

Deciding equivalence properties in security protocols

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joint work with

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Security protocols

Google SSO

BAC (e-passport)

Helios (e-voting)

TLS 1.3 (prior ver.)

WPA2 (wifi)

Security protocols

Google SSO

 Armando *et al.* (2008)

BAC (e-passport)

 Chothia and Smirnov (2010)

Helios (e-voting)

 Cortier and Smyth (2011)

TLS 1.3 (prior ver.)

 Cremers *et al.* (2016)

WPA2 (wifi)

 Vanhoef and Piessens (2017)

Security protocols

The attacker...



Reads / Writes



Intercepts

But they do not need to...



Break cryptography



Use side channels

Security protocols

The attacker...



Reads / Writes



Intercepts



Break cryptography



Use side channels

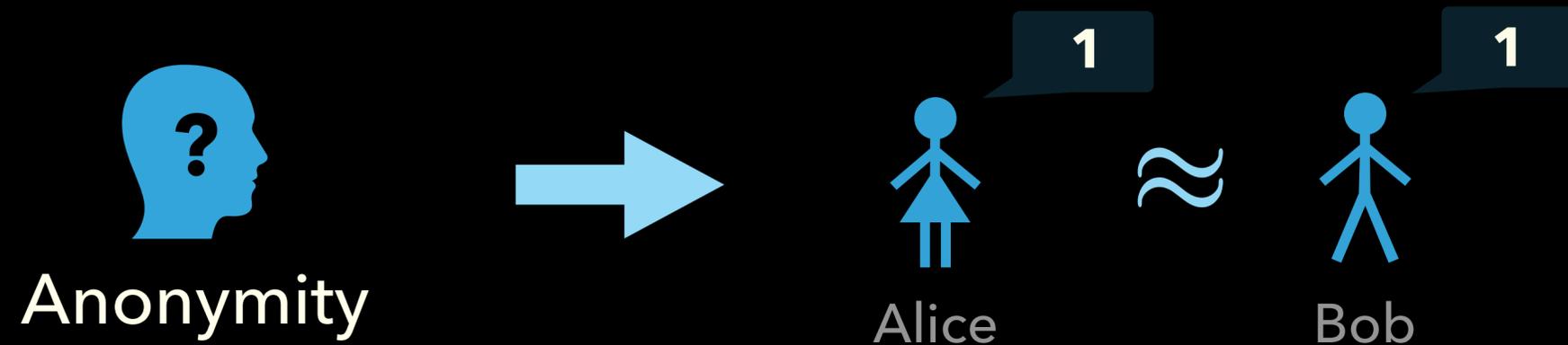
But they do not need to...

Dolev-Yao models

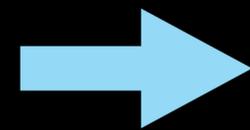
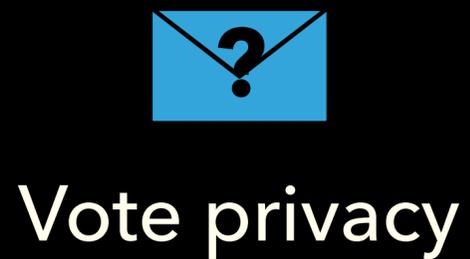
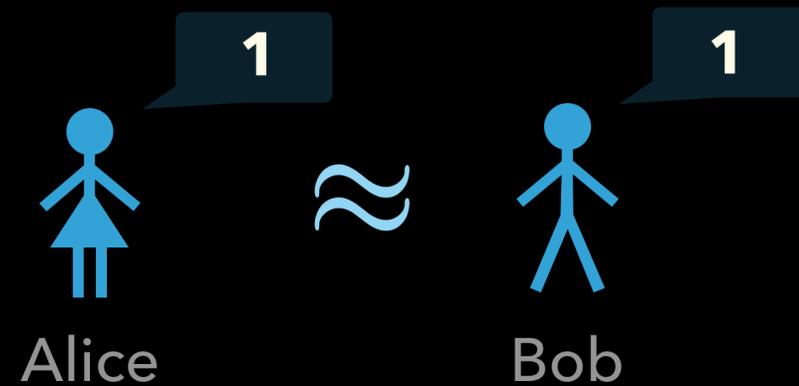
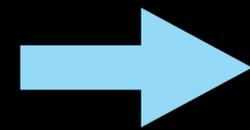
Concurrent systems where dishonest parties
have control over communications

but cryptography is idealised

Privacy = trace equivalence



Privacy = trace equivalence



Proving equivalence

for a fixed number of protocol sessions

Proving equivalence

for a fixed number of protocol sessions



Decidable

for subterm convergent crypto



coNEXP-complete

in the size of crypto equations + processes

Proving equivalence

for a fixed number of protocol sessions



Decidable

for subterm convergent crypto

Huge optimisations
for determinate processes



coNEXP-complete

in the size of crypto equations + processes

Problems of scalability
for non-determinate processes

Contributions

- ⊕ A refinement of trace equivalence
for processes with structural similarities
- ⊕ Lifting the optim. of determinate processes
to any process for this new equivalence
- ⊕ Reductions by symmetry

