.

The following seven list-related functions are available in Æmilia:

- `list_cons` constructs a possibly empty list composed of the values of the expressions in its argument, which must be of the same type.
- `first` returns the first element of its argument, which must be a non-empty list.
- `tail` returns what follows the first element of its argument, which must be a list.
- `concat` concatenates its arguments, which must be two lists whose elements are of the same type.
- `insert` inserts the value of its first argument into its second argument, which must be a list whose elements are of the same type as the first argument. The position at which the insertion takes place is established according to the lexicographical order of the elements.
- `remove` removes the value of the element whose position is given by its first argument, which must be an integer not less than one, from its second argument, which must be a list with sufficiently many elements.
- `length` computes the number of elements of its argument, which must be a list.

### 3.4.5 Arrays

The type `array`, which denotes a non-empty, fixed-length sequence of elements of the same type, is defined as follows:

```
"array" "(" <expr> "," <normal_type> ")"
```

where `<expr>` is its length and `<normal_type>` is the type of its elements. The array length expression must be integer valued, free of undeclared identifiers, free of invocations to pseudo-random number generators, and not less than one.

The following three array-related functions are available in Æmilia:

- `array_cons` constructs an array composed of the values of the expressions in its argument, which must be of the same type.
• **read** reads from its second argument, which must be an array with sufficiently many elements, the value of the element indexed by its first argument, which must be an integer between zero and the length of the second argument decremented by one.

• **write** writes to its third argument, which must be an array with sufficiently many elements of the same type as the second argument, the value of its second argument in the position indexed by its first argument, which must be an integer between zero and the length of the third argument decremented by one.

3.4.6 Records

The type **record**, which denotes a non-empty, fixed-length sequence of named elements of possibly different types called fields, is defined as follows:

```
"record" "(" <field_decl_sequence> ")"
```

where `<field_decl_sequence>` is a non-empty sequence of comma-separated field declarations, each of the form defined in Sect. 3.4.1.

The following three record-related functions are available in Æmilia:

```
<expr> ::= "record_cons" "(" <expr_sequence> ")"
| "get" "(" <identifier> "," <expr> ")"
| "put" "(" <identifier> "," <expr> "," <expr> ")"
```

where `<expr_sequence>` is a non-empty sequence of comma-separated expressions and:

• **record_cons** constructs a record composed of the values of the expressions in its argument.

• **get** gets from its second argument, which must be a record, the value of the field whose identifier is given by its first argument, which must belong to the second argument.

• **put** puts into its third argument, which must be a record, the value of its second argument in the field whose identifier is given by its first argument, which must belong to the third argument must and be of the same type as the second argument.

3.4.7 Priorities, Rates, and Weights

The type **prio** denotes the set of immediate and passive action priorities, which coincides with the set of positive integers.

The type **rate** denotes the set of exponentially timed action rates, which coincides with the set of positive reals.

The type **weight** denotes the set of immediate and passive action weights, which coincides with the set of positive reals.

3.5 Architectural Type Header

The architectural type header at the beginning of an Æmilia specification has the following syntax:

```
"ARCHI_TYPE" <identifier> "(" <init_const_formal_par_decl_sequence> ")"
```

where `<identifier>` is the name of the architectural type and `<init_const_formal_par_decl_sequence>` is either **void** or a non-empty sequence of comma-separated declarations of initialized constant formal parameters, each of the following form:

```
"const" <data_type> <identifier> ":=" <expr>
```
A constant formal parameter represents a formal parameter whose value, which stems in this case from the evaluation of the assigned expression, cannot change. The assigned expression must be of the same type as the identifier, free of undeclared identifiers, and free of invocations to pseudo-random number generators. As a consequence, the only identifiers that can occur in the assigned expression are those for the preceding constant formal parameters declared in the architectural type header.

### 3.6 Architectural Element Types

The first section of an Æmilia specification starts with the keyword `ARCHI_ELEM_TYPES` and is composed of a non-empty sequence of AET definitions, each of the following form:

```
<AET_header> <AET_behavior> <AET_interactions>
```

#### 3.6.1 AET Header

Similarly to the architectural type header, the header of an AET has the following syntax:

```
"ELEM_TYPE" <identifier> "(" <const_formal_par_decl_sequence> ")"
```

where `<identifier>` is the name of the AET and `<const_formal_par_decl_sequence>` is either `void` or a non-empty sequence of comma-separated declarations of constant formal parameters, each of the following form:

```
"const" <data_type> <identifier>
```

The value of each such formal constant parameter is defined upon declaration of the instances of the AET in the architectural topology section.

#### 3.6.2 AET Behavior: EMPA\textsubscript{gr} Operators and Actions

The behavior of an AET has the following syntax:

```
"BEHAVIOR" <behav_equation_sequence>
```

where `<behav_equation_sequence>` is a non-empty sequence of semicolon-separated EMPA\textsubscript{gr} behavioral equations, each of the following form:

```
<behav_equation_header> "+" <process_term>
```

The first behavioral equation in the sequence represents the initial behavior for the AET. Each of the other possible behavioral equations in the sequence must describe a behavior that can be directly or indirectly invoked by the initial one.

**Behavioral Equation Header**

The header of the first behavioral equation has the following syntax:

```
<identifier> "(" <init_var_formal_par_decl_sequence> ";" <local_var_decl_sequence> ")"
```

whereas the header of any subsequent behavioral equation has the following syntax:

```
<identifier> "(" <var_formal_par_decl_sequence> ";" <local_var_decl_sequence> ")"
```

In both headers, `<identifier>` is the name of the behavioral equation, while `<local_var_decl_sequence>` is either `void` or a non-empty sequence of comma-separated declarations of local variables, each of the following form:
"local" <normal_type> <identifier>

A local variable is typically used to store one of the values received when synchronizing an input action of an instance of the AET with an output action of another AEI.

In the header of the first behavioral equation, <init_var_formal_par_decl_sequence> is either void or a non-empty sequence of comma-separated declarations of initialized variable formal parameters, each of the following form:

<normal_type> <identifier> ":=" <expr>

In the header of the subsequent behavioral equations, <var_formal_par_decl_sequence> is either void or a non-empty sequence of comma-separated declarations of variable formal parameters, each of the following form:

<normal_type> <identifier>

A variable formal parameter represents a formal parameter whose value can change and, in the case of the first behavioral equation, is initialized by evaluating the assigned expression. The assigned expression must be of the same type as the identifier and free of undeclared identifiers. The only identifiers that can occur in the assigned expression are those for the constant formal parameters declared in the AET header. No initializing expression is needed for the variable formal parameters of each subsequent behavioral equation, as they will be assigned the values of the actual parameters contained in the invocations of the related behavioral equation.

Process Terms

The syntax for the process term following the behavioral equation header is a verbose variant of the syntax for the EMPA<sub>dr</sub> dynamic operators – stop, action prefix, alternative composition, and behavioral equation invocation:

<process_term> ::= "stop"
| <action> "." <process_term_1>
| "choice" "{" <process_term_2_sequence> "}
<process_term_1> ::= <process_term>
| <identifier> "(" <actual_par_sequence> ")"
<process_term_2> ::= ["cond" "(" <expr> ")" ":->"] <process_term>

Constant stop represents the process term that cannot execute any action. The action prefix operator (.) represents a process term that can execute an action given by its first operand and then behaves as the process term given by its second operand. The alternative composition operator (choice) represents a process term that behaves as one of the elements of <process_term_2_sequence>, which is a sequence of at least two comma-separated process terms, each possibly preceded by a boolean expression establishing the condition under which it is available. The behavioral equation invocation represents a process term that behaves as the behavioral equation whose name is given by <identifier>, when passing a possibly empty sequence of expressions represented by <actual_par_sequence>. The actual parameters must match by number, order and type with the variable formal parameters of the invoked behavioral equation. Note that a behavioral equation invocation can occur only immediately after an action prefix operator.

Actions

The syntax for an action occurring in the process term of a behavioral equation is as follows:

<action> ::= "<" <action_type> "," <action_rate> ">"
<action_type> ::= <identifier>
| <identifier> "?" "(" <local_var_sequence> ")"
| <identifier> "!" "(" <expr_sequence> ")"
\begin{verbatim}
<action_rate> ::= "exp" "(" <expr> ")" \\
   | "inf" "(" <expr> "," <expr> ")" \\
   | "inf" \\
   | "=" "(" <expr> "," <expr> ")" \\
   | "="

The action type is simply an identifier (unstructured action), an identifier followed by symbol ? and a non-empty sequence of local variables (input action), or an identifier followed by symbol ! and a non-empty sequence of expressions (output action). Whenever a local variable occurs in an expression within an output action, a behavioral equation invocation, or a boolean guard without previously occurring in an input action, it evaluates to zero, false, empty list, null array, or null record depending on its type.

The rate of an exponentially timed action (\texttt{exp}) is given by an expression, whose value must be a positive real, that is interpreted as the rate of the exponentially distributed random variable describing the action duration. The rate of an immediate action (\texttt{inf}) is expressed through a priority, given by an expression whose value must be an integer not less than one, and a weight, given by an expression whose value must be a positive real. The rate of a passive action (\texttt{\_}) is again expressed through two expressions denoting a priority and a weight, respectively. If not specified, the values of the priority and the weight of an immediate or passive action are assumed to be one.

There are three constraints to which the actions are subject. First, within the behavior of an AET, the actions in which an action type identifier occur must all be unstructured, input with the same number, order, and type of local variables, or output with the same number, order, and type of expressions. Second, within the behavior of an AET, the actions in which an action type identifier occur must all be exponentially timed, immediate with the same priority, or passive with the same priority. Third, every input action must be passive.

If several actions are simultaneously enabled in the current AET behavior, as in the case of the alternative composition, the one to be executed is selected as follows [10]. If all the considered actions are exponentially timed, then the race policy applies: each considered action is selected with a probability proportional to its rate. If some of the considered actions are immediate, then such immediate actions take precedence over the exponentially timed ones and the generative preselection policy applies: each considered immediate action with the highest priority is selected with a probability proportional to its weight. If some of the considered actions are passive, then the reactive preselection policy applies to them: for every action type, each considered passive action of that type with the highest priority level is selected with a probability proportional to its weight (the choice among passive actions of different types is nondeterministic).

An action of an AEI can synchronize with an action of another AEI, possibly exchanging values. Besides other constraints that we shall see in Sect. 3.7.3, in accordance with the generative-reactive paradigm [10] it must be the case that at most one of the two actions is not passive, with both actions being unstructured, or both being structured with at most one of them being an output action and their parameters matching by number, order, and type. If both actions are passive, then the resulting synchronizing action is passive as well, otherwise the rate of the resulting action is the (possibly normalized) rate of the involved non-passive action. The identifier of the resulting action type is internally represented by concatenating the two original identifiers, using symbol \# as a separator. If one of the two involved actions is an output action, then the resulting action is an output action with the same non-empty sequence of expressions as the original output action. If instead both involved actions are input actions, then the resulting action is an input action with the same non-empty sequence of local variables as one of the two original input actions.

3.6.3 AET Interactions

The identifiers of the types of the actions occurring in the behavior of an AET through which the instances of that AET can communicate with other AEIs are declared to be interactions as follows:

"INPUT_INTERACTIONS" <input_interactions> "OUTPUT_INTERACTIONS" <output_interactions>

Every interaction has two qualifiers associated with it. First, an interaction is classified to be either an input or an output interaction based on its communication direction, i.e. whether it tries to establish a
3.7 Architectural Topology

The second section of an Æmilia specification has the following syntax:

"ARCHI_TOPOLOGY" <AEIs> <architectural_interactions> <architectural_attachments>

3.7.1 Architectural Element Instances

The instances of the AETs defined in the first section of an Æmilia specification are declared as follows:

"ARCHI_ELEM_INSTANCES" <AEI_decl_sequence>

where <AEI_decl_sequence> is a non-empty sequence of semicolon-separated AEI declarations, each of the following form:

<AET_decl> ::= <identifier> ["[" <expr> "]"] ":" <identifier> "(" <pe_expr_sequence> ")"
        | "FOR_ALL" <identifier> "IN" <expr> ".." <expr>
        <identifier> ["[" <expr> "]"] ":" <identifier> "(" <pe_expr_sequence> ")"
In its simpler form, an AEI declaration contains the identifier of the AEI, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, the identifier of the related AET, which must have been defined in the first section of the Æmilia specification, and a possibly empty sequence of expressions free of invocations to pseudo-random number generators, which provide the actual values for the constant formal parameters of the AET and must match with them by number, order, and type. The only identifiers that can occur in the possible selector expression and in the actual parameters are the ones of the constant formal parameters declared in the architectural type header.

The second form is useful to concisely declare several instances of the same AET through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression and in the actual parameters, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

We observe that the identifier of an AEI can be augmented with a selector expression also in the simpler form of AEI declaration. This is useful whenever it is desirable to declare a set of indexed instances of the same AET, but only some of them have a common selector expression.

3.7.2 Architectural Interactions
The architectural interactions are declared through the following syntax:

"ARCHI_INTERACTIONS" <pe_architectural_interaction_decl>

where <pe_architectural_interaction_decl> is either void or a non-empty sequence of semicolon-separated architectural interaction declarations, each of the following form:

<architectural_interaction_decl> ::= <identifier> ["" ["expr"] "] "." <identifier> | "FOR_ALL" <identifier> "IN" <expr> "." <expr> <identifier> ["" ["expr"] "] "." <identifier>

In its simpler form, an architectural interaction declaration contains the identifier of the AEI to which the interaction belongs, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the identifier of the interaction. Both the AEI and the interaction for the type of the AEI, whose identifier concatenation through the dot notation gives rise to the name of the architectural interaction, must have been previously declared. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header.

The second form is useful to concisely declare several architectural interactions through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

3.7.3 Architectural Attachments
The architectural attachments are declared through the following syntax:

"ARCHI_ATTACHMENTS" <pe_architectural_attachment_decl>

where <pe_architectural_attachment_decl> is either void or a non-empty sequence of semicolon-separated architectural attachment declarations, each of the following form:

<architectural_attachment_decl> ::= "FROM" <identifier> ["" ["expr"] "] "." <identifier> "TO" <identifier> ["" ["expr"] "] "." <identifier>
In its simpler form, an architectural attachment declaration contains the indication of an output interaction followed by the indication of an input interaction. Each of the two interactions is expressed in dot notation through the identifier of the AEI to which the interaction belongs, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the identifier of the interaction. Both the AEI and the interaction for the type of the AEI must have been previously declared, with the interaction not being architectural. The two AEIs must be different from each other. At least one of the two interactions must be a uni-interaction, and at least one of them must occur in passive actions within the behavior of the AEI to which it belongs. The actions in which the two interactions occur within the behavior of the two AEIs must all be either unstructured or structured; in the latter case, the expressions of the output interaction must match with the local variables of the input interaction by number, order, and type. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header.

The second form is useful to concisely declare several architectural attachments through an indexing mechanism. This additionally requires the specification of up to two different index identifiers, which can then occur in the selector expressions, together with their ranges, each of which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

All the non-architectural interactions should be involved at least in one architectural attachment, with the non-architectural uni-interactions being involved at most in one architectural attachment. All the uni-interactions attached to the same and- or or-interaction must belong to different AEIs. Among all the uni-interactions attached to the same passive and-interaction, at most one is admitted that occurs in non-passive actions within the behavior of the AEI to which it belongs. No isolated groups of AEIs should be present.

### 3.8 Behavioral Variations

The third section of an Æmilia specification has the following syntax:

```
{"BEHAV_VARIATIONS" [<behav_hidings>] [<behav_restrictions>] [<behav_renamings>]}]
```

This section is optional. If present, at least one of its three optional subsections must be there.

