

A Stochastic Logic for Mobility and Global Computing

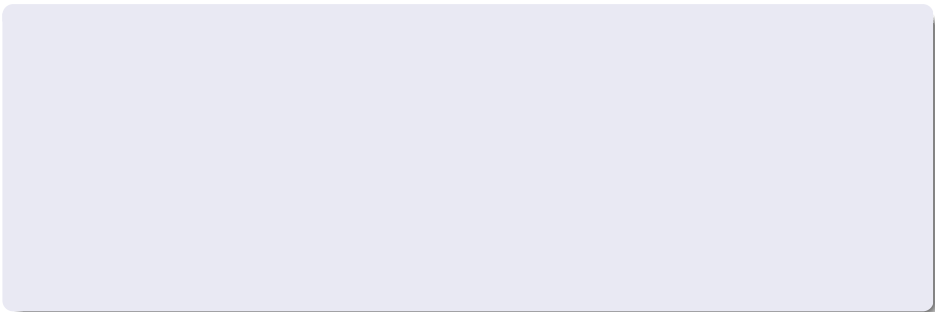
R. De Nicola², J.-P. Katoen¹, **Diego Latella**¹, M. Loreti², M. Massink¹

(1) Consiglio Nazionale delle Ricerche
Ist. di Scienza e Tecnologie dell'Informazione "A. Faedo"
Formal Methods && Tools Lab

(2) Univ. di Firenze
Dip. di Sist. e Inf.

PaCO

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- 1 STOKLAIM in one slide;

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- 2 MoSL: General;

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- 4 Example properties (Airbag);
- 5 Developments

KLAIM in one slide

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- *System:*

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Collection of **Sites** (i.e. **physical** addresses) with

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- **Processes** running

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- **Tuples** stored.

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Collection of nodes, each located at a specific site

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- Processes execute **actions**

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Collection of nodes, each located at a specific site

- Processes execute **actions**

- acting on local or remote sites

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Collection of nodes, each located at a specific site

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- acting on local or remote sites
- using **logical** addresses (locally mapped to physical ones)

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Collection of **Sites** (i.e. **physical** addresses) with

- **Processes** running
- **Tuples** stored.

- *System State (Network snapshot):*

Collection of nodes, each located at a specific site

- Processes execute **actions** which take time (*exp. dist. r.v.*)

- acting on local or remote sites
- using **logical** addresses (locally mapped to physical ones)

STOKLAIM in one (more) slide

- *Actions*

$$A ::= \mathbf{newloc}(!u) \mid \mathbf{out}(\vec{f})@l \mid \mathbf{in}(\vec{F})@l \mid \mathbf{read}(\vec{F})@l \mid \mathbf{eval}(P)@l$$

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- *Processes*

$$P ::= \mathbf{nil} \mid (A, r).P \mid P + P \mid P \mid P \mid X$$

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- *Networks*

$$N ::= \mathbf{0} \mid i ::_{\rho} P \mid i ::_{\rho} \langle \vec{f} \rangle \mid N \parallel N$$

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- *Stored Tuples*

$$\langle f_1, \dots, f_n \rangle \text{ with } f_j ::= v \mid P$$

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$$\langle f_1, \dots, f_n \rangle \text{ with } f_j ::= v \mid P$$

- *Patterns*

F_1, \dots, F_n as usual ...

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- ② both *action-* and *state*-based;
actions may bind variables