Refining trace equivalence

Performances (DEEPSEC)

Determinate

	#Agents	TIME
Wide-Mouth Frog (strong secrecy)	10	<1s ✓
	23	3s ✓
Denning-Sacco (strong secrecy)	7	<1s ✓
	29	6s ✓

Non-determinate

	#Agents	TIME
Helios Vanilla	6	<1s ⚡
Helios ZKP revote	11	2h 42min ✓
BAC	4	1s ⚡
(unlinkability)	6	>12h 🕒

✓ security property verified

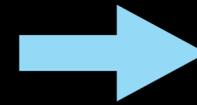
⚡ security property violated

🕒 timeout

Why this gap?

Determinate process. (simplified)

Parallel subprocess operate on
different communication channels



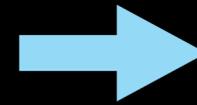
Partial-order reductions

Commutativity of
independent actions

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Partial-order reductions

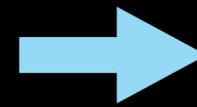
Commutativity of
independent actions

IDEA. Enforce independence natively, in the operational semantics

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Partial-order reductions

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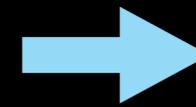
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$(\text{stickman} \parallel \text{woman}, \text{stickman} \parallel \text{woman})$

Why this gap?

Determinate process. (simplified)

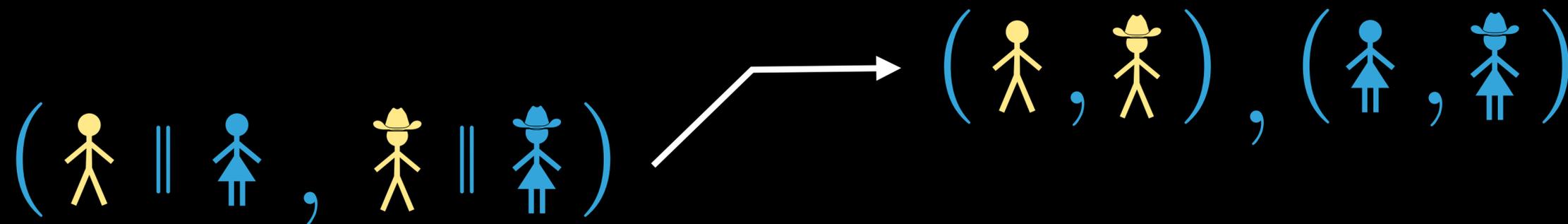
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Partial-order reductions

Commutativity of
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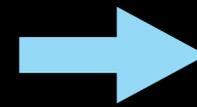
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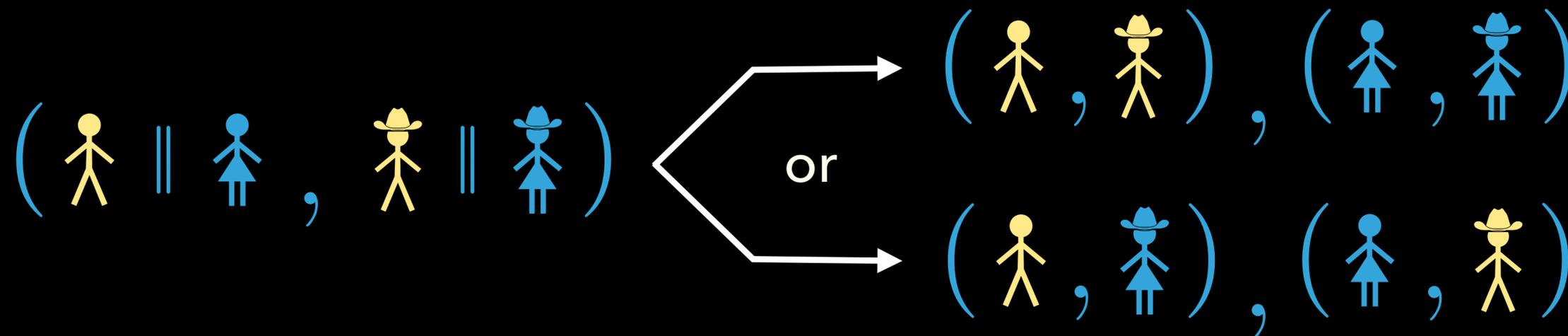
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Partial-order reductions