#### 3.8.1 Behavioral Hidings

The behavioral hidings are declared through the following syntax:

```
"BEHAV_HIDINGS" <behav_hiding_decl_sequence>
```

where `<behav_hiding_decl_sequence>` is a non-empty sequence of semicolon-separated behavioral hiding declarations, each of the following form:

```
<behav_hiding_decl> ::= "HIDE" "INTERNALS"
| "HIDE" "INTERACTIONS"
| "HIDE" "ALL"
| "HIDE" <identifier> ["[" <expr> "]"] "." <action_type_set_h>
| "FOR_ALL" <identifier> "IN" <expr> ".." <expr>
| "HIDE" <identifier> ["[" <expr> "]"] "." <action_type_set_h>
```

In its simpler form, an architectural attachment declaration contains the indication of an output interaction followed by the indication of an input interaction. Each of the two interactions is expressed in dot notation through the identifier of the AEI to which the interaction belongs, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the identifier of the interaction. Both the AEI and the interaction for the type of the AEI must have been previously declared, with the interaction not being architectural. The two AEIs must be different from each other. At least one of the two interactions must be a uni-interaction, and at least one of them must occur in passive actions within the behavior of the AEI to which it belongs. The actions in which the two interactions occur within the behavior of the two AEIs must all be either unstructured or structured; in the latter case, the expressions of the output interaction must match with the local variables of the input interaction by number, order, and type. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header.

The second form is useful to concisely declare several architectural attachments through an indexing mechanism. This additionally requires the specification of up to two different index identifiers, which can then occur in the selector expressions, together with their ranges, each of which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

All the non-architectural interactions should be involved at least in one architectural attachment, with the non-architectural uni-interactions being involved at most in one architectural attachment. All the uni-interactions attached to the same and- or or-interaction must belong to different AEIs. Among all the uni-interactions attached to the same passive and-interaction, at most one is admitted that occurs in non-passive actions within the behavior of the AEI to which it belongs. No isolated groups of AEIs should be present.
In its simpler form, a behavioral hiding declaration consists of making unobservable all the action types that are internal to the AEIs of the Æmilia specification, all the non-architectural interactions of the AEIs of the Æmilia specification, or both of them. Alternatively, it is possible to hide a set of action types of a specific AEI. In this case, the behavioral hiding declaration contains the identifier of the AEI to which the action types to be hidden belong, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the identifier of the action type to be hidden or one of the three shorthands above for sets of action types to be hidden. If specified, the AEI must have been previously declared. If specified, the action type to be hidden must occur in the behavior of the AEI and cannot be an architectural interaction. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header.

The more complex form is useful to concisely hide some of the action types of several AEIs through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

If an internal action type is hidden, it is converted to the special action type `invisible`. If a non-architectural interaction is hidden, all the synchronizing action types in which it is involved are converted to the special action type `invisible`. In both cases, all the possible action type parameters are dropped.

3.8.2 Behavioral Restrictions

The behavioral restrictions are declared through the following syntax:

```
"BEHAV_RESTRICTIONS" <behav_restriction_decl_sequence>
```

where `<behav_restriction_decl_sequence>` is a non-empty sequence of semicolon-separated behavioral restriction declarations, each of the following form:

```
<behav_restriction_decl> ::= "RESTRICT" "OBS_INTERNALS"
| "RESTRICT" "OBS_INTERACTIONS"
| "RESTRICT" "ALL_OBSERVABLES"
| "RESTRICT" <identifier> ["[" <expr> "]"] "." <action_type_set_r>
| "FOR_ALL" <identifier> "IN" <expr> ".." <expr>
| "RESTRICT" <identifier> ["[" <expr> "]"] "." <action_type_set_r>
```

```
<action_type_set_r> ::= <identifier>
| "OBS_INTERNALS"
| "OBS_INTERACTIONS"
| "ALL_OBSERVABLES"
```

In its simpler form, a behavioral restriction declaration consists of preventing the execution of all the observable action types that are internal to the AEIs of the Æmilia specification, all the observable, non-architectural interactions of the AEIs of the Æmilia specification, or both of them. Alternatively, it is possible to restrict a set of action types of a specific AEI. In this case, the behavioral restriction declaration contains the identifier of the AEI to which the action types to be restricted belong, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the identifier of the action type to be restricted or one of the three shorthands above for sets of action types to be restricted. If specified, the AEI must have been previously declared. If specified, the action type to be hidden must occur in the behavior of the AEI.
and cannot be an architectural interaction or hidden. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header.

The more complex form is useful to concisely restrict some of the action types of several AEIs through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

If an observable internal action type is restricted, it cannot be executed. If an observable, non-architectural interaction is restricted, none of the synchronizing action types in which it is involved can be executed.

### 3.8.3 Behavioral Renamings

The behavioral renamings are declared through the following syntax:

```
"BEHAV_RENAMINGS" <behav_renaming_decl_sequence>
```

where `<behav_renaming_decl_sequence>` is a non-empty sequence of semicolon-separated behavioral renaming declarations, each of the following form:

```
<behav_renaming_decl> ::= "RENAME" <identifier> ["[" <expr> "]"] "." <identifier> "AS" <identifier> ["[" <expr> "]"]
| "FOR_ALL" <identifier> "IN" <expr> ".." <expr> "RENAME" <identifier> ["[" <expr> "]"] "." <identifier> "AS" <identifier> ["[" <expr> "]"]
```

In its simpler form, a behavioral renaming declaration contains the identifier of the AEI to which the action type to be renamed belongs, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the identifier of the renaming action type possibly followed by another selector expression. The AEI must have been previously declared. The action type to be renamed must occur in the behavior of the AEI and cannot be hidden or restricted. The only identifiers that can occur in the possible selector expressions are the ones of the constant formal parameters declared in the architectural type header.

The more complex form is useful to concisely rename some of the action types of several AEIs through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expressions, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

An observable, non-restricted action type can be renamed to a single action type. If an observable, non-restricted, internal action type or an architectural interaction is renamed, it is converted to the specified renaming action type. If an observable, non-restricted, non-architectural interaction is renamed, all the synchronizing action types in which it is involved are converted to the specified renaming action type. Note that the renaming action type is not expressed in dot notation, which may turn out to be useful when checking for equivalence two .Elmilia specifications whose AEIs have different identifiers. In the model checking case, instead, any renaming action type must be different from the NuSMV 2.2.5 keywords, which are listed below:

```
A ABF AEG ATLTLSPEC Z
ABG EVAL EX LTLWFF apropos
AF AG EXE MAX array
ASSIGN AG FAIRNESS MODULE case
ASYNC AG FAIRNESS OUTPUT esac
AX BU GOTO G G DEP Reset if
CTRLWFF BU GOTO H SIMPWFF init
```
3.9 Compiling Æmilia Specifications

In this section we briefly describe how correct Æmilia specifications are compiled into finite semantic models suited for analysis.

3.9.1 Parsing

While parsing an Æmilia (or companion) specification, a .lis file is generated in which each line of the specification is reported by having it preceded by its line number. The parser is able to catch about 300 types of lexical, syntax and static semantic error or warning, which are signalled through suitable messages in the .lis file. The .lis file is terminated with the indication of the total number of errors and warnings that have been detected. A specification with no errors is said to be correct.

3.9.2 Semantic Models

A correct Æmilia specification can be compiled into three semantic models: the integrated semantic model, the functional semantic model, and the performance semantic model. All of them are state transition graphs, whose states are in correspondence with the vectors of the current behaviors of the AEIs. More precisely, the integrated semantic model is a state transition graph whose transitions are labeled with the type and the rate of the corresponding actions, with the lower priority transitions being pruned. The functional semantic model is a state transition graph in which only the action types label the transitions. The performance semantic model can be extracted in the form of a Markov chain [32] only if the Æmilia specification is performance closed, i.e. its integrated semantic model has no passive transitions and no non-determinism arises because of some boolean condition – occurring in a behavioral choice – that cannot be statically evaluated. In such a case, if the integrated semantic model has only exponentially timed transitions or both immediate and exponentially timed transitions, the performance semantic model is a continuous-time Markov chain obtained after removing the possible immediate transitions, with the transitions labeled with the rates of the corresponding actions. If instead the integrated semantic model has only immediate transitions, they are interpreted as taking one time unit and the performance semantic model is a discrete-time Markov chain, with the transitions labeled with the probabilities of the corresponding actions.

Due to the process term syntax within the behavior of the AEIs, which rules out static operators (hence recursion over them) as well as behavioral equation invocations outside the scope of an action prefix, the semantic model of an Æmilia specification with no variable formal parameters and local variables is guaranteed to be finitely branching and finite state.

When printed to the related .ism, .fsm or .psm file, the semantic model is a sequence of numbered global states with their outgoing transitions. Each global state is described through the vector of local states representing the current behavior of the AEIs. In the case of the integrated and functional semantic models, the global state numbered with one is the initial global state, which is composed of the local states representing the initial behavior of the AEIs. In the case of the performance semantic model, the concept of initial global state is replaced with an initial global state probability distribution – as the initial global state may not be unique – whose values are reported in the .psm file for every global state. Each transition is represented through its action-based label and the number of its target global state.
The .ism, .fsm or .psm file is terminated with the indication of the total number of global states and transitions and their classification. The global states are divided into tangible (having exponentially timed transitions), vanishing (having immediate transitions), open (having passive transitions), and deadlocked (having no transitions). In the case of the performance semantic model, the global states with no outgoing transitions are called absorbing rather than deadlocked as they might have self-looping transitions. Based on their action types, the transitions are divided into observable and invisible. Based on their action rates, the transitions are divided into exponentially timed, immediate, and passive.

The same global state and transition classification is reported, together with the related numbers, in a .siz file whenever the user is interested only in the size of the semantic model.

### 3.9.3 Concrete and Symbolic Representation of Data Values

In the case in which variable formal parameters and local variables are present in the behavioral equations of the AETs of an Æmilia specification, they must be compiled in a way that keeps the underlying semantic models both finitely branching and finite state. This can be achieved in two different ways.

If each of the occurring variable formal parameters and local variables has a finite value domain, i.e. its type is bounded integer, boolean, or array or record based on the two previous basic types, then a concrete treatment is applied. This means that every expression — occurring in a behavioral equation invocation, a boolean guard, or an output action — can be statically evaluated, after replacing every input action with a choice among as many instances of it as needed to instantiate all of its local variables in every possible way according to their finite value domains. In this case, the synchronization between an output action and an input action is possible only if their parameters have pairwise the same value. In the .ism, .fsm or .psm file, the current value of every variable formal parameter and local variable is represented through a concrete assignment — an assignment whose right-hand side does not contain any variable — printed immediately after the current behavior of the AEI to which the variable formal parameter or local variable belongs.

If instead there is at least one variable formal parameter or local variable with an infinite value domain, i.e. whose type is integer, real, list, or array or record based on the three previous types, then a concrete treatment is not possible. To keep the semantic models finite, a symbolic treatment is applied [5]. Every transition label is augmented with an expression and a sequence of symbolic assignments. The expression, which arises from the possible boolean guards of the alternative composition operator, represents the condition under which the transition can be executed. The symbolic assignments establish how the values of the variable formal parameters and of the local variables must be updated after executing the transition, due to behavioral equation invocations in the target global state or value passing between the synchronized structured actions involved in the transition. In the .ism, .fsm or .psm file, every transition is printed together with its boolean guard and its sequence of symbolic assignments. Moreover, a list of initial symbolic assignments, based on the initialization of the variable formal parameters in the header of the first behavioral equation of every AEI, is printed at the beginning of the file. We remind that the performance semantic model cannot be generated in the case of symbolic treatment if there is at least one boolean guard that cannot be statically evaluated.

We conclude by recalling that equivalence verification, model checking, security analysis, and Markov-chain-based performance evaluation can be applied only to correct Æmilia specifications in which all the possible variable formal parameters and local variables can be treated concretely. Simulation, instead, can be applied to any correct Æmilia specification (with no open and deadlock states), because the possible expressions — including guards and symbolic assignments — are directly evaluated while generating the portion of the integrated semantic model that is necessary to make the simulation advance.

### 3.9.4 Compile-Time Crashes

The compilation of an Æmilia specification can be interrupted because of lack of memory, inability to open a file, illegal value of a symbolic action rate, or an error occurred during the evaluation of a concrete assignment, like out-of-range bounded integer, symbolic array length mismatch, or invalid argument of an arithmetical operator, a mathematical function, a pseudo-random number generator, or a list- or array-related function. In each of these cases, which cannot be detected at parsing time, a suitable message is displayed.
3.10 Example A: The Alternating Bit Protocol

In this section we introduce a simple communication protocol and we present three different Æmilia specifications for it, which exemplify the syntax of the language and illustrate its expressiveness.

3.10.1 Informal Description

The alternating bit protocol [3] is a data-link-level communication protocol that establishes a means whereby two stations, one acting as a sender and the other acting as a receiver, connected by a full-duplex, FIFO communication channel that may lose messages, can cope with message loss. The name of the protocol stems from the fact that each message is augmented with an additional bit. Since consecutive messages that are not lost are tagged with additional bits that are pairwise complementary, it is easy to distinguish between an original message and its possible duplicates.

Initially, if the data link level of the sender obtains a message from the upper level in the protocol stack, it augments the message with an additional bit set to 0, sends the tagged message to the receiver, and starts a timer. If an acknowledgment tagged with 0 is received before the timeout expires, then the subsequent message obtained from the upper level will be sent with an additional bit set to 1, otherwise the current tagged message is sent again. On the other side, the data link level of the receiver waits for a message tagged with 0. If it receives such a tagged message for the first time, then it passes the message to the upper level in the protocol stack, sends an acknowledgment tagged with 0 back to the sender, and waits for a message tagged with 1. On the contrary, if it receives a duplicate tagged message – due to message loss, acknowledgment loss, or propagation taking an exceedingly long time – then it sends an acknowledgment tagged with the same additional bit back to the sender and keeps waiting.