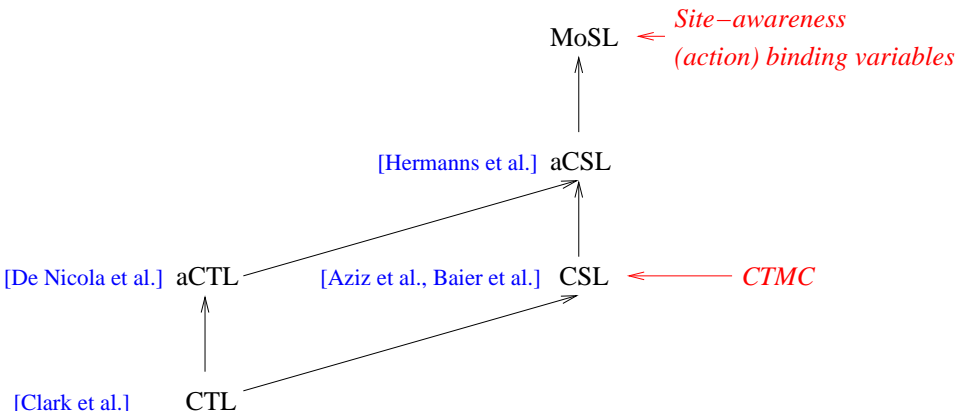
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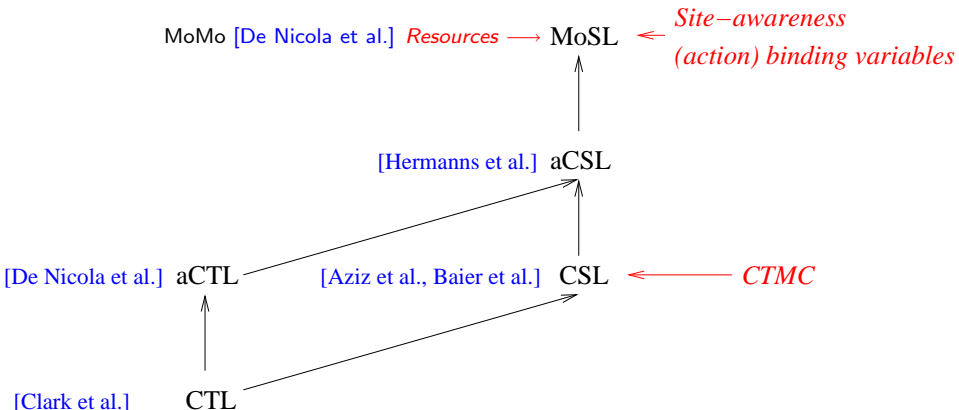
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- 3 a *real-time logic* (real-time bounds);
- 4 a *probabilistic logic* (performance and dependability aspects);
- 5 a *spatial logic* (spatial structure of the network);
- 6 a *resource-oriented logic* (GC open-endedness)

MoSL:General (cont'd)



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\mathcal{A}

\mathcal{A} ::=

MoSL: Atomic propositions

$\mathfrak{K} ::= \text{tt}$

MoSL: Atomic propositions

$$\mathfrak{A} ::= \text{tt} \mid Q@i$$

$$\mathfrak{A} ::= \text{tt} \mid Q@_i \mid \langle \vec{F} \rangle @_i .$$

$\aleph ::= \text{tt} \mid Q@l \mid \langle \vec{F} \rangle @l \ .$

Boot@A (satisfied if process *Boot* is ready to start at *A*)

$\aleph ::= tt \mid Q@l \mid \langle \vec{F} \rangle @l \ .$

Boot@*A* (satisfied if process *Boot* is ready to start at *A*)

<GO>@*A* (satisfied if value *GO* is stored at *A*)

MoSL: Action specifiers and action sets

In CTL

$$\Phi \quad \mathcal{U} \quad \Psi$$

MoSL: Action specifiers and action sets

In aCTL

$$\Phi \quad \Delta \mathcal{U} \Omega \quad \Psi$$

Δ, Ω : Sets of actions (uninterpreted, atomic)

MoSL: Action specifiers and action sets

In MoSL

$$\Phi \quad \Delta \mathcal{U} \Omega \quad \Psi$$

Δ, Ω : Sets of *action specifiers*, to be matched against KLAIM actions

MoSL: Action specifiers and action sets (cont'd)

init : o(*GO*, *A*)

Satisfied by any action executed at site *init*, by means of which a process uploads value *GO* to site *A*;

MoSL: Action specifiers and action sets (cont'd)

$init : o(GO, A)$

Satisfied by any action executed at site *init*, by means of which a process uploads value *GO* to site *A*;

$!z_1 : o(GO, !z_2)$

Satisfied by any action, executed at some site (z_1), by means of which a process uploads value *GO* to some site (z_2);

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$\Delta = \{\xi_1, \dots, \xi_n\}$ satisfied by any action satisfying any of ξ_j ;

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\top : satisfied by *any* action.