Commutativity of
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Equivalence by session

(MATCH)

$$(P_1 \parallel \dots \parallel P_n, Q_1 \parallel \dots \parallel Q_n) \longrightarrow (P_{\sigma(1)}, Q_1), \dots, (P_{\sigma(n)}, Q_n)$$

σ permutation of $\{1, \dots, n\}$

(EXEC)

$$(P, Q) \xrightarrow{\alpha} (P', Q') \quad \text{if } P \xrightarrow{\alpha} P' \text{ and } Q \xrightarrow{\alpha} Q'$$

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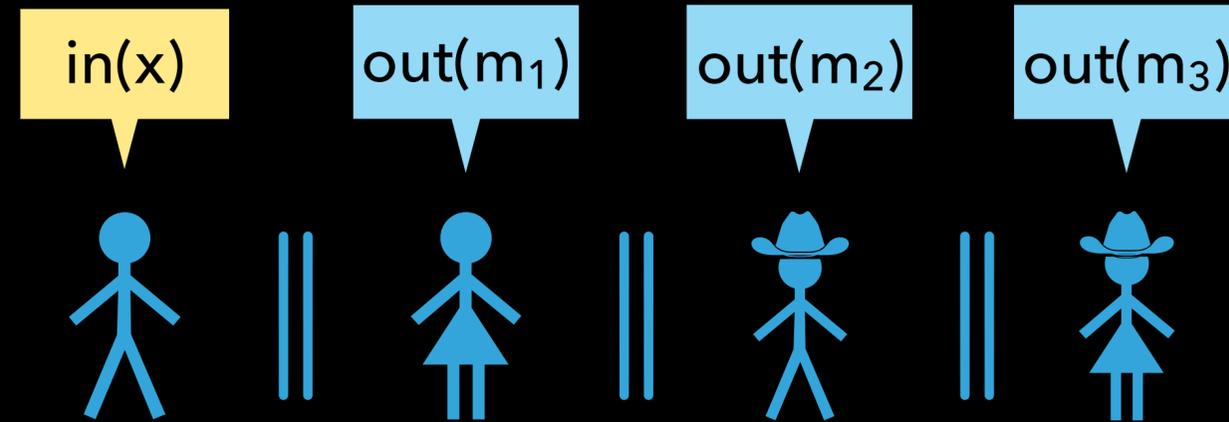
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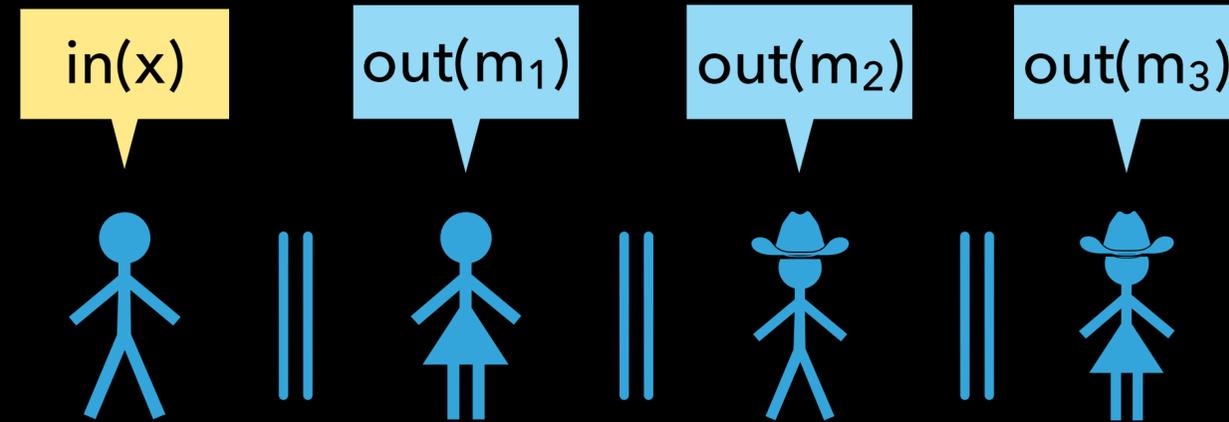
$$P \approx_s Q \quad \text{iff} \quad \text{Traces}(P) \sim \text{Traces}(P, Q) \sim \text{Traces}(Q)$$