3.10.2 Pure Æmilia Description with Markovian Delays

We show below a pure Æmilia specification of the alternating bit protocol called \( \text{abp.aem} \), where pure means that no variable formal parameters and local variables are used:

\[
\text{ARCHI_TYPE ABP_Type}(\text{const rate } \text{msg_gen_rate} := 5, \\
\text{const rate } \text{timeout_rate} := 1, \\
\text{const rate } \text{prop_rate} := 9.375, \\
\text{const weight } \text{delivery_prob} := 0.95)
\]

\[
\text{ARCHI_ELEM_TYPES}
\]

\[
\text{ELEM_TYPE Sender_Type}(\text{const rate } \text{msg_gen_rate}, \\
\text{const rate } \text{timeout_rate})
\]

\[
\text{BEHAVIOR}
\]

\[
\text{Sender_0}(\text{void}; \text{void}) = \\
\langle \text{generate_msg, exp(msg_gen_rate)} \rangle \cdot \langle \text{transmit_msg_0, inf} \rangle \cdot \text{Sender_0_Waiting}();
\]

\[
\text{Sender_0_Waiting}(\text{void}; \text{void}) = \\
\text{choice} \\
\{ \\
\langle \text{receive_ack_0, _} \rangle \cdot \text{Sender_1}(), \\
\langle \text{receive_ack_1, _} \rangle \cdot \text{Sender_0_Waiting}(), \\
\langle \text{timeout, exp(timeout_rate)} \rangle \cdot \text{Sender_0_Retransmitting}()
\};
\]

\[
\text{Sender_0_Retransmitting}(\text{void}; \text{void}) = \\
\text{choice}
\]
\[
\begin{verbatim}
{ 
<transmit_msg_0, inf> . Sender_0_Waiting(),
<receive_ack_0, _> . Sender_1(),
<receive_ack_1, _> . Sender_0_Retransmitting()
};

Sender_1(void; void) =
<generate_msg, exp(msg_gen_rate)> . <transmit_msg_1, inf> . Sender_1_Waiting();

Sender_1_Waiting(void; void) =
choice
{ 
<receive_ack_1, _> . Sender_0(),
<receive_ack_0, _> . Sender_1_Waiting(),
<timeout, exp(timeout_rate)> . Sender_1_Retransmitting()
};

Sender_1_Retransmitting(void; void) =
choice
{ 
<transmit_msg_1, inf> . Sender_1_Waiting(),
<receive_ack_1, _> . Sender_0(),
<receive_ack_0, _> . Sender_1_Retransmitting()
}
\end{verbatim}
\]

\textbf{INPUT\_INTERACTIONS}

UNI generate_msg;
receive_ack_0;
receive_ack_1

\textbf{OUTPUT\_INTERACTIONS}

UNI transmit_msg_0;
transmit_msg_1

\textbf{ELEM\_TYPE Line\_Type(const rate prop_rate, const weight delivery_prob)}

\textbf{BEHAVIOR}

Line(void; void) =
choice
{ 
<receive_0, _> . <propagate_0, exp(prop_rate)> . 
choice
{ 
<keep_0, inf(1, delivery_prob)> . <deliver_0, inf> . Line(),
<lose_0, inf(1, 1 - delivery_prob)> . Line()
},
<receive_1, _> . <propagate_1, exp(prop_rate)> . 
choice
{ 

<keep_1, inf(1, delivery_prob)> . <deliver_1, inf> . Line(), <lose_1, inf(1, 1 - delivery_prob)> . Line() 
}

INPUT_INTERACTIONS
UNI receive_0;
  receive_1

OUTPUT_INTERACTIONS
UNI deliver_0;
  deliver_1

ELEM_TYPE Receiver_Type(void)

BEHAVIOR
Receiver_0(void; void) =
  choice
  {
    <receive_msg_0, _> . <consume_msg, inf> . <transmit_ack_0, inf> . Receiver_1(), <receive_msg_1, _> . <transmit_ack_1, inf> . Receiver_0()
  };
Receiver_1(void; void) =
  choice
  {
    <receive_msg_1, _> . <consume_msg, inf> . <transmit_ack_1, inf> . Receiver_0(), <receive_msg_0, _> . <transmit_ack_0, inf> . Receiver_1()
  }

INPUT_INTERACTIONS
UNI receive_msg_0;
  receive_msg_1

OUTPUT_INTERACTIONS
UNI consume_msg;
  transmit_ack_0;
  transmit_ack_1

ARCHI_TOPOLOGY

ARCHI_ELEM_INSTANCES
S : Sender_Type(msg_gen_rate, timeout_rate);
LM : Line_Type(prop_rate, delivery_prob);
LA : Line_Type(prop_rate,
3.10 Example A: The Alternating Bit Protocol

```plaintext
delivery_prob);
R : Receiver_Type()

ARCHI_INTERACTIONS

S.generate_msg;
R.consume_msg

ARCHI_ATTACHMENTS

FROM S.transmit_msg_0 TO LM.receive_0;
FROM S.transmit_msg_1 TO LM.receive_1;
FROM LM.deliver_0 TO R.receive_msg_0;
FROM LM.deliver_1 TO R.receive_msg_1;
FROM R.transmit_ack_0 TO LA.receive_0;
FROM R.transmit_ack_1 TO LA.receive_1;
FROM LA.deliver_0 TO S.receive_ack_0;
FROM LA.deliver_1 TO S.receive_ack_1

END

The Æmilia specification above is parameterized with respect to the message generation rate, the timeout rate, the propagation rate of a single message, and the delivery probability of a single message. In order to allow for a Markov-chain-based performance evaluation, the timeout delay and the message propagation delay are assumed to be exponentially distributed. Supposed that the protocol uses two 9.6 Kbps lines and that the average length of a message is 1024 bits, the propagation rate is 9.375 messages per second. We also assume that the generation rate is 5 messages per second, the timeout delay is 1 second on average, and the delivery probability is 0.95.

We have three AETs: one for the sender, one for a half-duplex communication line, and one for the receiver. As far as Sender_Type is concerned, initially a message is generated (i.e. arrives from the upper level), which is then tagged with 0 and transmitted. Three cases arise. If an acknowledgment tagged with 0 is received, then the same behavior is repeated for the next generated message, which will be tagged with 1. If an acknowledgment tagged with 1 is received, the acknowledgment is simply ignored. If the timeout expires, then the message is retransmitted unless an acknowledgment tagged with 0 is received in the meanwhile.

Line_Type waits for the transmission of a message/acknowledgment tagged with 0 or 1, which is then propagated along the line. With probability 0.95 the message/acknowledgment reaches its destination, while with probability 0.05 the message/acknowledgment is lost. Afterwards, this behavior is repeated. Note that the types of the actions representing the fact that a message/acknowledgment is kept or lost are not declared to be interactions, as these events are not under the control of the protocol.

Receiver_Type initially waits for a message tagged with 0. If it is received, then the message tagged with 0 is passed to the upper level, an acknowledgment tagged with 0 is sent back, and this behavior is repeated for the next expected message, which shall be tagged with 1. As long as a message tagged with 1 is received instead, the message is ignored and an acknowledgment tagged with 1 is sent back.

The architectural topology section contains the declaration of one instance of Sender_Type, two instances of Line_Type – one for the messages and one for the acknowledgments – and one instance of Receiver_Type. The interactions S.generate_msg and R.consume_msg are declared to be architectural, as they are the access points for the upper levels of the protocol stack both at the sender side and at the receiver side.

Here is the size of the semantic models of abp.aem:

Size of the integrated semantic model underlying ABP_Type:

- 302 states:
  - 76 tangible,
  - 226 vanishing,
```
- 0 open,
- 0 deadlocked;

- 464 transitions:
  - 464 observable,
  - 0 invisible;
  - 140 exponentially timed,
  - 324 immediate,
  - 0 passive.

Size of the functional semantic model underlying ABP_Type:

- 302 states:
  - 302 nondeadlocked,
  - 0 deadlocked;

- 464 transitions:
  - 464 observable,
  - 0 invisible.

Size of the homogeneous continuous-time Markov chain underlying ABP_Type:

- 76 states:
  - 76 nonabsorbing,
  - 0 absorbing;

- 204 transitions.

### 3.10.3 Value Passing Æmilia Description with Markovian Delays

A more concise Æmilia description can be obtained if the tagging bit is encoded through a boolean variable that is passed across the components, as shown in the following `abp_vp.aem`:

```plaintext
ARCHI_TYPE ABP_VP_Type(const boolean starting_bit := false,
                        const rate msg_gen_rate := 5,
                        const rate timeout_rate := 1,
                        const rate prop_rate := 9.375,
                        const weight delivery_prob := 0.95)

ARCHI_ELEM_TYPES

ELEM_TYPE Sender_Type(const boolean starting_bit,
                      const rate msg_gen_rate,
                      const rate timeout_rate)

BEHAVIOR

Sender(boolean sent_bit := starting_bit;
        void) =
  <generate_msg, exp(msg_gen_rate)> . <transmit_msg!(sent_bit), inf> .
  Sender_Waiting(sent_bit);

Sender_Waiting(boolean sent_bit;
                local boolean received_bit) =
```

```plaintext
```
choice
{
  <receive_ack?(received_bit), _> . Sender_Checking(sent_bit, 
    received_bit),
  <timeout, exp(timeout_rate)> . Sender_Retransmitting(sent_bit)
};

Sender_Checking(boolean sent_bit, 
  boolean received_bit; 
  void) =
choice
{
  cond(received_bit = sent_bit) ->
    <check_bit, inf> . Sender(!sent_bit),
  cond(received_bit != sent_bit) ->
    <check_bit, inf> . Sender_Waiting(sent_bit)
};

Sender_Retransmitting(boolean sent_bit; 
  local boolean received_bit) =
choice
{
  <transmit_msg!(sent_bit), inf> . Sender_Waiting(sent_bit),
  <receive_ack?(received_bit), _> . Sender_Checking(sent_bit, 
    received_bit)
}

INPUT_INTERACTIONS
UNI generate_msg;
receive_ack

OUTPUT_INTERACTIONS
UNI transmit_msg

ELEM_TYPE Line_Type(const rate prop_rate, 
  const weight delivery_prob)

BEHAVIOR

Line(void; 
  local boolean tagging_bit) = 
  <receive?(tagging_bit), _> . <propagate, exp(prop_rate)> . 
  choice
  {
    <keep, inf(1, delivery_prob)> . <deliver!(tagging_bit), inf> . Line(),
    <lose, inf(1, 1 - delivery_prob)> . Line()
  }

INPUT_INTERACTIONS
UNI receive
OUTPUT_INTERACTIONS

UNI deliver

ELEM_TYPE Receiver_Type(const boolean starting_bit)

BEHAVIOR

Receiver(boolean expected_bit := starting_bit;
    local boolean received_bit) =
    <receive_msg?(received_bit), _> .
    choice
    {
    cond(received_bit = expected_bit) ->
        <consume_msg, inf> . <transmit_ack!(received_bit), inf> .
        Receiver(!expected_bit),
    cond(received_bit != expected_bit) ->
        <transmit_ack!(received_bit), inf> . Receiver(expected_bit)
    }

INPUT_INTERACTIONS

UNI receive_msg

OUTPUT_INTERACTIONS

UNI consume_msg;
    transmit_ack

ARCHI_TOPOLOGY

ARCHI_ELEM_INSTANCES

S : Sender_Type(starting_bit,
    msg_gen_rate,
    timeout_rate);
LM : Line_Type(prop_rate,
    delivery_prob);
LA : Line_Type(prop_rate,
    delivery_prob);
R : Receiver_Type(starting_bit)

ARCHI_INTERACTIONS

S.generate_msg;
R.consume_msg

ARCHI_ATTACHMENTS

FROM S.transmit_msg TO LM.receive;
FROM LM.deliver TO R.receive_msg;
FROM R.transmit_ack TO LA.receive;
FROM LA.deliver TO S.receive_ack

END

Since all the occurring variable formal parameters and local variables are of type boolean, the concrete treatment of data values applies. Here is the size of the semantic models of \texttt{abp_vp.aem}:

Size of the integrated semantic model underlying \texttt{ABP_VP_Type}:

- 366 states:
  - 76 tangible,
  - 290 vanishing,
  - 0 open,
  - 0 deadlocked;
- 556 transitions:
  - 556 observable,
  - 0 invisible;
  - 140 exponentially timed,
  - 416 immediate,
  - 0 passive.

Size of the functional semantic model underlying \texttt{ABP_VP_Type}:

- 366 states:
  - 366 nondeadlocked,
  - 0 deadlocked;
- 556 transitions:
  - 556 observable,
  - 0 invisible.

Size of the homogeneous continuous-time Markov chain underlying \texttt{ABP_VP_Type}:

- 76 states:
  - 76 nonabsorbing,
  - 0 absorbing;
- 214 transitions.

3.10.4 Value Passing Æmilia Description with General Delays

The value passing features are not only necessary to express data-driven computations and useful to obtain more concise Æmilia specifications. They also allow for the representation of systems in which some activities have generally distributed durations. As an example, in the case of the alternating bit protocol, it is reasonable to assume that the message generation time is exponentially distributed, while it is more realistic to describe the message propagation time through e.g. a normal distribution and the timeout period through a fixed duration.

This is accomplished using a sub-language of Æmilia in which there are no exponentially timed actions. In other words, a system with generally distributed delays is represented through a discrete-time model, in which an explicit clock process marks the discrete-time steps for the whole system. The timed events are treated by means of suitable list-typed variables that store the occurrence times of such events, where the related occurrence times are expressed through suitable invocations to pseudo-random number generators. Timer variables are then used in the specification of the various system components to detect when the occurrence
time of a timed event has come, in order to enable the particular action representing the occurrence of the event itself.

The guidelines above are followed in `abp_gd.aem` shown below, in which the delays are expressed in milliseconds, the propagation time is described through a normal distribution, and the timeout period is described through a fixed duration:

```plaintext
ARCHI_TYPE ABP_GD_Type(const boolean starting_bit := false,
  const real msg_gen_rate := 0.005,
  const integer timeout_period := 1000,
  const real prop_delay_mean := 107.0,
  const real prop_delay_st_dev := 7.0,
  const weight delivery_prob := 0.95)

ARCHI_ELEM_TYPES

ELEM_TYPE Msg_Gen_Type(const real msg_gen_rate)

BEHAVIOR

Msg_Gen(integer time_to_gen_next := ceil(exponential(msg_gen_rate)),
  integer msg_to_send := 0;
  void) =
choice
{cond(msg_to_send >= 1) ->
choice
{
  <generate_msg, inf(3, 1)> . Msg_Gen_Updating(time_to_gen_next,
    msg_to_send - 1),
  <idle, inf> . Msg_Gen_Updating(time_to_gen_next,
    msg_to_send)
},
  cond(msg_to_send = 0) ->
  <idle, inf> . Msg_Gen_Updating(time_to_gen_next,
    msg_to_send)
};

Msg_Gen_Updating(integer time_to_gen_next,
  integer msg_to_send; void) =
choice
{cond(time_to_gen_next = 0) ->
  <elapse_tick, _> . Msg_Gen(ceil(exponential(msg_gen_rate)),
    msg_to_send + 1),
  cond(time_to_gen_next > 0) ->
  <elapse_tick, _> . Msg_Gen(time_to_gen_next - 1,
    msg_to_send)
}

INPUT_INTERACTIONS

UNI elapse_tick
```
OUTPUT_INTERACTIONS

UNI generate_msg

ELEM_TYPE Sender_Type(const boolean starting_bit,
                        const integer timeout_period)

BEHAVIOR

Sender(boolean sent_bit := starting_bit;
        local boolean received_bit) =
    choice
    {
        <get_msg, _> . Sender_Transmitting(sent_bit),
        <receive_ack?(received_bit), _> . <elapse_tick, _> . Sender(sent_bit),
        <elapse_tick, _> . Sender(sent_bit)
    };

Sender_Transmitting(boolean sent_bit;
                      local boolean received_bit) =
    choice
    {
        <transmit_msg!(sent_bit), inf(2, 1)> . <elapse_tick, _> .
        Sender_Waiting(sent_bit,
                        timeout_period),
        <receive_ack?(received_bit), _> . <elapse_tick, _> .
        Sender_Transmitting(sent_bit),
        <elapse_tick, _> . Sender_Transmitting(sent_bit)
    };

Sender_Waiting(boolean sent_bit,
                integer time_to_timeout;
                local boolean received_bit) =
    choice
    {
        cond(time_to_timeout > 0) ->
            choice
            {
                <receive_ack?(received_bit), _> . Sender_Checking_1(sent_bit,
                                    time_to_timeout, received_bit),
                <elapse_tick, _> . Sender_Waiting(sent_bit,
                                    time_to_timeout - 1)
            },
        cond(time_to_timeout = 0) ->
            choice
            {
                <timeout, inf(2, 1)> . Sender_Retransmitting(sent_bit),
                <receive_ack?(received_bit), _> . Sender_Checking_2(sent_bit,
                                    received_bit)
            }
Sender_Checking_1(boolean sent_bit, integer time_to_timeout, boolean received_bit; void) =
choice
{ cond(received_bit = sent_bit) ->
  <elapse_tick, _> . Sender(!sent_bit),
cond(received_bit != sent_bit) ->
  <elapse_tick, _> . Sender_Waiting(sent_bit,
    time_to_timeout - 1)
};

Sender_Checking_2(boolean sent_bit, boolean received_bit; void) =
choice
{ cond(received_bit = sent_bit) ->
  <elapse_tick, _> . Sender(!sent_bit),
cond(received_bit != sent_bit) ->
  <idle, inf> . Sender_Retransmitting(sent_bit)
};

Sender_Retransmitting(boolean sent_bit; local boolean received_bit) =
choice
{ <transmit_msg!(sent_bit), inf(2, 1)> . <elapse_tick, _> .
  Sender_Waiting(sent_bit,
    timeout_period),
  <receive_ack?(received_bit), _> . Sender_Checking_2(sent_bit,
    received_bit),
  <elapse_tick, _> . Sender_Retransmitting(sent_bit)
}

