



ALMA MATER STUDIORUM  
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INFORMATICA - SCIENZA E INGEGNERIA

# A HYBRID APPROACH TO AUTOMATIC VERIFICATION OF CONCURRENT SYSTEMS

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# CONTENTS

presenting a technique for automatic verification of concurrent systems that has been used for designing analysis tools and demonstrating their correctness

the technique consists of

- \* associating behavioural types to programs that record relevant infos for a given property **implement a type inference system**
- \* define an analyzer of behavioural types or use off-the-shelf analyzers **not hard: resort to well-established theories**



# BIBLIO

- \* Cosimo Laneve, Luca Padovani: **An Algebraic Theory for Web Service Contracts**. *IFM* **2013**: 301-315; *Formal Aspects Comput.* 27(4): 613-640 (2015) finite transition systems
- \* Elena Giachino, Naoki Kobayashi, Cosimo Laneve: **Deadlock Analysis of Unbounded Process Networks**. *CONCUR* **2014**: 63-77; *Inf. Comput.* 252: 48-70 (2017) lams
- \* Abel Garcia, Cosimo Laneve, Michael Lienhardt: **Static analysis of cloud elasticity**. *PPDP* **2015**: 125-136; *Sci. Comput. Program.* 147: 27-53 (2017) presburger arithmetics eq.
- \* Elena Giachino, Einar Broch Johnsen, Cosimo Laneve, Ka I Pun: **Time Complexity of Concurrent Programs — A Technique Based on Behavioural Types**. *FACS* **2015**: 199-216; *J. Log. Algebraic Methods Program.* 105: 1-27 (2019) presburger arithmetics eq.
- \* Cosimo Laneve: **A Lightweight Deadlock Analysis for Programs with Threads and Reentrant Locks**. *FM* **2018**: 608-624; *Sci. Comput. Program.* 181: 64-81 (2019) lams
- \* Cosimo Laneve, Claudio Sacerdoti Coen: **Analysis of smart contracts balances**. In *Blockchain: Research and Applications*, vol 2(3) (2021) presburger arithmetics eq.
- \* Silvia Crafa, Cosimo Laneve: **Liquidity Analysis in Resource-Aware Programming**. *FACS* **2022**: 205-221 finite-length abstract computations

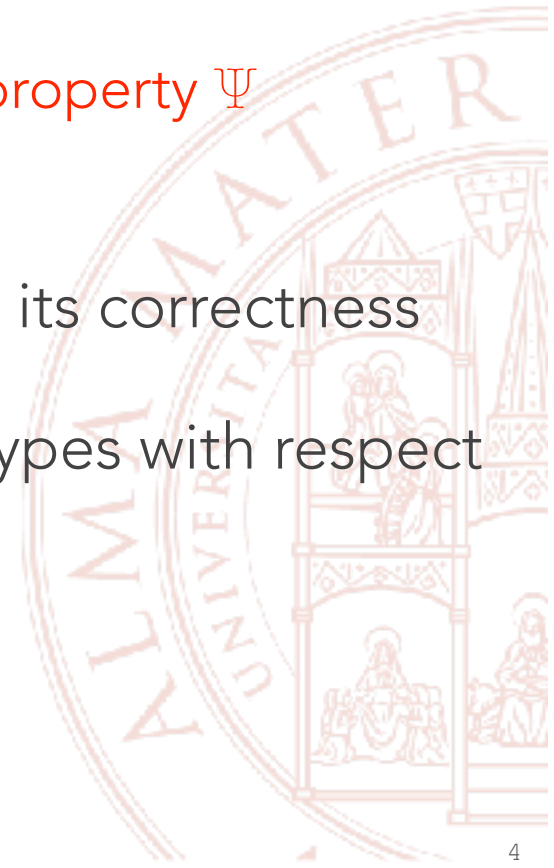
# THE TECHNIQUE IN DETAIL

INPUT: a programming language with an operational semantics  $\rightarrow$

demonstrate that a program  $P$  owns a property  $\Psi$

FIRST HALF: the behavioural type inference and its correctness

SECOND HALF: the correctness of behavioural types with respect to the property  $\Psi$