MoSL: Action specifiers and action sets (cont'd)

ACTION SPECIFIER	IS SATISFIED BY
$g_1 : \mathbf{O}(\vec{F}, g_2)$	any out action, executed at a site i_1 matching g_1 , uploading a tuple \vec{f} matching \vec{F} to a site i_2 matching g_2
$g_1 : \mathbf{I}(\vec{F}, g_2)$	any in action, executed at a site i_1 matching g_1 , downloading a tuple \vec{f} matching \vec{F} from a site i_2 matching g_2
$g_1 : \mathbf{R}(\vec{F}, g_2)$	any read action, executed at a site i_1 matching g_1 , reading a tuple \vec{f} matching \vec{F} from a site i_2 matching g_2
$g_1 : \mathbf{E}(F, g_2)$	any eval action, executed at a site i_1 matching g_1 , spawning a process P matching F to a site i_2 matching g_2
$g_1 : \mathbf{N}(g_2)$	any newloc action executed at a site i_1 matching g_1 , creating a node with physical address i_2 matching g_2

$$\Phi \ \Delta \ \mathcal{U}_{\Omega}^{<t} \ \Psi$$

- Satisfied by those paths where eventually a Ψ -state is reached, by time t , via a Φ -path, *and*, in addition, while evolving between Φ states, actions are performed satisfying Δ and the Ψ -state is entered via an action satisfying Ω .

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MoSL: State formulae

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MoSL: State formulae

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$\langle \vec{F} \rangle @ \iota \rightarrow \Phi$ *consumption*

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$$\langle \vec{f} \rangle @ \iota \leftarrow \Phi$$

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$\langle \vec{f} \rangle @ \iota \leftarrow \Phi$ *production*

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$$\mathcal{P}_{\bowtie p}(\varphi)$$

with $\bowtie \in \{<, >, \leq, \geq\}$ and $p \in [0, 1]$

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$$\mathcal{P}_{\bowtie p}(\varphi) \mid$$

$$\mathcal{S}_{\bowtie p}(\Phi)$$

with $\bowtie \in \{<, >, \leq, \geq\}$ and $p \in [0, 1]$

State Formulae Satisfaction relation

$$s \models \langle \vec{F} \rangle @ \iota \rightarrow \Phi \quad \text{iff} \quad s \equiv \iota ::_{\rho} \langle \vec{f} \rangle \parallel s', \text{match}(\vec{F}, \vec{f}) = \theta, \text{ and } s' \models \Phi$$

$$s \models \langle \vec{f} \rangle @ \iota \leftarrow \Phi \quad \text{iff} \quad s \equiv \iota ::_{\rho} \mathbf{nil} \parallel s' \text{ and } \iota ::_{\rho} \langle \vec{f} \rangle \parallel s \models \Phi$$

$$s \models \mathcal{P}_{\bowtie p}(\varphi) \quad \text{iff} \quad \mathbf{IP}\{\pi \in \text{Paths}(s) \mid \pi \models \varphi\} \bowtie p$$

$$s \models \mathcal{S}_{\bowtie p}(\Phi) \quad \text{iff} \quad \lim_{t \rightarrow \infty} \mathbf{IP}\{\pi \in \text{Paths}(s) \mid \pi[t] \models \Phi\} \bowtie p$$

Path Formulae Satisfaction relation

$\pi \models \Phi \Delta \mathcal{U}_{\Omega}^{\leq t} \Psi$ if and only if there exists $k, 0 < k \leq \text{len}(\pi)$ s.t.:

- ① $\sum_{j=0}^{k-1} \text{time}(\pi, j) < t$
- ② there exists Θ_{k-1} s.t.:
 - ① $\text{state}(\pi, k-1) \models \Phi$,
 - ② $\text{act}(\pi, k-1), \Theta_{k-1} \models \Omega$,
 - ③ $\text{state}(\pi, k) \models \Psi \Theta_{k-1}$
- ③ if $k > 1$ there exist $\Theta_0, \dots, \Theta_{k-2}$ s.t. for all $j, 0 \leq j \leq k-2$:
 - ① $\text{state}(\pi, j) \models \Phi$,
 - ② $\text{act}(\pi, j), \Theta_j \models \Delta$