INPUT_INTERACTIONS

UNI get_msg;
receive_ack;
elapse_tick

OUTPUT_INTERACTIONS

UNI transmit_msg

ELEM_TYPE Line_Type(const real prop_delay_mean,
  const real prop_delay_st_dev,
  const weight delivery_prob)
3.10 Example A: The Alternating Bit Protocol

```plaintext
Line(list(record(integer time_to_delivery,
    boolean tag)) prop_queue := list_cons();
    local boolean tagging_bit =
choice
{<receive?(tagging_bit), _> .
    choice
    {<keep, inf(2, delivery_prob)> . Line_Delivering(concat(prop_queue,
        list_cons(record_cons(ceil(normal(prop_delay_mean,
            prop_delay_st_dev)),
            tagging_bit)))),
        <lose, inf(2, 1 - delivery_prob)> . Line_Delivering(prop_queue)
    },<idle, inf> . Line_Delivering(prop_queue)
};

Line_Delivering(list(record(integer time_to_delivery,
    boolean tag)) prop_queue;
    void) =
choice
{cond((prop_queue != list_cons()) &&
    get(time_to_delivery,
        first(prop_queue)) <= 0) ->
    <deliver!(get(tag,
        first(prop_queue))), inf(3, 1)> . Line_Propagating(tail(prop_queue)),
cond((prop_queue = list_cons()) ||
    get(time_to_delivery,
        first(prop_queue)) > 0) ->
    <idle, inf> . Line_Propagating(prop_queue)
};

Line_Propagating(list(record(integer time_to_delivery,
    boolean tag)) prop_queue;
    void) =
choice
{cond(prop_queue != list_cons()) ->
    <propagate, inf(2, 1)> . Line_Updating(prop_queue,
        list_cons()),
cond(prop_queue = list_cons()) ->
    <elapse_tick, _> . Line(prop_queue)
};

Line_Updating(list(record(integer time_to_delivery,
    boolean tag)) prop_queue,
    list(record(integer time_to_delivery,
        boolean tag)) new_prop_queue;
    void) =
```
choice
{
  cond(prop_queue != list_cons()) ->
  <compute_time_to_delivery, inf(2, 1)> .
  Line_Updating(tail(prop_queue),
  concat(new_prop_queue,
  list_cons(record_cons(get(time_to_delivery,
    first(prop_queue)) - 1,
    get(tag,
    first(prop_queue))))),

  cond(prop_queue = list_cons()) ->
  <elapse_tick, _> . Line(new_prop_queue)
}

INPUT_INTERACTIONS
UNI receive;
  elapse_tick

OUTPUT_INTERACTIONS
UNI deliver

ELEM_TYPE Receiver_Type(const boolean starting_bit)

BEHAVIOR

Receiver(boolean expected_bit := starting_bit;
  local boolean received_bit) =
choice
{
  <receive_msg?(received_bit), _> . Receiver_Checking(expected_bit,
    received_bit),
  <elapse_tick, _> . Receiver(expected_bit)
};

Receiver_Checking(boolean expected_bit,
  boolean received_bit; void) =
choice
{
  cond(received_bit = expected_bit) ->
  <consume_msg, inf(2, 1)> . Receiver_Transmitting(!expected_bit,
    received_bit),
  cond(received_bit != expected_bit) ->
  <idle, inf> . Receiver_Transmitting(expected_bit,
    received_bit)
};

Receiver_Transmitting(boolean expected_bit,
  boolean received_bit; void) =
choice
{  
  <transmit_ack!(received_bit), inf(2, 1)> . <elapse_tick, _> .  
  Receiver(expected_bit),  
  <elapse_tick, _> . Receiver_Transmitting(expected_bit,  
  received_bit)  
}

INPUT_INTERACTIONS

UNI receive_msg;  
  elapse_tick

OUTPUT_INTERACTIONS

UNI consume_msg;  
  transmit_ack

ELEM_TYPE Clock_Type(void)

BEHAVIOR

Clock(void; void) =  
  <elapse_tick, inf> . Clock()

INPUT_INTERACTIONS

void

OUTPUT_INTERACTIONS

AND elapse_tick

ARCHI_TOPOLOGY

ARCHI_ELEM_INSTANCES

MG : Msg_Gen_Type(msg_gen_rate);  
S : Sender_Type(starting_bit,  
  timeout_period);  
LM : Line_Type(prop_delay_mean,  
  prop_delay_st_dev,  
  delivery_prob);  
LA : Line_Type(prop_delay_mean,  
  prop_delay_st_dev,  
  delivery_prob);  
R : Receiver_Type(starting_bit);  
C : Clock_Type()

ARCHI_INTERACTIONS

R.consume_msg

ARCHI_ATTACHMENT
FROM MG.generate_msg TO S.get_msg;
FROM S.transmit_msg TO LM.receive;
FROM LM.deliver TO R.receive_msg;
FROM R.transmit_ack TO LA.receive;
FROM LA.deliver TO S.receive_ack;
FROM C.elapse_tick TO MG.elapse_tick;
FROM C.elapse_tick TO S.elapse_tick;
FROM C.elapse_tick TO LM.elapse_tick;
FROM C.elapse_tick TO LA.elapse_tick;
FROM C.elapse_tick TO R.elapse_tick
END

Note that C.elapse_tick is an and-interaction, as it must simultaneously synchronize with the elapse_tick interactions of all the other AEIs in order to mark the discrete time steps for the whole system. Observe also that such an and-interaction is given the lowest priority, so that all the system activities logically belonging to the same time step can be completed before the clock ticks.

Because of the presence of integer-, integer-based-, and list-typed variable formal parameters and local variables, only the symbolic treatment of data values applies. Moreover, the symbolic performance semantic model of abp_gd.aem cannot be generated as the specification is not performance closed, due to non-determinism arising from the boolean guards within the alternative compositions that cannot be statically evaluated. Here is the size of the other two semantic models of abp_gd.aem:

Size of the integrated semantic model underlying ABP_GD_Type:
- 701 states:
  - 0 tangible,
  - 701 vanishing,
  - 0 open,
  - 0 deadlocked;
- 2781 transitions:
  - 2781 observable,
  - 0 invisible;
  - 0 exponentially timed,
  - 2781 immediate,
  - 0 passive.

Size of the functional semantic model underlying ABP_GD_Type:
- 701 states:
  - 701 nondeadlocked,
  - 0 deadlocked;
- 2781 transitions:
  - 2781 observable,
  - 0 invisible.

3.11 Example B: The NRL Pump

In this section we illustrate an extension of the alternating bit protocol used in a trusted device to guarantee a suitable replication of information from low security users to high security users.
3.11 Example B: The NRL Pump

3.11.1 Informal Description

The NRL Pump [25] is a hardware device that interfaces a high security level LAN with a low security level LAN. In essence, the pump places a buffer between the low LAN and the high LAN, pumps data from the low LAN to the high LAN, and probabilistically modulates the timing of the acknowledgments from the high LAN to the low LAN on the basis of the average transmission delay from the high LAN to the pump. The low level and high level enclaves communicate with the pump through special interfacing software called wrappers, which implement the pump protocol. Each wrapper is made of an application-dependent part, which supports the set of functionalities that satisfy application-specific requirements, and a pump-dependent part, which is a library of routines that implement the pump protocol. For security reasons, each process that uses the pump must register its address with the pump administrator.

In order to establish a connection, the low LAN has to send a connection request message to the main thread of the pump, which identifies the sending process and the address of the final destination. If both addresses are valid (i.e., they have been previously registered), the main thread sends back a connection valid message, otherwise it sends back a connection reject message. In the first case, the connection is managed by a trusted low thread and a trusted high thread, which are created during the connection setup phase to interact with the low LAN and the high LAN, respectively. Registered high processes are always ready to accept a connection from the pump through the same handshake mechanism seen above. Once the connection has been established, the pump sends a connection grant message to both LANs with initialization parameters for the communication. During the connection, the trusted low thread receives data messages from the low LAN, stores them in the connection buffer, and sends back the related acknowledgments by introducing an additional stochastic delay computed on the basis of the average rate at which the trusted high thread consumes messages. On the other hand, the trusted high thread delivers to the high LAN any data message contained in the connection buffer, and the high LAN has to send back to the trusted high thread the related acknowledgments before the expiration of a timeout. If the high LAN violates this protocol, the trusted high thread aborts the connection. In such a case, as soon as the trusted low thread detects that the trusted high thread is dead, it immediately sends to the low LAN all the remaining acknowledgments and a connection exit message. Another special message is connection close, which is sent by the low LAN to the pump at the end of a normal connection.

3.11.2 ÀEmilia Description

The following ÀEmilia specification called nrl_pump.aem describes the scenario illustrated above, which comprises a low wrapper, a main thread, a trusted high thread, a trusted low thread, a connection buffer, a high channel, and a high wrapper:

```
ARCHI_TYPE NRL_Pump_Type(const integer buffer_size := 1,
                          const rate conn_gen_rate := 10,
                          const rate conn_init_rate := 62.5,
                          const rate data_trans_rate := 125,
                          const rate ack_trans_rate := 1306.12,
                          const rate ack_delay_rate := 435.37,
                          const rate timeout_rate := 57.04,
                          const weight valid_prob := 0.99)

ARCHI_ELEM_TYPES

ELEM_TYPE LW_Type(const rate conn_gen_rate,
                   const rate data_trans_rate)

BEHAVIOR

LW_Beh(void; void) =
  <send_conn_request, exp(conn_gen_rate)>.
```
choice
{
  <receive_conn_valid, _> . <receive_conn_grant, _> .
  <send_msg, exp(data_trans_rate)> . <receive_low_ack, _> .
  choice
  {
    <receive_conn_exit, _> . LW_Beh(),
    <send_conn_close, exp(data_trans_rate)> . LW_Beh()
  },
  <receive_conn_reject, _> . LW_Beh()
}

INPUT_INTERACTIONS

UNI receive_conn_valid;
  receive_conn_grant;
  receive_conn_reject;
  receive_low_ack;
  receive_conn_exit

OUTPUT_INTERACTIONS

UNI send_conn_request;
  send_msg;
  send_conn_close

ELEM_TYPE MT_Type(const rate data_trans_rate,
                   const weight valid_prob)

BEHAVIOR

MT_Beh(void; void) =
  <receive_conn_request, _> .
  choice
  {
    <conn_is_valid, inf(1, valid_prob)> . <wakeup_tht, inf> .
    <send_conn_valid, exp(data_trans_rate)> . MT_Beh(),
    <conn_not_valid, inf(1, 1 - valid_prob)> .
    <send_conn_reject, exp(data_trans_rate)> . MT_Beh()
  }

INPUT_INTERACTIONS

UNI receive_conn_request

OUTPUT_INTERACTIONS

UNI wakeup_tht;
  send_conn_valid;
  send_conn_reject

ELEM_TYPE THT_Type(const rate conn_init_rate,
                    const rate timeout_rate)
BEHAVIOR

THT_Beh(void; void) =
  choice
  {
  <receive_high_wakeup, _> . <init_high_conn, exp(conn_init_rate)> .
  <wakeup_tlt, inf> . THT_Beh(),
  <read_msg, _> . <forward_msg, inf> .
  choice
  {
  <receive_high_ack, _> . <delete_msg, inf> .
  <send_ok_to_tlt, inf> . THT_Beh(),
  <wait_for_timeout, exp(timeout_rate)> . <comm_timeout, inf> .
  <delete_msg, inf> . <send_abort_to_tlt, inf> . THT_Beh()}
  }

INPUT_INTERACTIONS

UNI receive_high_wakeup;
read_msg;
receive_high_ack

OUTPUT_INTERACTIONS

UNI wakeup_tlt;
forward_msg;
delete_msg;
send_ok_to_tlt;
comm_timeout;
send_abort_to_tlt

ELEM_TYPE TLT_Type(const rate data_trans_rate,
const rate ack_trans_rate,
const rate ack_delay_rate)

BEHAVIOR

TLT_Beh(void; void) =
  <receive_low_wakeup, _> . <send_conn_grant, exp(data_trans_rate)> .
  <receive_msg, _> . <store_msg, inf> .
  choice
  {
  <wait_delay, exp(ack_delay_rate)> . <send_low_ack, exp(ack_trans_rate)> .
  choice
  {
  <receive_abort_from_tht, _> . <send_conn_exit, exp(data_trans_rate)> .
  TLT_Beh(),
  <receive_ok_from_tht, _> . <receive_conn_close, _> . TLT_Beh()}
  ,
  <receive_abort_from_tht, _> . <send_low_ack, exp(ack_trans_rate)> .
  <send_conn_exit, exp(data_trans_rate)> . TLT_Beh(),
<receive_ok_from_tht, _> . <wait_delay, exp(ack_delay_rate)> .
<send_low_ack, exp(ack_trans_rate)> . <receive_conn_close, _> . TLT_Beh()
}

INPUT_INTERACTIONS

UNI receive_low_wakeup;
  receive_msg;
  receive_abort_from_tht;
  receive_ok_from_tht;
  receive_conn_close

OUTPUT_INTERACTIONS

UNI send_conn_grant;
  store_msg;
  send_low_ack;
  send_conn_exit

ELEM_TYPE Buffer_Type(const integer buffer_size)

BEHAVIOR

Buffer_Beh(integer(0..buffer_size) msg_num := 0;
  void) =
  choice
  {
    cond(msg_num < buffer_size) ->
      <accept_msg, _> . Buffer_Beh(msg_num + 1),
    cond(msg_num > 0) ->
      choice
      {
        <read_msg, inf> . Buffer_Beh(msg_num),
        <delete_msg, _> . Buffer_Beh(msg_num - 1)
      }
  }

INPUT_INTERACTIONS

UNI accept_msg;
  delete_msg

OUTPUTINTERACTIONS

UNI read_msg

ELEM_TYPE HC_Type(const rate data_trans_rate,
                   const rate ack_trans_rate)

BEHAVIOR

HC_Beh(void; void) =
  <accept_msg, _> .

3.11 Example B: The NRL Pump

choice
{
   <receive_timeout, _> . HC_Beh(),
   <transmit_msg, exp(data_trans_rate)> . <accept_high_ack, _> .
   choice
   {
      <receive_timeout, _> . HC_Beh(),
      <transmit_high_ack, exp(ack_trans_rate)> . HC_Beh()
   }
}

INPUT_INTERACTIONS
UNI accept_msg;
   receive_timeout;
   accept_high_ack

OUTPUT_INTERACTIONS
UNI transmit_msg;
   transmit_high_ack

ELEM_TYPE HW_Type(void)

BEHAVIOR

HW_Beh(void; void) =
   <receive_msg, _> . <send_high_ack, inf> . HW_Beh()

INPUT_INTERACTIONS
UNI receive_msg

OUTPUT_INTERACTIONS
UNI send_high_ack

ARCHI_TOPOLOGY

ARCHI_ELEM_INSTANCES

LW : LW_Type(conn_gen_rate,
     data_trans_rate);
MT : MT_Type(data_trans_rate,
     valid_prob);
THT : THT_Type(conn_init_rate,
     timeout_rate);
TLT : TLT_Type(data_trans_rate,
     ack_trans_rate,
     ack_delay_rate);
B   : Buffer_Type(buffer_size);
HC  : HC_Type(data_trans_rate,
     ack_trans_rate);
HW : HW_Type()

ARCHI_INTERACTIONS

void

ARCHI_ATTACHMENTS

FROM LW.send_conn_request TO MT.receive_conn_request;
FROM MT.send_conn_valid TO LW.receive_conn_valid;
FROM MT.send_conn_reject TO LW.receive_conn_reject;
FROM MT.wakeup_tht TO THT.receive_high_wakeup;
FROM THT.wakeup_tlt TO TLT.receive_low_wakeup;
FROM TLT.send_conn_grant TO LW.receive_conn_grant;
FROM LW.send_msg TO TLT.receive_msg;
FROM TLT.store_msg TO B.accept_msg;
FROM TLT.send_low_ack TO LW.receive_low_ack;
FROM B.read_msg TO THT.read_msg;
FROM THT.forward_msg TO HC.accept_msg;
FROM HC.transmit_msg TO HW.receive_msg;
FROM THT.comm_timeout TO HC.receive_timeout;
FROM HW.send_high_ack TO HC.accept_high_ack;
FROM HC.transmit_high_ack TO THT.receive_high_ack;
FROM THT.delete_msg TO B.delete_msg;
FROM THT.send_abort_to_tlt TO TLT.receive_abort_from_tht;
FROM THT.send_ok_to_tlt TO TLT.receive_ok_from_tht;
FROM TLT.send_conn_exit TO LW.receive_conn_exit;
FROM LW.send_conn_close TO TLT.receive_conn_close

END

The formal parameters of the Æmilia specification represent the connection buffer capacity, the connection generation rate (one connection every 100 msec), the connection initialization rate (corresponds to the round-trip delay), the data and acknowledgment transmission rates, the acknowledgment delay rate (corresponds to the delay for transmitting 3 acknowledgments), the timeout rate (corresponds to twice the delay for transmitting a data message and the related acknowledgment), and the probability that a connection request is valid, respectively. The values of the rates are a consequence of the assumption that the channel capacity is 64 Kbps, the data message length is 512 bits, and the acknowledgment length is 49 bits.