# THE TECHNIQUE IN DETAIL — THE FIRST HALF

## the behavioural type inference and its correctness

1. define **behavioural types** that are abstract specifications of programs detailed enough to verify  $\Psi$
2. define a **relation**, say  $\sqsupseteq$  and called *greater-than*, on behavioural types, e.g.  $\mathbb{b} \sqsupseteq \mathbb{b}'$
3. define an **inference system** such that  $\Gamma \vdash P : \mathbb{b}$   
**comments:** (1) there are as many rules as the syntactic constructs in the language  
(2) additional rules are needed for the runtime configurations of the program, c.f.  $\rightarrow$   
the difficulty of implementing  $\Gamma \vdash P : \mathbb{b}$  is the same of standard semantic analysis
4. THEOREM (**subject reduction**) if  $\Gamma \vdash P : \mathbb{b}$  and  $P \rightarrow P'$  then there are  $\Gamma', \mathbb{b}'$  such that  $\Gamma' \vdash P' : \mathbb{b}'$  and  $\mathbb{b} \sqsupseteq \mathbb{b}'$   
in standard type systems  $\mathbb{b} = \mathbb{b}'$

# THE TECHNIQUE IN DETAIL — THE SECOND HALF

## the correctness of behavioural types

5. define a property  $\Psi'$  over behavioural types and specify  $\mathbb{b} \Vdash \Psi'$

**comments:** (1)  $\Psi'$  is different from  $\Psi$  because behavioural types and programs have different models

(2) the algorithm for  $\mathbb{b} \Vdash \Psi'$  must terminate

(2) usually  $\mathbb{b}$  is either a finite model or one uses a terminating fixpoint technique

(3)  $\mathbb{b} \Vdash \Psi'$  requires no work if there is a well-established theory

6. demonstrate that, if  $\mathbb{b} \Vdash \Psi'$  and  $\mathbb{b} \sqsupseteq \mathbb{b}'$ , then  $\mathbb{b}' \Vdash \Psi'$

7. demonstrate that, if  $\Gamma \vdash P : \mathbb{b}$  and  $\mathbb{b} \Vdash \Psi'$  then  $P$  owns the property  $\Psi$

# A CASE STUDY

- \* Cosimo Laneve, Luca Padovani: **An Algebraic Theory for Web Service Contracts.** *IFM* **2013: 301-315**; *Formal Aspects Comput.* 27(4): 613-640 (2015) finite transition systems
- \* Elena Giachino, Naoki Kobayashi, Cosimo Laneve: **Deadlock Analysis of Unbounded Process Networks.** *CONCUR* **2014: 63-77**; *Inf. Comput.* 252: 48-70 (2017) lams
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# THE PROGRAMMING LANGUAGE — miniJava

\* programs in miniJava are  $(\mathbb{D}, P)$

\*  $\mathbb{D}$  is a finite set of **method name definitions**  $A(x_1, \dots, x_n) = P_A$

\*  $P$  is the **main process**

\* the syntax of  $P$  and  $P_A$  is

```
P ::= 0 | (v x) P | (v P) P | if e then P else P
      | A(e1, ..., en) | sync(x) { P }
```

```
e ::= x | v | e op e
```