Reducing the trace space

Partial-order reductions

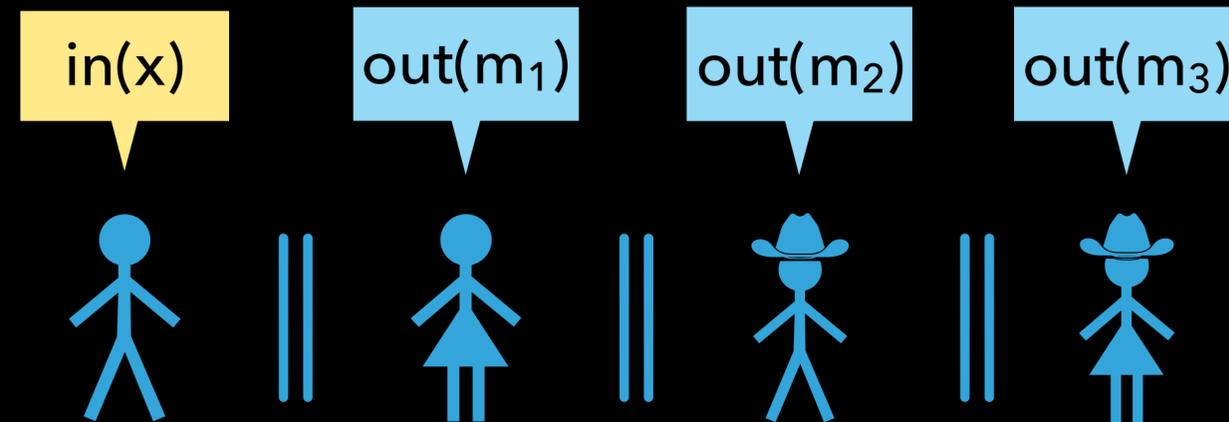


Partial-order reductions



IDEA. Perform first (in any order) actions that increase the attacker's knowledge

Partial-order reductions



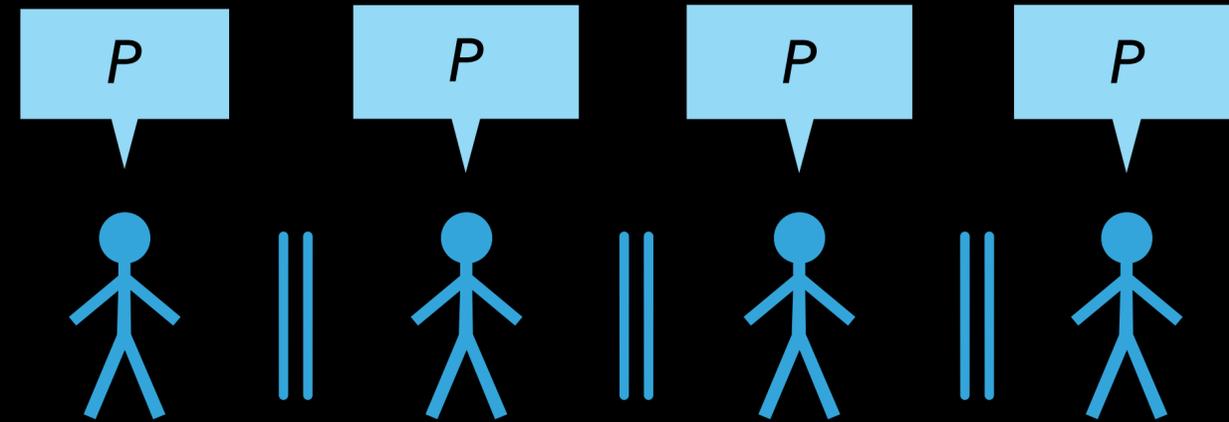
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In practice:

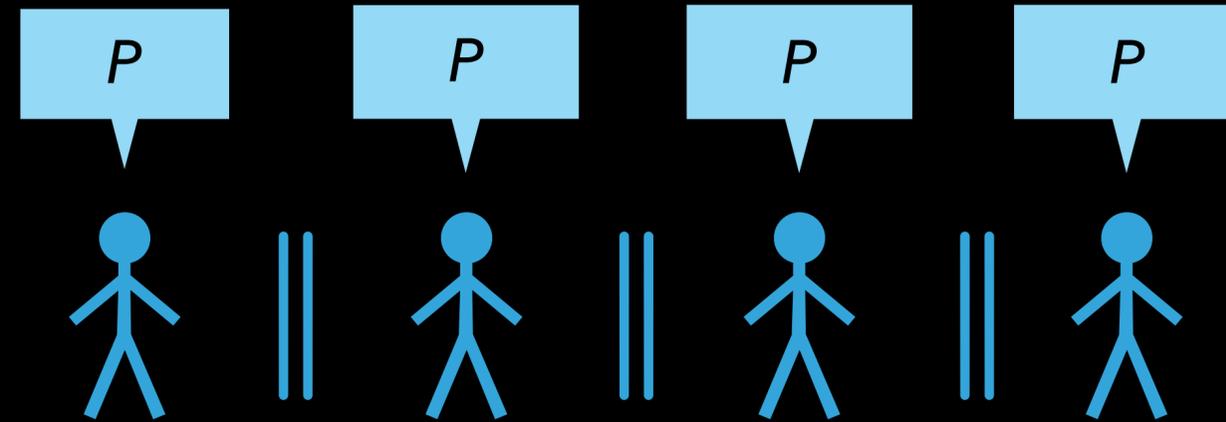
Only consider traces that alternate between

1. deterministic execution of all outputs
2. non-deterministic execution of 1 input

Symmetries

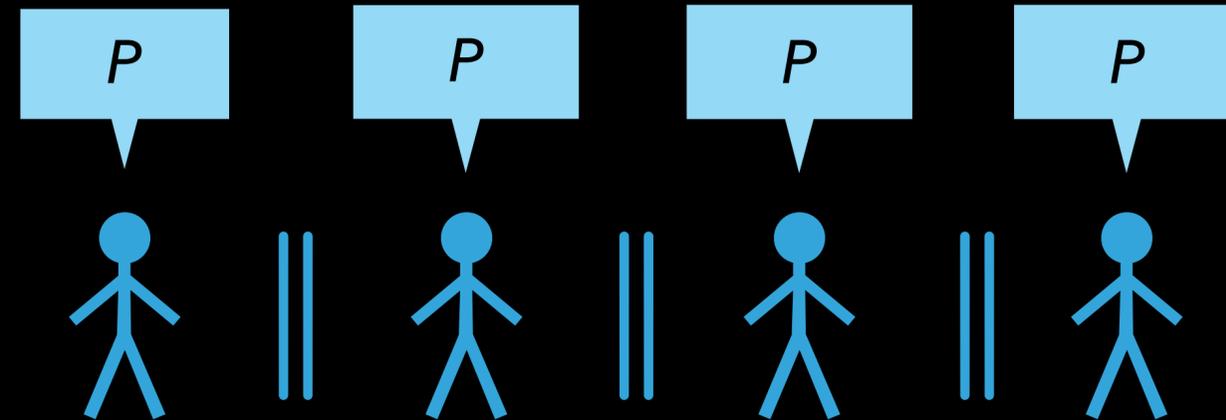


Symmetries



IDEA. Starting the trace with any of the copies of P makes no difference

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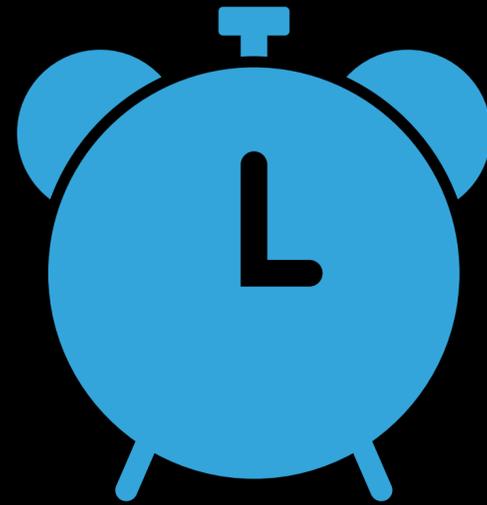
In practice:

In transitions $(P_1 \parallel \dots \parallel P_n, Q_1 \parallel \dots \parallel Q_n) \rightarrow (P_{\sigma(1)}, Q_1), \dots, (P_{\sigma(n)}, Q_n)$
only consider permutations σ up to the equivalence relation:

$$\sigma \sim \sigma' \quad \text{iff} \quad \exists u, v. \sigma' = u\sigma v \quad \text{and} \quad \forall i. P_{u(i)} = P_i, Q_{v(i)} = Q_i$$

Results

Experimental results



Work in progress

Conclusion

efficient detection of logical flaws in security protocols

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DONE

- + A refinement of trace equivalence
for lighter proofs in practical scenarios
- + Partial-order reductions
as a built-in mechanism of the new equivalence

FUTURE

- Implementation
in the DEEPSEC prover
- Catch false negatives