LW_Type represents the wrapper at the sending site, which periodically generates a connection request. After sending the request, LW_Type is ready to accept either a connection reject message or a connection valid message followed by a connection grant message. If a connection is established, LW_Type sends a data message to the trusted low thread and then waits for the related acknowledgment. Afterwards, LW_Type can either receive a connection exit message in the case that the connection is aborted by the high LAN, or send a connection close message in the case that the connection is correctly terminated.

MT_Type listens to the port of the NRL Pump to which the low LAN sends connection request messages. We abstract away from the verification of the validity of an incoming request by assuming to know the probability of receiving a valid request. If a valid connection must be established, MT_Type awakens the main thread and sends a connection valid message to the low LAN, or send a connection close message in the case that the connection is correctly terminated.

TH_Type, which is spawned by the main thread during the setup phase, initializes the connection towards the high LAN. For the sake of simplicity, we assume that the high wrapper cannot refuse the connection request and we abstract away from the handshaking with the high wrapper through a single exponentially timed action. Afterwards, TH_Type awakens the trusted low thread. When the connection becomes active, TH_Type checks the buffer for new incoming data messages. Upon reading a message from the buffer,
3.11 Example B: The NRL Pump

THT_Type outputs it to the high communication channel. An immediate action is used to express the synchronization between THT_Type and the high communication channel, which in turn explicitly models the message transmission delay. Then, THT_Type waits for the reception of the related acknowledgment from the high LAN. The arrival of an acknowledgment competes with the timeout fixed by THT_Type. In particular, if the acknowledgment is received before the end of the timeout, THT_Type removes the message from the buffer and informs the trusted low thread about the successful transmission. On the other hand, if the timeout expires before the reception of the acknowledgment, the trusted high thread notifies the timeout expiration, removes the message from the buffer, and informs the trusted low thread about the aborted connection.

TLT_Type waits for the trusted high thread to awaken it, then establishes the connection from the low LAN to the pump by sending a connection grant message to the low LAN. At that moment, TLT_Type is ready to receive a data message from the low LAN. Upon receiving a data message, TLT_Type stores it in the connection buffer, then delays the transmission of the acknowledgment to the low LAN through an exponentially timed action. After the expiration of such a delay, TLT_Type sends the acknowledgment to the low LAN. At any moment, TLT_Type may receive a message from the trusted high thread concerning the status of the connection. In particular, in the case of trusted high thread failure, TLT_Type must send a connection exit message to the low LAN. On the contrary, if the trusted high thread is correctly working, TLT_Type can accept a connection close message from the low LAN. If TLT_Type detects the trusted high thread failure before sending the acknowledgment to the low LAN, then TLT_Type immediately transmits the acknowledgment and the connection exit message to the low LAN.

Buffer_Type, which is initially empty, can be accessed by the trusted low thread and the trusted high thread only. When Buffer_Type is not full, a new data message can be accepted from the trusted low thread. When Buffer_Type is not empty, a data message can be read or deleted by the trusted high thread.

HC_Type models the communications between the trusted high thread and the high LAN. We need an explicit component to express the transmission delay of messages along that link, because the round-trip delay of a communication between the trusted high thread and the high LAN must compete with the timeout set by the trusted high thread. Initially, HC_Type is ready to accept a data message from the trusted high thread. An incoming message is transmitted to the high LAN according to an exponentially distributed delay. After the delivery of the message, HC_Type waits for the related acknowledgment to be transmitted back to the trusted high thread. HC_Type is always willing to accept a timeout notification from the trusted high thread, in which case the connection will be aborted and all the pending messages will be dropped.

Finally, HW_Type represents the wrapper at the receiving site, which accepts data messages from the high channel and sends back the related acknowledgments.

We conclude by reporting the size of the semantic models of nrl_pump.aem:

Size of the integrated semantic model underlying NRL_Pump_Type:
- 46 states:
  - 20 tangible,
  - 26 vanishing,
  - 0 open,
  - 0 deadlocked;
- 58 transitions:
  - 58 observable,
  - 0 invisible;
  - 31 exponentially timed,
  - 27 immediate,
  - 0 passive.

Size of the functional semantic model underlying NRL_Pump_Type:
- 46 states:
  - 46 nondeadlocked,
- 0 deadlocked;
- 58 transitions:
  - 58 observable,
  - 0 invisible.

Size of the homogeneous continuous-time Markov chain underlying NRL_Pump_Type:
- 20 states:
  - 20 nonabsorbing,
  - 0 absorbing;
- 32 transitions.

### 3.12 Example C: Dining Philosophers

In this section we present a simple randomized distributed algorithm for the solution of a classical mutual exclusion problem, which illustrates the declaration of a parameterized architectural topology.

#### 3.12.1 Informal Description

Suppose there are $n$ philosophers sitting at a round table, each with a plate in front of him/her, and $n$ chopsticks on the table, each shared by two neighbor philosophers. Every philosopher alternately thinks and eats. In order to get the rice at the center of the table, a philosopher needs both the chopstick on his/her right and the chopstick on his/her left. The problem is that of defining a set of rules ensuring deadlock freedom, which the philosophers should follow whenever they are hungry in order to get the chopsticks they share with their neighbors.

The Lehmann-Rabin algorithm [28] provides a symmetric solution to the problem, in the sense that all the philosophers behave according to the same protocol. Whenever a philosopher is hungry, he/she flips a fair coin to decide which chopstick to pick up first, waits for that chopstick to become free, gets it, then tries to get the other chopstick. It is free, then the philosopher picks it up and starts eating, otherwise the philosopher puts down the first chopstick and restarts the whole process.

#### 3.12.2 Æmilia Description

The following Æmilia specification called `dining_philosophers.aem` describes the Lehmann-Rabin algorithm, assuming an exponential timing for the two activities carried out by every philosopher:

```plaintext
ARCHI_TYPE LR_Dining_Philosophers_Type(const integer philosopher_num := 3,
 const rate think_rate := 4.50,
 const rate eat_rate := 0.75)

ARCHI_ELEM_TYPES

ELEM_TYPE Philosopher_Type(const rate think_rate,
 const rate eat_rate)

BEHAVIOR

Philosopher_Thinking(void; void) =
<think, exp(think_rate)> . Philosopher_Picking();

Philosopher_Picking(void; void) =
```
3.12 Example C: Dining Philosophers

choice
{
  <flip_head, inf(1, 0.5)> . <pick_up_right_first, inf> .
  choice
  {
    <pick_up_left_then, inf(2, 1)> . Philosopher_Eating(),
    <put_down_right, inf> . Philosopher_Picking()
  },
  <flip_tail, inf(1, 0.5)> . <pick_up_left_first, inf> .
  choice
  {
    <pick_up_right_then, inf(2, 1)> . Philosopher_Eating(),
    <put_down_left, inf> . Philosopher_Picking()
  }
};

Philosopher_Eating(void; void) =
  <eat, exp(eat_rate)> . <put_down_right, inf> . <put_down_left, inf> .
  Philosopher_Thinking()

INPUT_INTERACTIONS

void

OUTPUT_INTERACTIONS

UNI pick_up_right_first;
  pick_up_right_then;
  put_down_right;
  pick_up_left_first;
  pick_up_left_then;
  put_down_left

ELEM_TYPE Chopstick_Type(void)

BEHAVIOR

Chopstick_Picking(void; void) =
  choice
  {
    <pick_up_first, _> . Chopstick_Putting(),
    <pick_up_then, _> . Chopstick_Putting()
  };

Chopstick_Putting(void; void) =
  <put_down, _> . Chopstick_Picking()

INPUT_INTERACTIONS

OR pick_up_first;
  pick_up_then;
  put_down
As far as the behavior is concerned, whenever both `pick_up_left_then` (resp. `pick_up_right_then`) and `put_down_right` (resp. `put_down_left`) are enabled, then the first one is executed as it has higher priority. We also observe that all the input interactions of the chopsticks are or-interactions, because each chopstick is shared by two neighbor philosophers, but only one of them at a time can use the chopstick.

On the topology side, we note that the indexing mechanism for the declaration of AEIs and attachments provides a concise and parameterized way to describe the application of the algorithm to an arbitrary number of philosophers.

Here is the size of the semantic models of `dining_philosophers.aem` for $n = 3$:

Size of the integrated semantic model underlying `LR_Dining_Philosophers_Type`:

- 109 states:
  - 13 tangible,
  - 96 vanishing,
  - 0 open,
  - 0 deadlocked;

- 147 transitions:
  - 147 observable,
- 0 invisible;
- 27 exponentially timed,
- 120 immediate,
- 0 passive.

Size of the functional semantic model underlying LR_Dining_Philosophers_Type:

- 109 states:
  - 109 nondeadlocked,
  - 0 deadlocked;

- 147 transitions:
  - 147 observable,
  - 0 invisible.

Size of the homogeneous continuous-time Markov chain underlying LR_Dining_Philosophers_Type:

- 13 states:
  - 13 nonabsorbing,
  - 0 absorbing;

- 30 transitions.

The size of the state space grows by a multiplicative factor between three and four with respect to the number $n$ of philosophers. As an example, for $n = 10$ the integrated semantic model of dining.philosophers.aem has 175887 states and 282530 transitions.
Chapter 4

The Equivalence Verifier

4.1 Introduction

TwoTowers 5.1 is able to check whether two correct Æmilia specifications – in which all the possible variable formal parameters and local variables are of type bounded integer, boolean, or array or record based on the two previous basic types – are equivalent. The verification is carried out by applying the partition refinement algorithm by Kanellakis and Smolka [24] and the result of the check is written to a .evr file, together with a distinguishing modal logic formula [15] – in the case of non-equivalence – expressed in a verbose variant of the Hennessy-Milner logic [20] or one of its probabilistic extensions [27, 13].

The equivalence verifier allows a comparative study of two Æmilia specifications to be conducted, aiming at establishing whether they possess the same functional, security and performance properties in general. Should the two Æmilia specifications be equivalent, in order to know whether they satisfy a particular functional property, security requirement, or performance guarantee, it is necessary to apply to one of them the model checker, the security analyzer, or the performance evaluator, respectively.

4.2 Bisimulation-Based Behavioral Equivalences

Four different bisimulation-based behavioral equivalences are available in TwoTowers 5.1: strong bisimulation equivalence, weak bisimulation equivalence, strong (extended) Markovian bisimulation equivalence, and weak (extended) Markovian bisimulation equivalence [29, 10, 6].

Strong bisimulation equivalence relates two Æmilia specifications if they are able to simulate each other’s functional behavior. For each pair of strongly bisimilar states of the integrated semantic models of the two Æmilia specifications, it must be the case that, whenever one of the two states is able to perform an action of a certain type, then the other state is able to perform an action of the same type, with the two reached states being again strongly bisimilar.

Weak bisimulation equivalence is a coarser variant of the previous equivalence, in which it is possible – to some extent – to abstract from the execution of invisible actions, i.e. those actions whose type has been hidden in the behavioral section of the Æmilia specifications to which equivalence checking is applied. In essence, given a pair of weakly bisimilar states of the integrated semantic models of two Æmilia specifications, it must be the case that, whenever one of the two states is able to perform an action of a certain type, then the other state is able to perform an action of the same type possibly preceded and followed by the execution of invisible actions, with the two reached states being again weakly bisimilar.

Strong Markovian bisimulation equivalence is a finer variant of the first equivalence, which takes into account timing/probabilistic aspects as well. Given a pair of strongly Markovian bisimilar states of the integrated semantic models of two Æmilia specifications, it must be the case that, whenever one of the two states is able to perform a set of actions of a certain type and priority, then the other state is able to perform a set of actions of the same type and priority, with both states reaching the same equivalence class of states with the same aggregated rate.
Weak Markovian bisimulation equivalence is a coarser variant of the previous equivalence, in which it is possible – to some extent – to abstract from the execution of invisible immediate actions in the continuous-time case. Basically, given a pair of weakly Markovian bisimilar states of the integrated semantic models of two Æmilia specifications, it must be the case that, whenever one of the two states is able to perform a set of actions of a certain type and priority, then the other state is able to perform a set of actions of the same type and priority, each possibly preceded and followed by the execution of invisible immediate actions, with both states reaching the same equivalence class of states with the same aggregated rate.

Two Æmilia specifications are equivalent in accordance with one of the four equivalences above whenever so are the initial global states of their integrated semantic models. We recall that each of the four bisimulation-based equivalences is deadlock sensitive, i.e. it never equates a deadlock-free Æmilia specification to an Æmilia specification that can deadlock, and that the two Markovian ones comply with the notion of exact aggregation for Markov chains known as ordinary lumping [11, 21].