in Java this is

```
Thread t = new Thread() { P };
t.start();
```

in Java this is

```
synchronized(x) { . . . }
```

\* you may write complex programs

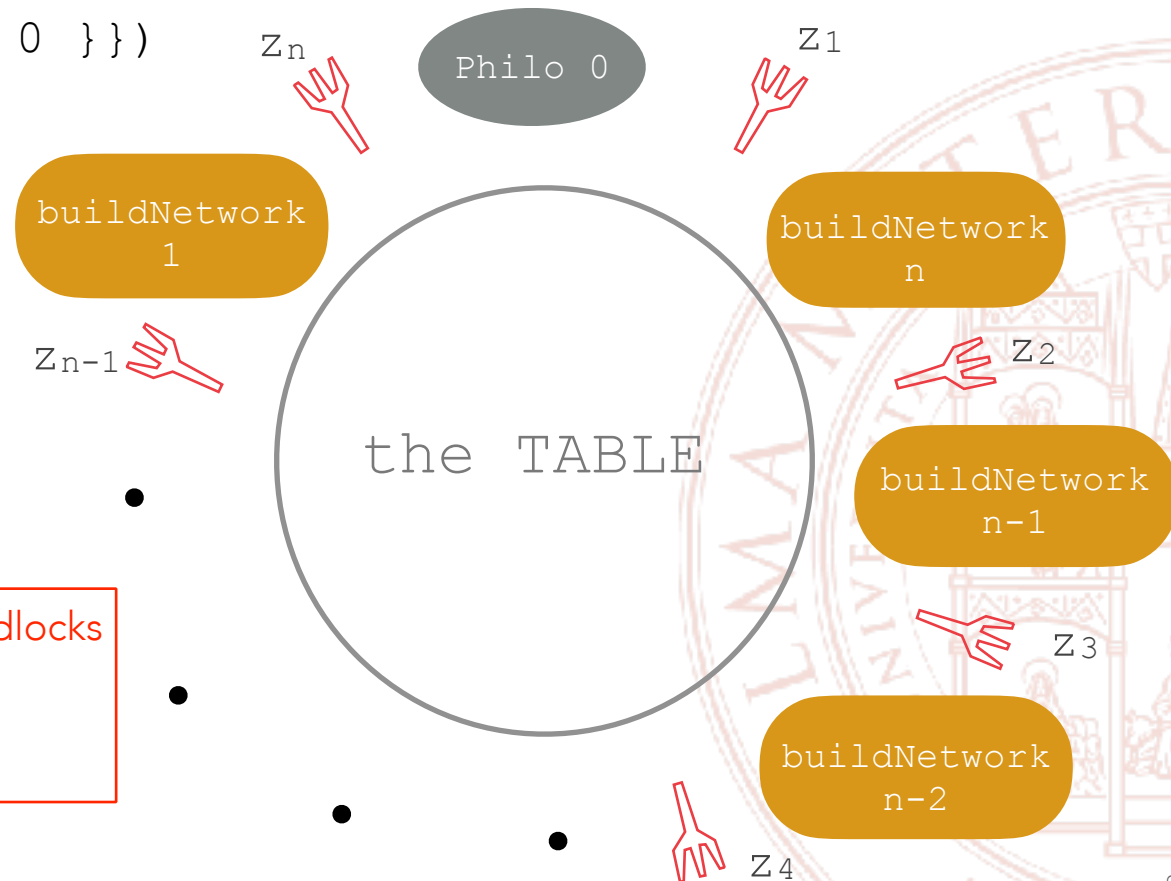


# THE DINING PHILOSOPHERS IN miniJava

\* you may write complex programs in miniJava:

```
buildNetwork(x,y,n) = (v z) (  
  if (n==1) then sync(x){sync(y){ 0 }}  
  else (v sync(x){sync(z){ 0 }}) buildNetwork(z,y,n-1)  
)
```

```
(v sync(zn){sync(z1){ 0 }})  
buildNetwork(z1,zn,n)
```



- **symmetric strategy**: possible deadlocks
- at least one Philo with a **different strategy**: no deadlocks

# THE OPERATIONAL SEMANTICS OF miniJava

\* program  $(\mathbb{D}, \mathbb{P})$

\* the initial state is  $P \bullet \varepsilon$ , generic states are  $P_1 \bullet \sigma_1 \mid \dots \mid P_n \bullet \sigma_n$

\* the operational semantics:

sequence of locks that have been acquired by  $P_1$

parallel threads

(ZERO)  
 $0 \bullet \sigma \longrightarrow$

(NEWO)  

$$\frac{z = \text{fresh}()}{(\nu x) P \bullet \sigma \mid \mathbb{P} \longrightarrow P\{z/x\} \bullet \sigma \mid \mathbb{P}}$$

(NEWT)  

$$(\nu P) Q \bullet \sigma \longrightarrow P \bullet \varepsilon \mid Q \bullet \sigma$$

(IFT)  

$$\frac{\llbracket e \rrbracket \neq 0}{\text{if } e \text{ then } P \text{ else } Q \bullet \sigma \longrightarrow P \bullet \sigma}$$

(IFF)  

$$\frac{\llbracket e \rrbracket = 0}{\text{if } e \text{ then } P \text{ else } Q \bullet \sigma \longrightarrow Q \bullet \sigma}$$