$\gamma, \Theta \models \top$

$\gamma, \Theta \models \{\xi_1, \dots, \xi_n\}$ iff there exists $0 < j \leq n$ s.t. $\gamma, \Theta \models \xi_j$

$\gamma, \Theta \models \xi$ iff $\text{match}(\xi, \gamma) = \Theta$

MoSL: Examples

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- If, in the current state, there is a request for a $S2$ -type service placed on site A , the probability that such a request gets served within 72.04 time-units is at least 0.85:

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- In equilibrium, the probability is at least 0.87 that in at least 75% of the cases a $S1$ -type request is placed at site A within 500 time units:

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$$\langle S2 \rangle @ A \Rightarrow P_{\geq 0.85}(\text{tt} \top \mathcal{U}_{\{A:I(S2,A)\}}^{<72.04} \text{tt})$$

- In equilibrium, the probability is at least 0.87 that in at least 75% of the cases a $S1$ -type request is placed at site A within 500 time units:

$$S_{\geq 0.87}(P_{\geq 0.75}(\text{tt} \top \mathcal{U}_{\{!z:\mathbf{O}(S1,A)\}}^{<500} \text{tt}))$$

The Airbag scenario - Sensoria D8.0

When an accident occurs to a car registered with the Accident Assistance Service and the airbag of the car deploys, the following happens. First, an automated message is sent to the Accident Assistance Server which contains the vehicle's GPS data, the vehicle identification number and a collection of sensor data. Then, the Accident Assistance Server places a call to the driver's mobile phone. If, due to his injuries, the driver is unable to answer the call, and the severity of the accident is confirmed also by the sensor data, the emergency services are alerted and the vehicle location is communicated to them. Incoming cars are alerted as well.

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- If the driver does not answer the phone call, the emergency services are alerted *anyway*.
- Alerting cars which are approaching the accident area *not considered*.

Modelling assumptions

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- Each entity of interest is (assumed modeled as a STOKLAIM site and is) provided with its physical address.
 - Accident Assistance Server address: *AccAssSrv*,
 - Phone Server address: *PhSrv*,
 - Emergency Server address: *EmSrv*,
 - Each car has its own address.

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storing $(CarID, GPSTData, SenData) @ AccAssSrv$

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- Placing a phone-call: storing the phone number to site *PhSrv*

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- $PhNr : CID \rightarrow PhN$; $PhNr(carID) = carID$ driver's mobile phone nr.
- Answering a phone-call: removing the phone number from site *PhSrv*

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 - Accident Assistance Server address: *AccAssSrv*,
 - Phone Server address: *PhSrv*,
 - Emergency Server address: *EmSrv*,
 - Each car has its own address.
- Each car is uniquely identified by a car identifier $CarID \in CID$, finite.
- Accident notification:
storing $(CarID, GPSData, SenData) @ AccAssSrv$
- $PhNr : CID \rightarrow PhN$; $PhNr(carID) = carID$ driver's mobile phone nr.
- Answering a phone-call: removing the phone number from site *PhSrv*
- The Accident Assistance Server alerts the Emergency Server by uploading the GPS data to site *EmSrv*.

Guaranteeing acceptable timing for the detection of an accident which seriously injured the driver and for rescue alerting.

Performance (Response time)

Suppose it has been detected that an accident involving car *car_id* has taken place and that the driver is seriously injured

Ideal Requirement:

Emergency Service alerted within maximal time *t_alert*

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■-property:

$$\mathcal{P}_{\geq 0.997}(\top \diamond^{< t_alert} \{AccAssSrv: \mathbf{O}((car_id, gps), EmSrv)\} \text{tt})$$

Performance (Response time, cont'd)

Focus on those states reached after a phone call has been placed to the driver mobile phone, and nobody has answered for a given period of time, t_{answ} .

Ideal Requirement:

It should never happen that the phone is ringing for t_{answ} time units without a ■-state being reached.