### 4.3 Syntax of Distinguishing Formulas

Whenever two Æmilia specifications are not found to be equivalent, a distinguishing modal logic formula is produced, which has the following syntax:

\[
<\text{formula_expr}> ::= \text{"TRUE"} \\
| \text{"FALSE"} \\
| <\text{formula_expr}> "\&\" <\text{formula_expr}> \\
| <\text{formula_expr}> "\|\" <\text{formula_expr}> \\
| \text{"NOT" }(" <\text{formula_expr}> \text{"} )") \\
| \text{"EXISTS_TRANS" }(" \text{"LABEL" }(" <\text{action_type_label}> \text{"} )" ;" \\
| \text{"REACHED_STATE_SAT" }(" <\text{formula_expr}> \text{"} )") \\
| \text{"EXISTS_WEAK_TRANS" }(" \text{"LABEL" }(" <\text{action_type_label}> \text{"} )" ;" \\
| \text{"REACHED_STATE_SAT" }(" <\text{formula_expr}> \text{"} )") \\
| \text{"FOR_ALL_TRANS" }(" \text{"LABEL" }(" <\text{action_type_label}> \text{"} )" ;" \\
| \text{"REACHED_STATE_SAT" }(" <\text{formula_expr}> \text{"} )") \\
| \text{"FOR_ALL_WEAK_TRANS" }(" \text{"LABEL" }(" <\text{action_type_label}> \text{"} )" ;" \\
| \text{"REACHED_STATE_SAT" }(" <\text{formula_expr}> \text{"} )") \\
| \text{"EXISTS_TRANS_SET" }(" \text{"LABEL" }(" <\text{action_type_label}> \text{"} )" ;" \\
| <\text{min_value_type}> \\
| \text{"REACHED_STATES_SAT" }(" <\text{formula_expr}> \text{"} )") \\
| \text{"EXISTS_WEAK_TRANS_SET" }(" \text{"LABEL" }(" <\text{action_type_label}> \text{"} )" ;" \\
| <\text{min_value_type}> \\
| \text{"REACHED_STATES_SAT" }(" <\text{formula_expr}> \text{"} )") \\
| \text{"FOR_ALL_TRANS_SETS" }(" \text{"LABEL" }(" <\text{action_type_label}> \text{"} )" ;" \\
| <\text{min_value_type}> \\
| \text{"REACHED_STATES_SAT" }(" <\text{formula_expr}> \text{"} )") \\
| \text{"FOR_ALL_WEAK_TRANS_SETS" }(" \text{"LABEL" }(" <\text{action_type_label}> \text{"} )" ;" \\
| <\text{min_value_type}> \\
| \text{"REACHED_STATES_SAT" }(" <\text{formula_expr}> \text{"} )")
\]

\[
<\text{min_value_type}> ::= \text{"MIN_AGGR_EXP_RATE"} \\
| \text{"MIN_AGGR_GEN_PROB"} \\
| \text{"MIN_AGGR_REA_PROB"}
\]

where the satisfaction relation with respect to a given state of the integrated semantic model of an Æmilia specification is defined as follows:

- Constant \text{"TRUE"} is satisfied in every state, while constant \text{"FALSE"} is never satisfied.
- The logical conjunction (\text{"\&\"}) of two properties is satisfied in a given state if so are both properties.
• The logical disjunction (\lor) of two properties is satisfied in a given state if so is at least one of the two properties.
• The logical negation (\neg) of a property is satisfied in a given state if the property is not satisfied in that state.
• Quantifier \texttt{EXISTS\_TRANS} expresses, with respect to a given state, the fact that from that state it is possible to reach a state satisfying a certain property by traversing a transition that is labeled with a certain action type.
• Quantifier \texttt{EXISTS\_WEAK\_TRANS} expresses, with respect to a given state, the fact that from that state it is possible to reach a state satisfying a certain property by traversing a sequence of transitions, with one of them being labeled with a certain action type and all the others being invisible.
• Quantifier \texttt{FOR\_ALL\_TRANS} expresses, with respect to a given state, the fact that whenever a transition labeled with a certain action type can be traversed from that state, the reached state necessarily satisfies a certain property.
• Quantifier \texttt{FOR\_ALL\_WEAK\_TRANS} expresses, with respect to a given state, the fact that whenever a sequence of transitions, with one of them being labeled with a certain action type and all the others being invisible, can be traversed from that state, the reached state necessarily satisfies a certain property.
• Quantifier \texttt{EXISTS\_TRANS\_SET} expresses, with respect to a given state, the fact that from that state it is possible to reach a set of states satisfying a certain property by traversing a set of transitions that are labeled with a certain action type of a certain priority, whose aggregated rate is above a certain threshold.
• Quantifier \texttt{EXISTS\_WEAK\_TRANS\_SET} expresses, with respect to a given state, the fact that from that state it is possible to reach a set of states satisfying a certain property by traversing a set of sequences of transitions whose aggregated rate is above a certain threshold, with every sequence having one transition labeled with a certain action type of a certain priority and all the other transitions in the sequence being invisible and immediate.
• Quantifier \texttt{FOR\_ALL\_TRANS\_SETS} expresses, with respect to a given state, the fact that whenever a set of transitions, labeled with a certain action type of a certain priority and having an aggregated rate above a certain threshold, can be traversed from that state, the reached states necessarily satisfy a certain property.
• Quantifier \texttt{FOR\_ALL\_WEAK\_TRANS\_SETS} expresses, with respect to a given state, the fact that whenever a set of sequences of transitions whose aggregated rate is above a certain threshold, with every sequence having one transition labeled with a certain action type of a certain priority and all the other transitions in the sequence being invisible and immediate, can be traversed from that state, the reached states necessarily satisfy a certain property.

The last four formulas specify a lower bound for the aggregated rate of the considered set of transitions or transition sequences, which is a positive real number interpreted as an aggregated exponential rate, a generative probability, or a reactive probability depending on whether the considered action type refers to an exponentially timed, immediate or passive action, respectively.

When concerned with an Æmilia specification, a modal logic formula expressed in the syntax above holds if it is satisfied by the initial global state of the integrated semantic model of the Æmilia specification.

4.4 Example A: The Alternating Bit Protocol

From an abstract point of view, the system behavior enforced by the application of the alternating bit protocol is the same as the behavior of a one-position buffer, in which messages are alternately generated and consumed. This can be formalized through the following \texttt{abp\_spec\_aem}:
ARCHI_TYPE ABP_Spec_Type(const rate msg_gen_rate := 5)

ARCHI_ELEM_TYPES

ELEM_TYPE One_Pos_Buffer_Type(const rate msg_gen_rate)

BEHAVIOR

One_Pos_Buffer(void;
void) =
<generate_msg, exp(msg_gen_rate)>.<consume_msg, inf>.One_Pos_Buffer()

INPUT_INTERACTIONS

UNI generate_msg

OUTPUT_INTERACTIONS

UNI consume_msg

ARCHI_TOPOLOGY

ARCHI_ELEM_INSTANCES

OPB : One_Pos_Buffer_Type(msg_gen_rate)

ARCHI_INTERACTIONS

OPB.generate_msg;
OPB.consume_msg

ARCHI_ATTACHMENTS

void

END

Now the question is whether the Æmilia specification abp.aem of Sect. 3.10.2 is equivalent to the Æmilia specification abp.spec.aem, which would imply the correctness of abp.aem. Before applying equivalence verification, we need to modify both specifications to get rid of the dot notation for the observable action types, and in abp.aem we have to hide all the action types not related to message generation or consumption, as these are the only ones occurring in abp.spec.aem — hence the only ones that can be matched in the bisimulation setting. Therefore, we rewrite abp.aem into abp.impl.aem by defining a new architectural type called ABP_Impl_Type with the same parameters, AETs, and architectural topology as before, and in addition the following behavioral variations:

BEHAV_VARIATIONS

BEHAV_HIDINGS

HIDE LM.ALL;
HIDE LA.ALL;
HIDE S.timeout
Then we add the following behavioral variations to `abp_spec.aem`:

```
BEHAV_RENAMINGS

RENAME OPB.generate_msg AS generate_msg;
RENAME OPB.consume_msg AS consume_msg
```

The result of the strong bisimulation equivalence verification is the following:

```
ABP_Impl_Type isn't strongly bisimulation equivalent to ABP_Spec_Type
as demonstrated by the following modal logic formula
satisfied by ABP_Impl_Type but not by ABP_Spec_Type:

NOT(EXISTS_TRANS(
    LABEL(generate_msg);
    REACHED_STATE_SAT(
        EXISTS_TRANS(
            LABEL(consume_msg);
            REACHED_STATE_SAT(TRUE)
        )
    )
)
```

which means that the second specification can consume a message right after its generation, while this is not possible in the case of the first specification because of its actions explicitly modeling message transmission, propagation, loss, and delivery. In other words, we cannot expect the two Æmilia specifications to be strongly bisimulation equivalent, as the invisible actions – modeling details related to the message flow – of `abp_impl.aem` cannot be matched by any of the actions of `abp_spec.aem`.

The result of the weak bisimulation equivalence verification is the following:

```
ABP_Impl_Type is weakly bisimulation equivalent to ABP_Spec_Type.
```

This ensures that the two specifications have the same functional behavior up to invisible actions. So, it is now worth investigating whether the two specifications guarantees the same performance.

The following are the results of the strong and weak Markovian bisimulation equivalence verifications:

```
ABP_Impl_Type isn't strongly Markovian bisimulation equivalent to ABP_Spec_Type
as demonstrated by the following modal logic formula
satisfied by ABP_Impl_Type but not by ABP_Spec_Type:

NOT(EXISTS_TRANS_SET(
    LABEL(generate_msg);
    MIN_AGGR_EXP_RATE(5.000000);
    REACHED_STATES_SAT(
        EXISTS_TRANS_SET(
            LABEL(consume_msg);
            MIN_AGGR_GEN_PROB(1.000000);
```


ABP_Impl_Type isn’t weakly Markovian bisimulation equivalent to ABP_Spec_Type as demonstrated by the following modal logic formula satisfied by ABP_Impl_Type but not by ABP_Spec_Type:

\[
\text{NOT}(\exists \text{WEAK TRANS SET}(
\quad \text{LABEL}(\text{generate msg});
\quad \text{MIN AGGR EXP RATE}(5.000000);
\quad \text{REACHED STATES SAT}(
\quad \exists \text{WEAK TRANS SET}(
\quad \quad \text{LABEL}(\text{consume msg});
\quad \quad \text{MIN AGGR GEN PROB}(1.000000);
\quad \quad \text{REACHED STATES SAT}(\text{TRUE})
\quad )
\quad )
\quad )
\]

As we should have expected, the two Œmilia specifications are not equivalent from the performance viewpoint. The reason is that abp.spec.aem completely abstracts from message losses as well as propagation delays. The same results are obtained when considering the value passing Œmilia specification abp.vp.aem of Sect. 3.10.3 – enriched with suitable behavioral variations – in place of abp_impl.aem.
Chapter 5

The Model Checker

5.1 Introduction

TwoTowers 5.1 is able to check whether certain functional properties, each expressed as a LTL formula [14] in a .ltl file, are satisfied by a correct Æmilia specification, in which all the possible variable formal parameters and local variables are of type bounded integer, boolean, or array or record based on the two previous basic types. The verification is carried out by invoking the symbolic model checker NuSMV 2.2.5 [12] and the result of the check is written to a .mcr file, together with a counterexample for each property that is not satisfied.

5.2 Syntax of .ltl Specifications

A .ltl specification is a non-empty sequence of semicolon-separated property definitions, each of the following form:

<property_def> ::= "PROPERTY" <identifier> ["[" <expr> "]"] "IS" <property_expr>
    | "FOR_ALL" <identifier> "IN" <expr> ".." <expr>
    "PROPERTY" <identifier> ["[" <expr> "])" "IS" <property_expr>

In its simpler form, a property definition contains the identifier of the property, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the property expression. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification to which the model checking is applied.

The second form is useful to concisely define several variants of the same property through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression and in the property expression, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

We observe that the identifier of a property can be augmented with a selector expression also in the simpler form of property definition. This is useful whenever it is desirable to define a set of indexed variants of the same property, but only some of them have a common selector expression.

The property expression is based on propositional and LTL operators and has the following verbose syntax:

<property_expr> ::= "TRUE"
    | "FALSE"
where the satisfaction relation with respect to a given state of the functional semantic model of an Æmilia specification is defined as follows:

- Constant `TRUE` is satisfied in every state, while constant `FALSE` is never satisfied.
- The logical conjunction (`\`\) of two properties is satisfied in a given state if so are both properties.
- The logical disjunction (`\`\) of two properties is satisfied in a given state if so is at least one of the two properties.
- The logical negation (NOT) of a property is satisfied in a given state if the property is not satisfied in that state.
- The logical exclusive disjunction (`\`\) of two properties is satisfied in a given state if so is exactly one of the two properties.
- The logical implication (`\`\) between two properties is satisfied in a given state if it is not the case that the first property is satisfied while the second one is not.
- The logical equivalence (`\`\) between two properties is satisfied in a given state if both properties are satisfied or none of them is.
- Constant `DEADLOCK_FREE` is satisfied in a given state if no computation path starting from that state deadlocks.
- The property expression after `DEADLOCK_FREE` in the syntax above represents an action type, which is denoted through its identifier preceded by the identifier of the AEI possibly augmented with an integer-valued selector expression enclosed in square brackets, which must be free of undeclared identifiers and invocations to pseudo-random number generators. The AEI must be declared in the Æmilia specification to which the model checking is applied, and the action type must occur in the behavior of the type of the AEI. This property is satisfied in a given state if, along every computation path starting from that state, the state executes an action with the specified type (or a synchronizing type involving it, or a type renaming it).
- Operator `NEXT_STATE_SAT` expresses with respect to a given state the fact that, for every computation path traversing that state, the next state along the path satisfies a certain property.
5.3 Example A: The Alternating Bit Protocol

- Operator `ALL_FUTURE_STATES_SAT` expresses with respect to a given state the fact that, for every computation path traversing that state, the traversed state and all the subsequent ones along the path satisfy a certain property.

- Operator `SOME_FUTURE_STATE_SAT` expresses with respect to a given state the fact that, for every computation path traversing that state, there exists a state among the traversed one and all the subsequent ones along the path that satisfies a certain property.

- Operator `UNTIL` expresses with respect to a given state the fact that, for every computation path traversing that state, there exists a state among the traversed one and all the subsequent ones along the path that satisfies the second property, with all the states between the traversed one and the one that satisfies the second property satisfying the first property.

- Operator `RELEASES` expresses with respect to a given state the fact that, for every computation path starting from that state, all the states among the traversed one and the subsequent ones along the path satisfy the second property up to and including the first state (if any) that satisfies the first property.

- Operator `PREV_STATE_SAT` expresses with respect to a given state the fact that, for every computation path traversing that state, the previous state along the path satisfied a certain property.

- Operator `ALL_PAST_STATES_SAT` expresses with respect to a given state the fact that, for every computation path traversing that state, the traversed state and all the previous ones along the path satisfied a certain property.

- Operator `SOME_PAST_STATE_SAT` expresses with respect to a given state the fact that, for every computation path traversing that state, there exists a state among the traversed one and all the previous ones along the path that satisfied a certain property.

- Operator `SINCE` expresses with respect to a given state the fact that, for every computation path traversing that state, there exists a state among the traversed one and all the previous ones along the path that satisfied the second property, with all the states between the traversed one and the one that satisfied the second property satisfying the first property.

- Operator `TRIGGERED` expresses with respect to a given state the fact that, for every computation path traversing that state, all the states among the traversed one and the previous ones along the path satisfied the second property up to and including the first state (if any) that satisfied the first property.

The infix temporal operators `UNTIL`, `RELEASES`, `SINCE`, and `TRIGGERED` take precedence over the logical conjunction operator, which takes precedence over the two logical disjunction operators, which takes precedence over the logical equivalence operator, which takes precedence over the logical implication operator. All the mentioned infix operators are left associative, except for the logical implication one, which is right associative. The precedence and associativity of such operators can be altered using parentheses ( ).

When checked against an Φmelia specification, a property expressed in a .ltl file holds if it is satisfied by the initial global state of the functional semantic model of the Φmelia specification.

5.3 Example A: The Alternating Bit Protocol

The correctness of the Φmelia specification `abp.aem` of Sect. 3.10.2 can be checked against the following `abp.ltl`:

```
PROPERTY deadlock_freedom IS
  DEADLOCK_FREE;

PROPERTY always_consumes_after_generating IS
  ALL_FUTURE_STATES_SAT(R.consume_msg -> SOME_PAST_STATE_SAT(S.generate_msg));
```
The Model Checker

PROPERTY correct_alternation IS
   ALL_FUTURE_STATES_SAT(
      (S.generate_msg -> (NEXT_STATE_SAT((NOT(S.generate_msg) UNTIL R.consume_msg) \
                                    NOT(R.consume_msg)))) \
      AND
      (R.consume_msg -> (NEXT_STATE_SAT((NOT(R.consume_msg) UNTIL S.generate_msg) \
                                    NOT(S.generate_msg))))
   )

The first property ensures that the protocol never causes a deadlock to occur. The second property guarantees
that, whenever a message is consumed at the receiver side, then it must have been previously generated at the
sender side. The third property establishes that message generations and consumptions correctly alternate.
Whenever a message is generated at the sender side, then along every computation path it must be the
case that either no new message is generated until the considered one is consumed at the receiver side, or no
further message generations and consumptions take place. Likewise, whenever a message is consumed at the
receiver side, then along every computation path it must be the case that either no message is consumed until
a new one is generated at the sender side, or no further message generations and consumptions take place.