(CALL)  

$$\frac{\llbracket \bar{e} \rrbracket = \bar{v} \quad A(\bar{z}) = P}{A(\bar{e}) \bullet \sigma \longrightarrow P\{\bar{v}/\bar{z}\} \bullet \sigma}$$

(SYNC)  

$$\frac{x \notin \mathbb{P}}{\text{sync}(x)\{ P \} \bullet \sigma \mid \mathbb{P} \longrightarrow P \bullet \sigma \cdot x \mid \mathbb{P}}$$

reentrancy

# DEADLOCKS IN miniJava

a program  $(\mathbb{D}, \mathbb{P})$  is **deadlock-free** if, whenever

$$\mathbb{P} \bullet \varepsilon \rightarrow^* \mathbb{P} \quad \text{and} \quad \mathbb{P} = \text{sync}(x) \{ Q \} \bullet \sigma \mid \mathbb{P}'$$

then there is  $\mathbb{P}''$  such that  $\mathbb{P} \rightarrow \mathbb{P}''$

e.g.

- \*  $(\nu \text{ sync}(x) \{ \text{sync}(y) \{ 0 \} \}) \text{ sync}(y) \{ \text{sync}(x) \{ 0 \} \}$  deadlocks
- \*  $(\nu \text{ sync}(z_n) \{ \text{sync}(z_1) \{ 0 \} \}) \text{ buildNetwork}(z_1, z_n, n)$  deadlocks  
for every  $n$
- \*  $(\nu \text{ sync}(z_1) \{ \text{sync}(z_n) \{ 0 \} \}) \text{ buildNetwork}(z_1, z_n, n)$  never  
deadlocks

# LAMS

our behavioural types are **lams**

## lams define sets of dependencies

\* dependencies are relations containing pairs  $(x, y)$

\* the syntax is:

$$\ell = 0 \mid (x, y) \mid (\forall x) \ell \mid \ell \& \ell' \mid \ell + \ell' \mid \mathbf{A}(x_1, \dots, x_n)$$

\* a program is  $(\mathcal{L}, \ell)$  where  $\mathcal{L}$  are lam-function definitions

$$\mathbf{A}(x_1, \dots, x_n) = (\forall z_1, \dots, z_m) \ell$$

\* example of a lam-function:

$$\text{buildNetwork}(x, y) = (\forall z)((x, y) + (x, z) \& \text{buildNetwork}(z, y))$$

# LAMS — THE RELATION $\exists$

$$\ell \exists \ell'$$

- \* if  $\ell$  contains a function invocation  $\mathbf{A}(u_1, \dots, u_n)$
- \*  $\mathbf{A}(x_1, \dots, x_n) = (\forall z_1, \dots, z_m) \ell_A$  is in  $\mathcal{L}$
- \*  $\ell'$  is  $\ell$  where the invocation  $\mathbf{A}(u_1, \dots, u_n)$  has been replaced by  $\ell_A \{z_1', \dots, z_m' / z_1, \dots, z_m\} \{u_1, \dots, u_n / x_1, \dots, x_n\}$  with  $z_1', \dots, z_m'$  fresh variables

**example of  $\exists$ :**

$$\begin{aligned} & (y, x) \& \text{buildNetwork}(x, y) \\ \exists & (y, x) \& (x, y) + (y, x) \& (x, z_1) \& \text{buildNetwork}(z_1, y) \\ \exists & (y, x) \& (x, y) + (y, x) \& (x, z_1) \& [(z_1, y) + (z_1, z_2) \& \text{buildNetwork}(z_2, y)] \\ = & (y, x) \& (x, y) + (y, x) \& (x, z_1) \& (z_1, y) + (y, x) \& (x, z_1) \& (z_1, z_2) \& \\ & \text{buildNetwork}(z_2, y) \end{aligned}$$