Performance (Response time, cont'd)

Focus on those states reached after a phone call has been placed to the driver mobile phone, and nobody has answered for a given period of time, t_{answ} .

Realistic Requirement:

In at most 0.2% of the cases the phone is ringing for t_{answ} time units without a ■-state being reached.

Performance (Response time, cont'd)

Focus on those states reached after a phone call has been placed to the driver mobile phone, and nobody has answered for a given period of time, t_{answ} .

Realistic Requirement:

In at most 0.2% of the cases the phone is ringing for t_{answ} time units without a ■-state being reached.

■-property:

$$\mathcal{P}_{<0.002}(\langle PhNr(car_id) \rangle @ PhSrv \top \mathcal{U}^{[t_{answ}, t_{answ}]} \neg \blacksquare)$$

Performance (Response time, cont'd)

Consider now the situation in which an accident has been just notified.

Ideal Requirement:

A phone call is placed to the driver mobile phone with a delay of at most t_{call} time units, bringing to a ■-state.

Performance (Response time, cont'd)

Consider now the situation in which an accident has been just notified.

Realistic Requirement:

In at least 99.8% of the cases, a phone call is placed to the driver mobile phone with a delay of at most t_{call} time units, bringing to a ■-state.

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Acceptable Behaviour

REQUIREMENT:

Ideal Requirement:

The system does not behave *unacceptably*, after an accident has been notified.

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Realistic Requirement:

The probability that the system behaves *unacceptably*, after an accident has been notified, is less than 0.004.

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FINAL property:

$$\mathcal{P} < 0.004 \left(\top \diamond \{!car_addr:0(!car_id,!gps,!sdata),AccAssSrv\} \neg \blacksquare \right)$$

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$$\mathcal{P} < 0.002 \left(\langle PhNr(car_id) \rangle @ PhSrv \top \mathcal{U}^{[t_answ, t_answ]} \neg \blacksquare \right)$$

$$\mathcal{P} \geq 0.997 \left(\top \diamond \langle t_alert \right. \\ \left. \{ AccAssSrv : \mathbf{O}((car_id, gps), EmSrv) \} \text{tt} \right)$$

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Performance (Response time, cont'd)

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$$\mathcal{P} \leq 0 \left(\top \square \neg \langle \langle !car_id, !gps, !sdata \rangle \rangle @ AccAssSrv \right)$$

Performance (Response time, cont'd)

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Periodic testing the system with *fake* accident notifications

Performance (Response time, cont'd)

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Liveness of diagnostic routines:

Performance (Response time, cont'd)

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Availability

Assume furthermore that the presence of token *FAULT* at address *AccAssSrv* signals that the Accident Assistance Server is down.

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$$\mathcal{S}_{>0.99}(\neg(\langle FAULT \rangle @ AccAssSrv))$$

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$$\mathcal{P}_{\boxtimes p}(\neg(\langle ERR003 \rangle @ AccAssSrv) \uparrow \mathcal{U}^{[t,t]} \langle ERR003 \rangle @ AccAssSrv).$$

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$$\mathcal{P}_{\bowtie p}(\neg(\langle ERR003 \rangle @ AccAssSrv) \dashv\vdash \mathcal{U}^{[t,t']} \langle ERR003 \rangle @ AccAssSrv).$$

- $\mathcal{U}^{[t,t']}$ generalises $\mathcal{U}^{<t}$
- model-checking $\mathcal{P}_{\bowtie p}(\varphi)$ automatically returns also $\mathbb{P}(\{\pi \mid \pi \models \varphi \text{ and } \pi \text{ from } s\})$ for all states s .

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Implementation of a model-checking algorithm for full MoSL *which uses* CSL model-checkers (MRMC)

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 - StoKLAIM uIMC semantics plus CTMDP model-checking.

- StoKlaim simulation and reachability graph generation.
- StoKLAIM \models MoSL verification
- implemented in OCaml
 - OCaml provides mechanisms for interoperability with the C language
 - these primitives are used for interacting with MRMC (computing *steady* and *path* probabilities)
- The tool is still at a prototype level
 - systems with about 10^6 states can be handled

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