The following is the result of the model checking:

Validity of the properties for ABP_Type:
- Property "deadlock_freedom" is satisfied.
- Property "always_consumes_after_generating" is satisfied.
- Property "correct_alternation" is satisfied.

5.4 Example C: Dining Philosophers

The correctness of the Æmilia specification dining_philosophers.aem of Sect. 3.12.2 can be checked against
the following dining_philosophers.ltl:

PROPERTY deadlock_freedom IS
   DEADLOCK_FREE;

FOR_ALL i IN 0..philosopher_num - 1
   PROPERTY starvation_freedom[i] IS
      ALL_FUTURE_STATES_SAT(SOME_FUTURE_STATE_SAT(P[i].eat));

FOR_ALL i IN 0..philosopher_num - 1
   PROPERTY no_adjacent_philosopher_simultaneously_eating[i] IS
      ALL_FUTURE_STATES_SAT(\n         P[i].eat -> NEXT_STATE_SAT(\n            NOT(P[mod(i + 1, philosopher_num)].eat) \\n            NOT(P[mod((philosopher_num + i) - 1, philosopher_num)].eat)
            UNTIL P[i].put_down_left)\n         )

The first property ensures that the algorithm avoids deadlock, in the sense that whenever several philosophers
are hungry, at least one of them manages to get the chopsticks and eat. The second set of properties
guarantees that no philosopher starves, i.e. whenever a philosopher is hungry, it eventually manages to eat.
The third set of properties establishes the mutual exclusive usage of the chopsticks, in the sense that whenever
a philosopher eats, then none of its two neighbors can eat until the philosopher releases both chopsticks.

What follows is the result of the model checking, where for each unsatisfied property a computation path
violating it is printed as the sequence of the types of the actions executed along the path, together with the
indication of possible loops in the path:
Validity of the properties for LR_Dining_Philosophers_Type:

- Property "deadlock_freedom" is satisfied.

- Property "starvation_freedom[0]" isn't satisfied as demonstrated by the following execution sequence:

  ```
  <<<loop starts here>>>
  P[1].think
  P[1].flip_tail
  C[2].pick_up_first.2#P[1].pick_up_left_first
  C[1].pick_up_then.1#P[1].pick_up_right_then
  P[1].eat
  C[1].put_down.1#P[1].put_down_right
  C[2].put_down.2#P[1].put_down_left
  P[1].think
  ```

- Property "starvation_freedom[1]" isn't satisfied as demonstrated by the following execution sequence:

  ```
  <<<loop starts here>>>
  P[1].think
  P[1].flip_head
  C[1].pick_up_first.1#P[1].pick_up_right_first
  C[2].pick_up_then.2#P[1].pick_up_left_then
  P[2].think
  P[2].flip_head
  P[0].think
  <<<loop starts here>>>
  P[0].flip_head
  C[0].pick_up_first.1#P[0].pick_up_right_first
  C[0].put_down.1#P[0].put_down_right
  P[0].flip_head
  ```

- Property "starvation_freedom[2]" isn't satisfied as demonstrated by the following execution sequence:

  ```
  <<<loop starts here>>>
  P[1].think
  P[1].flip_tail
  C[2].pick_up_first.2#P[1].pick_up_left_first
  C[1].pick_up_then.1#P[1].pick_up_right_then
  P[1].eat
  C[1].put_down.1#P[1].put_down_right
  C[2].put_down.2#P[1].put_down_left
  P[1].think
  ```

- Property "no_adjacent_philosopher_simultaneously_eating[0]" is satisfied.

- Property "no_adjacent_philosopher_simultaneously_eating[1]" is satisfied.

- Property "no_adjacent_philosopher_simultaneously_eating[2]" is satisfied.
Chapter 6

The Security Analyzer

6.1 Introduction

TwoTowers 5.1 is able to check whether certain information flow properties, which are related to the security levels of the system activities as expressed in a .sec file, are satisfied by a correct Æmilia specification, in which all the possible variable formal parameters and local variables are of type bounded integer, boolean, or array or record based on the two previous basic types. The analysis is carried out by means of the equivalence verifier and the result of the check is written to a .sar file, together with a modal logic formula expressed in a verbose variant of the Hennessy-Milner logic [20] (see Sect. 4.3) to explain a possible security violation.

6.2 Security Properties

Two different security properties can be analyzed with TwoTowers 5.1: non-interference and non-deducibility on composition [19].

Supposing that low security users observe public operations only while high security users perform confidential operations only, an interference from high security users to low security users occurs if what the high users can do is reflected in what the low users can observe. Formally, given an Æmilia specification and classified each of its action types as being high, low or irrelevant from the security viewpoint, non-interference is satisfied if the functional semantic model of the Æmilia specification with all the high action types being hidden is weakly bisimulation equivalent to the functional semantic model of the Æmilia specification with all the high action types being restricted (the irrelevant action types are hidden in both models). In this case the low users cannot infer the behavior of the high users by observing the public view of the system, because the low users are not able to distinguish between the situation in which the high users are carrying out some confidential operation and the opposite situation in which the high users are not doing anything. This means that the system does not leak any secret information from the high users to the low users.

Non-deducibility on composition is about the capability of altering or not the system view of the low users when considering each of their potential interactions with the high users. Formally, given an Æmilia specification and the usual security-based classification of its action types, non-deducibility on composition is satisfied if, for each pair of states of the functional semantic model of the Æmilia specification such that the first one has a transition that reaches the second one and is labeled with a high action type, the two states are weakly bisimulation equivalent after restricting all the high action types (and hiding all the irrelevant ones). This means that the low users are not able to note any difference in the system behavior before and after each interaction with the high users.

The second property is more restrictive than the first one. Whenever an Æmilia specification satisfies non-deducibility on composition, then it satisfies non-interference as well.
6.3 Syntax of .sec Specifications

A .sec specification has the following syntax

"HIGH_SECURITY" <security_decl_sequence> "LOW_SECURITY" <security_decl_sequence>

where <security_decl_sequence> is a non-empty sequence of semicolon-separated security declarations, each of the following form:

<security_decl> ::= "OBS_NRESTR_INTERNALS"
| "OBS_NRESTR_INTERACTIONS"
| "ALL_OBS_NRESTR"
| <identifier> ["[" <expr> "]"] "." <action_type_set_s>
| "FOR_ALL" <identifier> "IN" <expr> ".." <expr>
| <identifier> ["[" <expr> "]"] "." <action_type_set_s>

<action_type_set_s> ::= <identifier>
| "OBS_NRESTR_INTERNALS"
| "OBS_NRESTR_INTERACTIONS"
| "ALL_OBS_NRESTR"

In its simpler form, a security declaration consists of associating a high or low security level with all the observable, non-restricted action types that are internal to the AEIs of the Æmilia specification, all the observable, non-restricted interactions of the AEIs of the Æmilia specification, or both of them. Alternatively, it is possible to associate a high or low security level with a set of action types of a specific AEI. In this case, the security declaration contains the identifier of the AEI to which the high/low action types belong, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the identifier of the high/low security action type or one of the three shorthands above for sets of high/low security action types. If specified, the AEI must be declared in the Æmilia specification to which the security analysis is applied. If specified, the high/low security action type must occur in the behavior of the type of the AEI and cannot be hidden or restricted. Moreover, a high security action type cannot be redeclared to be low security. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification.

The more complex form is useful to concisely declare several action types to be at the same security level through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

6.4 Example B: The NRL Pump

In order to check for the absence of illegal information flows in the Æmilia specification nrl_pump.aem of Sect. 3.11.2, we classify its action types through the following nrl_pump.sec:

HIGH_SECURITY HW.ALL_OBS_NRESTR

LOW_SECURITY LW.ALL_OBS_NRESTR

where all the action types of the high (resp. low) wrapper are declared to be high (resp. low) security. The following is the result of the non-interference analysis:
NRL_Pump_Type violates the non-interference property as demonstrated by the following modal logic formula satisfied when the high security actions are hidden but not when the high security actions are restricted:

```
EXISTS_WEAK_TRANS(
  LABEL(LW.send_conn_request#MT.receive_conn_request);
  REACHED_STATE_SAT(
    EXISTS_WEAK_TRANS(
      LABEL(LW.receive_conn_valid#MT.send_conn_valid);
      REACHED_STATE_SAT(TRUE)
    ) /
    NOT(EXISTS_WEAK_TRANS(
      LABEL(LW.receive_conn_valid#MT.send_conn_valid);
      REACHED_STATE_SAT(
        EXISTS_WEAK_TRANS(
          LABEL(LW.receive_conn_grant#TLT.send_conn_grant);
          REACHED_STATE_SAT(
            NOT(EXISTS_WEAK_TRANS(
              LABEL(LW.send_msg#TLT.receive_msg);
              REACHED_STATE_SAT(
                EXISTS_WEAK_TRANS(
                  LABEL(LW.receive_low_ack#TLT.send_low_ack);
                  REACHED_STATE_SAT(
                    EXISTS_WEAK_TRANS(
                      LABEL(LW.send_conn_close#TLT.receive_conn_close);
                      REACHED_STATE_SAT(TRUE)
                    )
                  )
                )
              )
            )
          )
        )
      )
    )
  )
)
```

The negative outcome above shows that, because of the acknowledgment mechanism, all the connections are always aborted in the absence of high users, whereas some connections can successfully terminate in the presence of high users. This reveals the existence of a covert channel related to a connect/disconnect strategy, which a malicious high user may set up to pass confidential information to some low user.

Since nrl_pump.aem does not satisfy non-interference, it cannot satisfy non-deducibility on composition, either. In fact, the following is the result of the non-deducibility on composition analysis:
NRL_Pump_Type violates the non-deducibility on composition property as demonstrated by the following modal logic formula satisfied by global state 45 with the high security actions restricted but not by global state 27 with the high security actions restricted:

\[
\text{NOT} (\exists \text{WEAK TRANS}(\text{LABEL}(\text{LW.send_conn_close} \# \text{TLT.receive_conn_close}); \text{REACHED_STATE}_\text{SAT}(\text{TRUE}))
\]
Chapter 7

The Performance Evaluator

7.1 Introduction

TwoTowers 5.1 is able to evaluate the performance of correct \(\text{\AE}milia\) specifications in two different ways. In the first case instant-of-time, stationary/transient performance measures, which are defined through state and transitions rewards [22] in a .rew file, are computed by solving the Markov chain underlying the \(\text{\AE}milia\) specification. The value of each such performance measure, which is written to a .val file, is given by the sum of the stationary/transient state probabilities and transition frequencies of the Markov chain, each weighed by the corresponding state reward or transition reward, respectively. A state reward represents the rate at which gain is cumulated while staying in a certain state, whereas a transition reward represents the gain that is instantaneously earned when executing a certain transition. In TwoTowers 5.1 three methods are available for solving Markov chains: Gaussian elimination, an adaptive variant of symmetric stochastic over-relaxation, and uniformization [32]. Gaussian elimination is an exact method for computing the stationary solution of small Markov chains (up to a few thousands of states), while symmetric stochastic over-relaxation is an iterative method for computing the stationary solution of larger Markov chains. On the contrary, uniformization is an iterative method for computing the transient solution of Markov chains. The state probability distribution representing the solution of a Markov chain is written to a .dis file. The Markovian performance evaluation can be applied only to (correct and) performance closed \(\text{\AE}milia\) specifications in which all the possible variable formal parameters and local variables are of type bounded integer, boolean, or array or record based on the two previous basic types.

In the second case the method of independent replications [34], based on simulation experiments described in a .sim file, is applied to estimate with 90% confidence level the mean, variance or distribution of performance measures, which are specified through an extension of state and transition rewards in the same .sim file. The discrete event simulation can be trace driven, which means that certain values are taken from a .trc file instead of being sampled from pseudo-random number generators. The result of the simulation is written to a .est file. Unlike the Markovian performance evaluation, the simulation-based performance evaluation can be applied to any (correct) \(\text{\AE}milia\) specification with no open and deadlock states, thus making it possible the estimation of the performance measures of systems with generally distributed delays. Besides the compile-time crashes mentioned in Sect. 3.9.4, the discrete event simulation of an \(\text{\AE}milia\) specification can be interrupted – during the construction of the portion of the integrated semantic model that is necessary to make the simulation advance – because of the generation of a deadlock state, the generation of an open state, or the absence of sufficiently many values to be read from a .trc file.

7.2 Syntax of .rew Specifications

A .rew specification is a non-empty sequence of semicolon-separated measure definitions, each of the following form:

\[
\text{<measure_def>} ::= \"MEASURE\" <identifier> [\"[\ "<expr> "]\"] \"IS\" <reward_structure>
\]
In its simpler form, a measure definition contains the identifier of the measure, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the reward structure. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification to which the Markovian performance evaluation is applied.

The second form is useful to concisely define several variants of the same measure through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression and in the reward structure, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

We observe that the identifier of a measure can be augmented with a selector expression also in the simpler form of measure definition. This is useful whenever it is desirable to define a set of indexed variants of the same measure, but only some of them have a common selector expression.

The reward structure is a non-empty sequence of reward assignments, each of the following form:

```
<reward_assign> ::= "ENABLED" "(" <identifier> ")" 
"->" <reward_type> "(" <expr> ")"
```

In its simpler form, a reward assignment contains the identifier of an action type preceded by the identifier of an AEI possibly augmented with an integer-valued selector expression enclosed in square brackets, which must be free of undeclared identifiers and invocations to pseudo-random number generators. The AEI must be declared in the Æmilia specification to which the Markovian performance evaluation is applied, and the action type must occur in the behavior of the type of the AEI within non-passive actions. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification.

The meaning is that, whenever an action with the specified type is enabled in a state (resp. the transition that leaves that state and is originated from the considered action) is associated a state (resp. transition) reward given by the value of the expression following symbol ->. The reward expression must be real valued as well as free of undeclared identifiers and invocations to pseudo-random number generators. The only identifiers that can occur in the reward expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification, together with the index possibly occurring at the beginning of the measure definition. An action type can occur at most once in the reward structure specified within a measure definition.

The second form is useful to concisely define several variants of the same reward assignment through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression and in the reward expression, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression. The index for the reward assignment must be different from the index possibly occurring at the beginning of the measure definition.
7.3 Syntax of .sim Specifications

A .sim specification is composed of five sections:

\[
\begin{align*}
&\text{<clock_act_type>} \\
&\text{<sim_run_length>} \\
&\text{<sim_run_number>} \\
&\text{<measure_def_sequence>} \\
&\text{[<trace_def_sequence>]} \\
\end{align*}
\]

7.3.1 Clock Action Type

The clock action type represents the action type on the basis of which time is assumed to progress during the simulation. Every execution of a transition labeled with the clock action type (or a type involving or renaming it) corresponds to a clock tick.

The clock action type is defined through the following syntax:

\[
"\text{RUN_LENGTH_ON_EXEC}" \text{<identifier>} ["\text{<expr>}"]\text{.} \text{<identifier>}
\]

which contains the identifier of an action type preceded by the identifier of an AEI possibly augmented with an integer-valued selector expression enclosed in square brackets, which must be free of undeclared identifiers and invocations to pseudo-random number generators. The AEI must be declared in the Æmilia specification to which the simulation-based performance evaluation is applied, and the action type must occur in the behavior of the type of the AEI within non-passive actions. The action type cannot be hidden or restricted in the Æmilia specification. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification.

7.3.2 Simulation Run Length

The simulation run length specifies the number of times that a transition labeled with the clock action type (or a type involving or renaming it) must be executed in order for a simulation run to be considered terminated.