# THE STATIC SEMANTICS OF miniJava

**Processes** –  $\{x_1 \cdot x_2 \cdots x_n\} = (x_1, x_2) \& \cdots \& (x_{n-1}, x_n) :$

$$\begin{array}{c} \text{(T-ZERO)} \\ \Gamma ; \sigma \vdash 0 : \{\sigma\} \end{array} \qquad \begin{array}{c} \text{(T-NEW)} \\ \Gamma, x : \text{Obj} ; \sigma \vdash P : \ell \quad x \notin \sigma \\ \hline \Gamma ; \sigma \vdash (\nu x) P : (\nu x) \ell \end{array}$$

$$\begin{array}{c} \text{(T-SYNC)} \\ \Gamma ; \sigma \cdot x \vdash P : \ell \\ \hline \Gamma ; \sigma \vdash \text{sync}(x)\{ P \} : \ell \end{array}$$

$$\begin{array}{c} \text{(T-IF)} \\ \Gamma \vdash e : \text{int} \quad \Gamma ; \sigma \vdash P : \ell \quad \Gamma ; \sigma \vdash P' : \ell' \\ \hline \Gamma ; \sigma \vdash \text{if } e \text{ then } P \text{ else } P' : \ell + \ell' \end{array}$$

$$\begin{array}{c} \text{(T-PAR)} \\ \Gamma ; \sigma \vdash P : \ell \quad \Gamma, u : \text{Obj} ; u \vdash Q : \ell' \\ \hline \Gamma ; \sigma \vdash (\nu Q) P : \ell \& (\nu u) \ell' \end{array}$$

$$\begin{array}{c} \text{(T-CALL)} \\ \Gamma \vdash \bar{u} : \overline{\text{Obj}} \quad \Gamma \vdash \bar{e} : \overline{\text{int}} \\ \hline \Gamma ; \sigma \vdash A(\bar{u}, \bar{e}) : A(\bar{u}) \& \{\sigma\} \end{array}$$

**Programs:**

$$\begin{array}{c} \text{(T-PROG)} \\ \left( u : \text{Obj} ; u \vdash P_A : \ell_A \right)^{A(\bar{x}, \bar{y}) = P_A \in \mathbb{D}} \quad \mathcal{L} = \bigcup_{A(\bar{x}, \bar{y}) = P_A \in \mathbb{D}} \{ A(u, \bar{x}) = \ell_A \} \\ \Gamma, u' : \text{Obj} ; u' \vdash P : \ell \\ \hline \Gamma \vdash (\mathbb{D}, P) : (\mathcal{L}, \ell) \end{array}$$

# THE SUBJECT REDUCTION THEOREM

judgments for states



if  $\Gamma \vdash \mathbb{P} : \ell$  and  $\mathbb{P} \rightarrow \mathbb{P}'$  then there are  $\Gamma', \ell'$  such that  
 $\Gamma' \vdash \mathbb{P}' : \ell'$  and  $\ell \cong \ell'$



# THE SECOND HALF: CIRCULAR DEPENDENCIES IN LAMS

example of  $\exists$ :

this is a **circular dependency**

this is also a **circular dependency**  
(by transitive closure)

$$\begin{aligned} & (y, x) \& \text{buildNetwork}(x, y) \\ \exists & (y, x) \& (x, y) + (y, x) \& (x, z_1) \& \text{buildNetwork}(z_1, y) \\ \exists & (y, x) \& (x, y) + (y, x) \& (x, z_1) \& [(z_1, y) + (z_1, z_2) \& \text{buildNetwork}(z_2, y)] \\ = & (y, x) \& (x, y) + (y, x) \& (x, z_1) \& (z_1, y) + (y, x) \& (x, z_1) \& (z_1, z_2) \& \\ & \text{buildNetwork}(z_2, y) \end{aligned}$$

a lam  $\ell$  has a **circularity** if there is  $\ell'$  such that  
 $\ell \exists \ell'$  and  $\ell'$  has a summand with a circular dependency

THEOREM: it is decidable whether a lam  $\ell$  has a **circularity** or not



# THE SECOND HALF: CIRCULAR DEPENDENCIES IN LAMS

absence of circularities in lams corresponds to deadlock freedom  
in `miniJava` processes

THEOREM: if  $\Gamma \vdash \mathbb{P} : \ell$  and  $\ell$  has **no circularity** then  $\mathbb{P}$  is  
**deadlock-free**



# CONCLUSIONS

1. type inference relates programs and behavioural types
2. behavioural type analysis allows us to demonstrate sensible properties on programs