The simulation run length is defined through the following syntax:

\[
"\text{RUN_LENGTH}" \text{<expr>}
\]

where the expression must be integer valued as well as free of undeclared identifiers and invocations to pseudo-random number generators. The only identifiers that can occur in the expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification to which the simulation-based performance evaluation is applied. The value of the expression must be greater than zero.

7.3.3 Simulation Run Number

The simulation run number specifies the number of independent simulation runs that have to be carried out in order for the simulation to be considered terminated.

The simulation run number is defined through the following syntax:

\[
"\text{RUN_NUMBER}" \text{<expr>}
\]
where the expression must be integer valued as well as free of undeclared identifiers and invocations to pseudo-random number generators. The only identifiers that can occur in the expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification to which the simulation-based performance evaluation is applied. The value of the expression must be between 1 and 30.

7.3.4 Measure Definition Sequence

The fourth section is a non-empty sequence of semicolon-separated measure definitions, each of the following form:

\[
\text{<measure_def>} ::= "\text{MEASURE}\ <\text{identifier}> \ [\{\ <\text{expr}> \}] \ "\text{IS}\ "\text{<measure_expr>}
| "\text{FOR\_ALL}\ <\text{identifier}> \ "\text{IN}\ "\text{<expr>} \ .. \ <\text{expr}>\ "\text{MEASURE}\ <\text{identifier}> \ [\{\ <\text{expr}> \}] \ "\text{IS}\ "\text{<measure_expr>}
\]

In its simpler form, a measure definition contains the identifier of the measure, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the measure expression. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification to which the simulation-based performance evaluation is applied.

The second form is useful to concisely define several variants of the same measure through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression and in the measure expression, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

We observe that the identifier of a measure can be augmented with a selector expression also in the simpler form of measure definition. This is useful whenever it is desirable to define a set of indexed variants of the same measure, but only some of them have a common selector expression.

The measure expression has the following syntax:

\[
\text{<measure_expr>} ::= "\text{MEAN}\ (\ <\text{sim_expr}> , \ <\text{expr}> .. \ <\text{expr}> )"
| "\text{VARIANCE}\ (\ <\text{sim_expr}> , \ <\text{expr}> .. \ <\text{expr}> )"
| "\text{DISTRIBUTION}\ (\ <\text{sim_expr}> , \ <\text{expr}> .. \ <\text{expr}> , \ <\text{expr}> )"
\]

where \text{<sim_expr>} is the expression whose mean, variance, or distribution has to be estimated during the simulation, while the other expressions, which must be integer valued as well as free of undeclared identifiers and invocations to pseudo-random number generators, delimit the observation interval within a simulation run. The first expression represents the beginning of the observation interval, whose value must be between zero and the simulation run length decremented by one. The second expression represents the end of the observation interval, whose value must be between one and the simulation run length, and greater than the value of the previous expression. The third expression, which is present only in the case of the distribution, represents the width of the subintervals – within the observation interval – at the end of which the distribution must be estimated. Its value must be greater than zero and a divisor of the length of the observation interval, which is given by the difference between the values of the two previous expressions. The only identifiers that can occur in these expressions are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification to which the simulation-based performance evaluation is applied, together with the index possibly occurring at the beginning of the measure definition.

The syntax for \text{<sim_expr>} is the same as the syntax for \text{<expr>}, with in addition the following reward-based production:

\[
\text{<sim_expr>} ::= "\text{REWARD}\ (\ "\text{EXECUTED}\ (\ "\text{<identifier>} \ [\{\ <\text{expr}> \}] \ "\text{.}
\text{<identifier>} \ "\rightarrow\ "\text{<reward_expr>} , \ "\text{<cumulative}> \ "\text{)\)"
\]

7.3 Syntax of .sim Specifications

The syntax of an action type preceded by the identifier of an AEI possibly augmented with an integer-valued selector expression enclosed in square brackets, which must be free of undeclared identifiers and invocations to pseudo-random number generators. The AEI must be declared in the Æmilia specification to which the simulation-based performance evaluation is applied, and the action type must occur in the behavior of the type of the AEI within non-passive actions. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification, together with the index possibly occurring at the beginning of the measure definition.

The meaning is that, whenever a transition labeled with the specified action type (or a type involving or renaming it) is executed, then a reward is earned whose value is given by the expression following symbol ->. All the values of the reward expression collected during a run are summed up at the end of the run – with this sum being divided by the number of collected values if the measure is not cumulative – then all the sums are involved in a statistical inference process at the end of the simulation in order to derive the measure estimate with 90% confidence level. The reward expression must be real valued as well as free of undeclared identifiers and invocations to pseudo-random number generators. The only identifiers that can occur in the reward expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification, together with the index possibly occurring at the beginning of the measure definition.

The syntax for <reward_expr> is the same as the syntax for <expr>, with in addition the following variable-based production:

\[
\text{<reward_expr>} \::= \text{<identifier>} \left[\left[ \text{<expr>} \right]\right] \text{.} <\text{identifier}> \text{.} <\text{identifier>}
\]

which contains the identifier of a variable formal parameter or local variable preceded by the identifier of a behavior, which is in turn preceded by the identifier of an AEI possibly augmented with an integer-valued selector expression enclosed in square brackets, which must be free of undeclared identifiers and invocations to pseudo-random number generators. The AEI must be declared in the Æmilia specification to which the simulation-based performance evaluation is applied, the behavior must be defined within the type of the AEI, and the variable formal parameter or local variable must be declared in the behavior header. Upon evaluation, this denotes the value hold in the variable formal parameter or local variable at the time of the evaluation. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification, together with the index possibly occurring at the beginning of the measure definition.

7.3.5 Trace Definition Sequence

The fifth section, which is optional, is a possibly empty list of semicolon-separated trace definitions, each of the following form:

\[
\text{<trace_def>} \::= \text{"DRAW" } <\text{trace_expr}> \text{"FROM" } <\text{trace_file_path}> \left[\left[ <\text{expr}> \right]\right] \text{.} <\text{.trc>}
\]

In its simpler form, a trace definition contains the trace expression to be sampled, the trace file path – without extension – from which the values for the trace expression are to be read during simulation, a possible integer-valued expression enclosed in square brackets, which represents a selector and must be free of undeclared identifiers and invocations to pseudo-random number generators, and the .trc extension. The only identifiers that can occur in the possible selector expression are the ones of the constant formal
parameters declared in the architectural type header of the Æmilia specification to which the simulation-based performance evaluation is applied.

The second form is useful to concisely define several variants of the same trace through an indexing mechanism. This additionally requires the specification of the index identifier, which can then occur in the selector expression, together with its range, which is given by two integer-valued expressions. These two expressions must be free of undeclared identifiers and invocations to pseudo-random number generators, with the value of the first expression being not greater than the value of the second expression.

The path of a trace file is relative to the directory containing the .sim specification, must start with ./, and must contain / (rather than \) as separator for directory names. The trace file path can be augmented with a selector expression also in the simpler form of trace definition. This is useful whenever it is desirable to associate different trace files with a set of indexed variants of the same trace expression belonging to different AEIs, but only some of them have a common selector expression.

The syntax for $\langle \text{trace_expr} \rangle$ is the same as the syntax for $\langle \text{expr} \rangle$, except that it must start with an invocation to a pseudo-random number generator and has the following constant-based production in place of the production for a simple identifier:

\[
\langle \text{trace_expr} \rangle ::= \langle \text{identifier} \rangle \text{["["} \langle \text{expr} \rangle \text{"]"]} \text{."} \langle \text{identifier} \rangle
\]

which contains the identifier of a constant formal parameter preceded by the identifier of an AEI possibly augmented with an integer-valued selector expression enclosed in square brackets, which must be free of undeclared identifiers and invocations to pseudo-random number generators. The AEI must be declared in the Æmilia specification to which the simulation-based performance evaluation is applied, and the constant formal parameter must be declared in the header of the type of the AEI. The overall trace expression must occur in the behavior of the type of some AEI of the Æmilia specification, and at most one trace file can be associated with it. Note that no variable formal parameter or local variable can occur in the trace expression. The only identifiers that can occur in the possible selector expression are the ones of the constant formal parameters declared in the architectural type header of the Æmilia specification, together with the index possibly occurring at the beginning of the trace definition.

### 7.4 Syntax of .trc Specifications

A .trc file must contain sufficiently many real numbers in fixed point notation, each starting at the beginning of a new line.

### 7.5 Example A: The Alternating Bit Protocol

In this section we evaluate the performance of the alternating bit protocol.

#### 7.5.1 Markovian Performance Evaluation

The performance measures of interest for the Æmilia specification abp.aem of Sect. 3.10.2 can be defined through the following abp.rew:

```plaintext
MEASURE throughput IS
    ENABLED(S.generate_msg) -> TRANS_REWARD(1);

MEASURE utilization IS
    ENABLED(LM.propagate_0) -> STATE_REWARD(1)
    ENABLED(LM.propagate_1) -> STATE_REWARD(1)
```
The throughput represents the number of messages that are delivered per unit of time. It is obtained by associating an instantaneous unit reward with the transitions originated from $S.\text{generate\_msg}$. Equivalently, it could have been obtained by associating a reward rate equal to the rate of $S.\text{generate\_msg}$ with every state in which $S.\text{generate\_msg}$ is enabled. The utilization represents instead the percentage of time during which the channel is busy because of message propagation. It is obtained by associating a unit reward rate with every state in which $LM.\text{propagate}\_0$ or $LM.\text{propagate}\_1$ is enabled.

The following is the result of the Markovian performance evaluation at steady state:

Stationary value of the performance measures for ABP_Type:

- Value of measure "throughput":
  1.88226

- Value of measure "utilization":
  0.26291

As we can see, the throughput is much less than the maximum potential value (i.e. the rate of $S.\text{generate\_msg}$) and the utilization is about 26%.

Similar results are obtained when considering the value passing Æmilia specification $abp.\text{vp.aem}$ of Sect. 3.10.3 in place of $abp.\text{aem}$, provided that the following $abp.\text{vp.rew}$ is used:

MEASURE throughput IS
  ENABLED(S.\text{generate\_msg}) -> TRANS_REWARD(1);

MEASURE utilization IS
  ENABLED(LM.\text{propagate}) -> STATE_REWARD(1)

### 7.5.2 Simulation-Based Performance Evaluation

The mean, variance, and distribution of the same performance measures as before can be defined for the Æmilia specification $abp.\text{gd.aem}$ with general delays of Sect. 3.10.4 through the following $abp.\text{gd.sim}$:

RUN_LENGTH_ON_EXEC
C.\text{elapse\_tick}

RUN_LENGTH
10000

RUN_NUMBER
20

MEASURE throughput_avg IS
  MEAN
  {
    REWARD(EXECUTED(MG.\text{generate\_msg}) -> 1,
    CUMULATIVE) / 10,
    0..10000
  };

MEASURE throughput_var IS
  VARIANCE
  {

REWARD(EXECUTED(MG.generate_msg) -> 1, CUMULATIVE) / 10, 0..10000 );

MEASURE throughput_distr IS DISTRIBUTION {
    REWARD(EXECUTED(MG.generate_msg) -> 1, CUMULATIVE) / 1, 0..10000, 1000
};

MEASURE utilization_avg IS MEAN {
    REWARD(EXECUTED(LM.propagate) -> 1, CUMULATIVE) / 10000, 0..10000
};

MEASURE utilization_var IS VARIANCE {
    REWARD(EXECUTED(LM.propagate) -> 1, CUMULATIVE) / 10000, 0..10000
};

MEASURE utilization_distr IS DISTRIBUTION {
    REWARD(EXECUTED(LM.propagate) -> 1, CUMULATIVE) / 1000, 0..10000, 1000
}

Note that the duration of each run corresponds to 10000 msec of execution of the protocol and that the throughput is expressed in number of messages delivered per second, hence the division by 10 instead of 10000. The distributions of the throughput and of the utilization are estimated at the end of each of the 10 seconds.

The following is the result of the simulation-based performance evaluation, where the 90% confidence intervals are shown in square brackets:

90% confidence estimate of the performance measures for ABP_GD_Type:

- Estimate of measure "throughput_avg":
  3.005 [2.75757, 3.25243]

- Estimate of measure "throughput_var":
  0.455237
- Estimate of measure "throughput_distr":
  3.25
  [2.80682, 3.69318]
  2.5
  [1.98826, 3.01174]
  3.05
  [2.46139, 3.63861]
  2.8
  [2.20989, 3.39011]
  3.25
  [2.64479, 3.85521]
  3
  [2.31652, 3.68348]
  3.2
  [2.65999, 3.74001]
  2.6
  [1.84376, 3.35624]
  3.75
  [3.24697, 4.25303]
  2.65
  [2.02863, 3.27137]

- Estimate of measure "utilization_avg":
  0.33745
  [0.31401, 0.36089]

- Estimate of measure "utilization_var":
  0.00408571
  [0.00233904, 0.00583238]

- Estimate of measure "utilization_distr":
  0.30735
  [0.255711, 0.358989]
  0.3047
  [0.253016, 0.356384]
  0.2883
  [0.219288, 0.357312]
  0.336
  [0.277625, 0.394375]
  0.36775
  [0.30015, 0.43535]
  0.3422
  [0.283319, 0.401081]
  0.373
  [0.317583, 0.428417]
  0.3199
  [0.253941, 0.385859]
  0.4162
  [0.36628, 0.46612]
  0.3191
  [0.262867, 0.375333]
7.6 Example B: The NRL Pump

In order to measure the bandwidth of the covert channel of the Æmilia specification nrl_pump.aem of Sect. 3.11.2, we use the following nrl_pump.rew:

\[
\begin{align*}
\text{MEASURE} & \quad \text{closed\_connections\_per\_time\_unit} \quad \text{IS} \\
& \quad \text{ENABLED}(\text{LW}\text{.send\_conn\_close}) \rightarrow \text{TRANS\_REWARD}(1); \\
\text{MEASURE} & \quad \text{aborted\_connections\_per\_time\_unit} \quad \text{IS} \\
& \quad \text{ENABLED}(\text{TLT}\text{.send\_conn\_exit}) \rightarrow \text{TRANS\_REWARD}(1)
\end{align*}
\]

The two measures above are strictly related to the connect/diconnect strategy that a malicious high user may exploit to pass confidential information to low users. The number of connections that can be closed or aborted per unit of time represents an estimate of how many bits can be leaked in a certain period. We recall that the low users can deduce the presence of the high users only if some connections are correctly terminated, as in that case the high users must have sent acknowledgments.

The following is the result of the Markovian performance evaluation at steady state:

Stationary value of the performance measures for NRL_Pump_Type:

- Value of measure "closed\_connections\_per\_time\_unit": 4.37617
- Value of measure "aborted\_connections\_per\_time\_unit": 2.27526

This means that a malicious high user can set up a one-bit covert channel by means of which the high user can leak about 6 bits per second.

7.7 Example C: Dining Philosophers

In the case of the Æmilia specification dining_philosophers.aem of Sect. 3.12.2, it is interesting to assess the degree of concurrency between non-adjacent philosophers, which can be expressed through the following dining_philosophers.rew:

\[
\begin{align*}
\text{MEASURE} & \quad \text{mean\_number\_eating\_philosophers} \quad \text{IS} \\
& \quad \text{FOR\_ALL} \ i \ \text{IN} \ 0..\text{philosopher\_num} - 1 \\
& \quad \text{ENABLED}(P[i]\text{.eat}) \rightarrow \text{STATE\_REWARD}(1)
\end{align*}
\]

The degree of concurrency is obtained by counting the number of philosophers that are eating in each state.

The following is the result of the Markovian performance evaluation conducted with the adaptive variant of symmetric stochastic over-relaxation at steady state when there are 10 philosophers:

Stationary value of the performance measures for LR_Dining_Philosophers_Type:

- Value of measure "mean\_number\_eating\_philosophers": 4.16684

This means that on average there are about 4 non-adjacent philosophers that are simultaneously eating at each instant.
Bibliography


